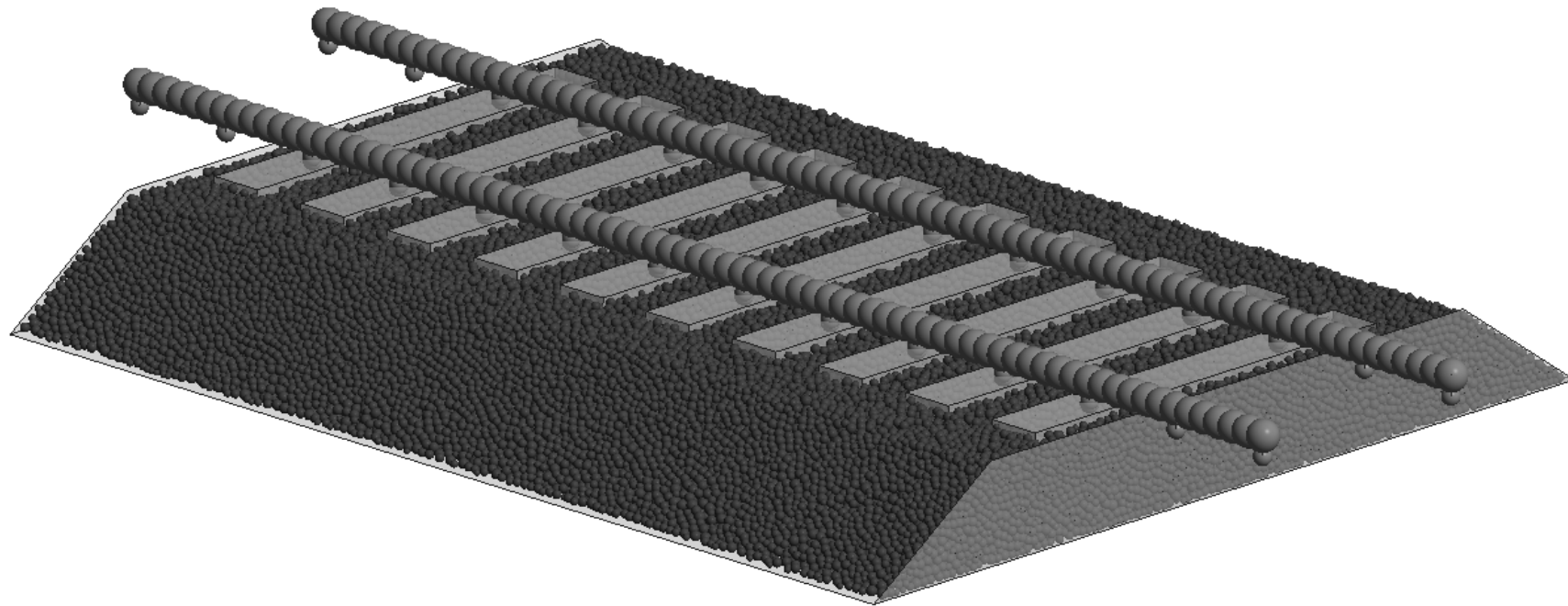


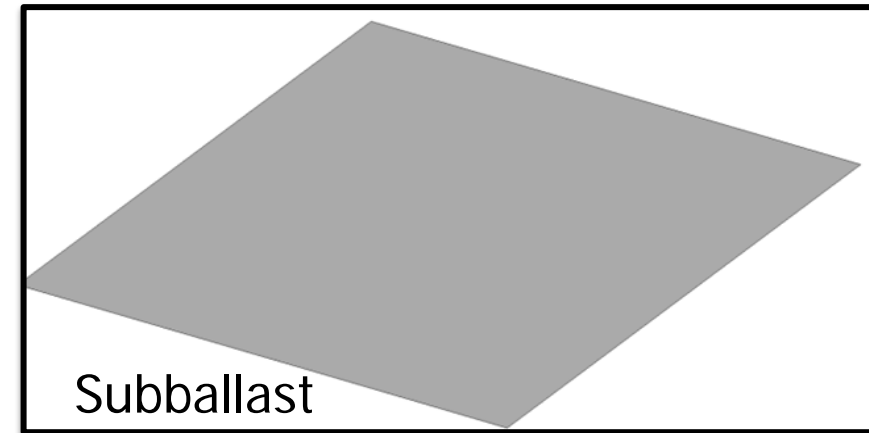
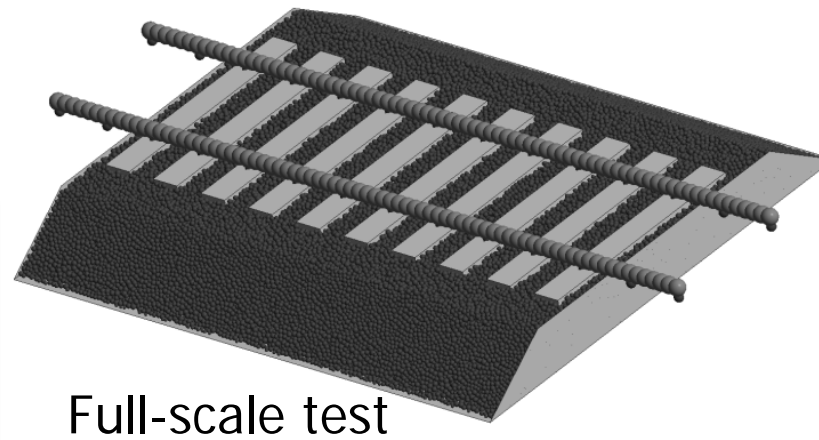
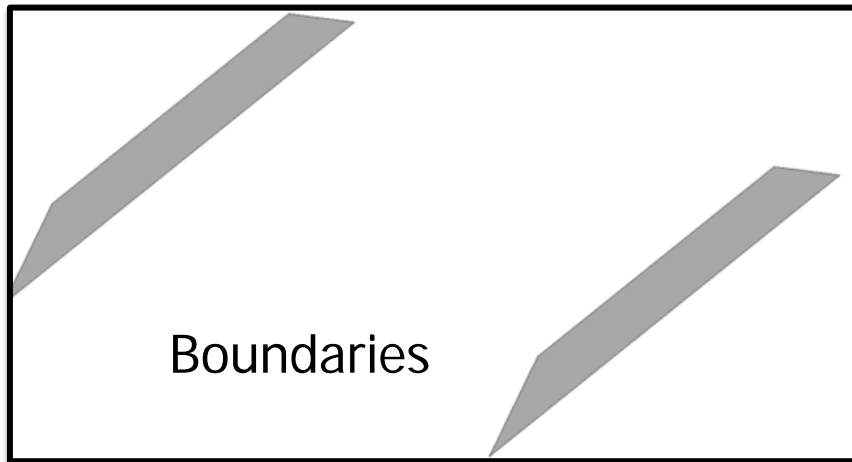
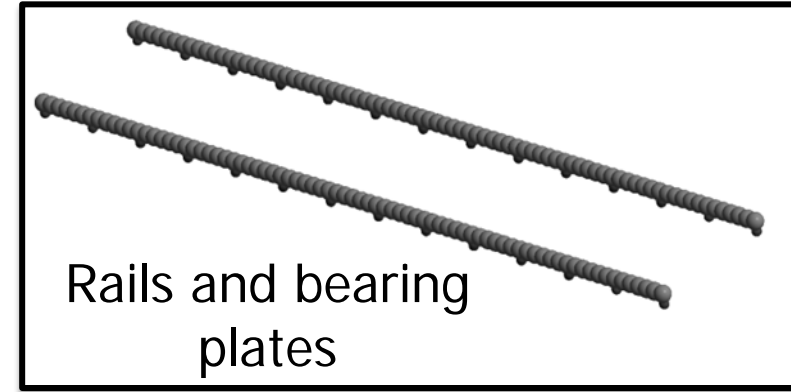
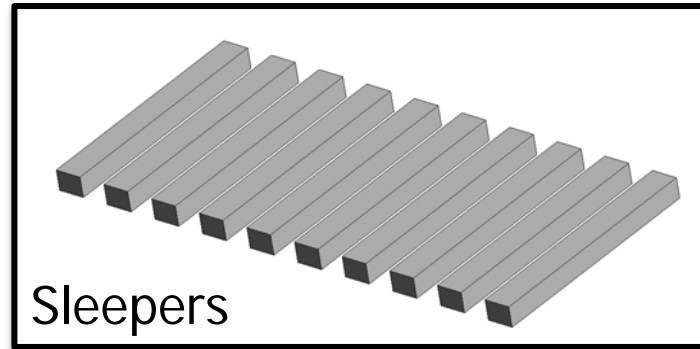
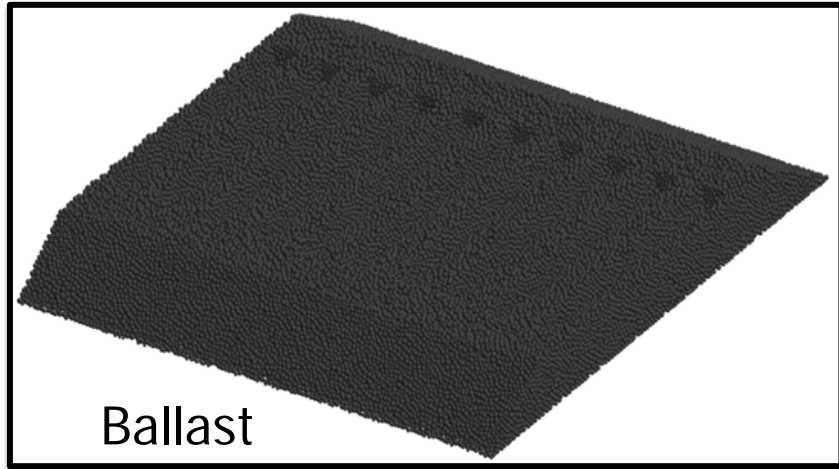
Full-scale numerical calculation of ballasted tracks with the Discrete Element Method



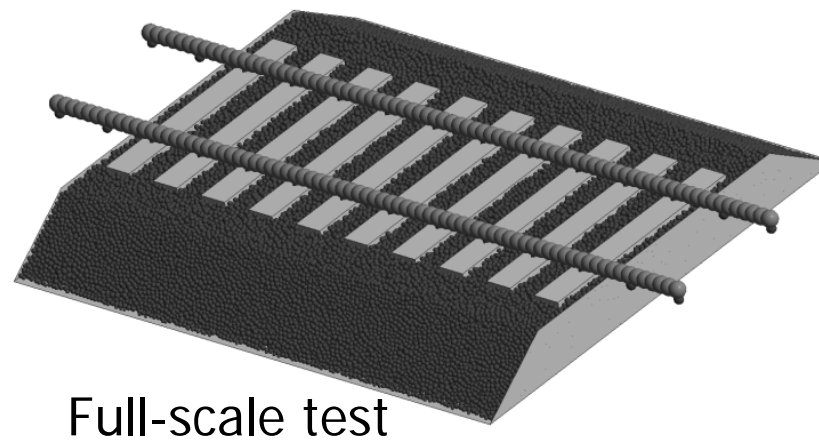
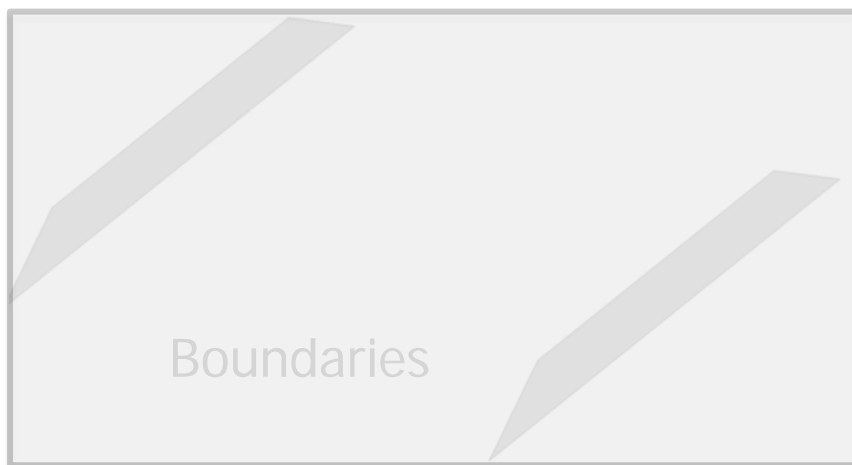
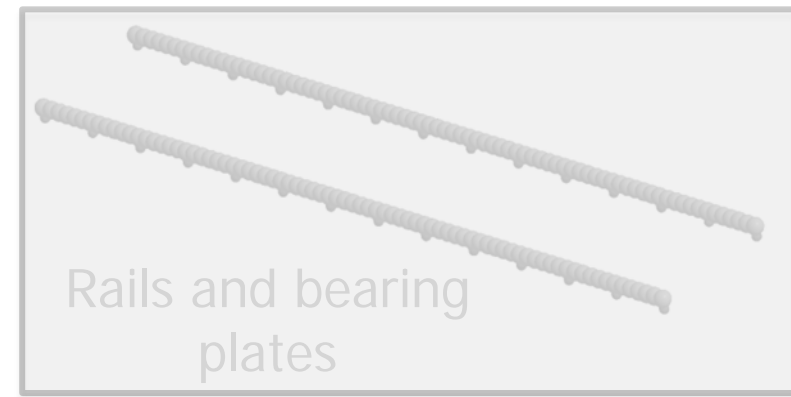
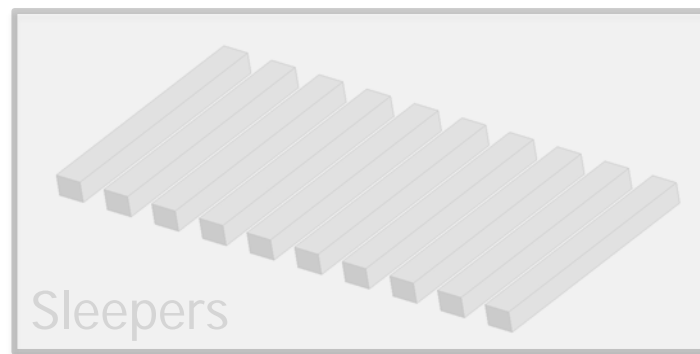
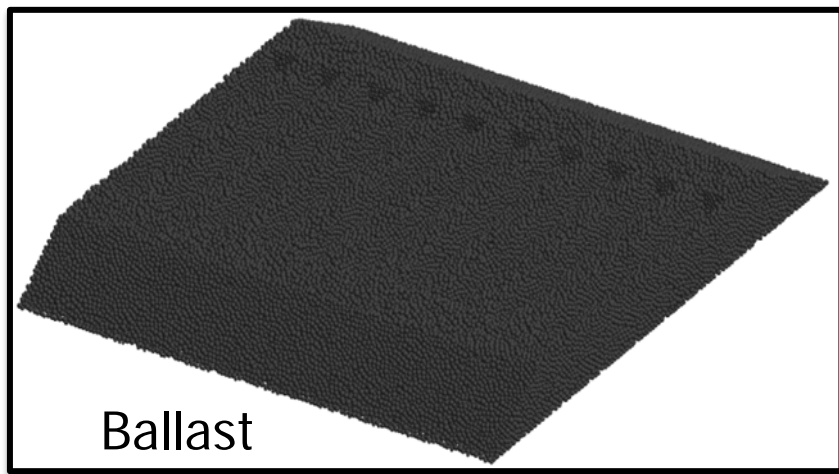
Joaquín Irazábal, Fernando Salazar and Eugenio Oñate



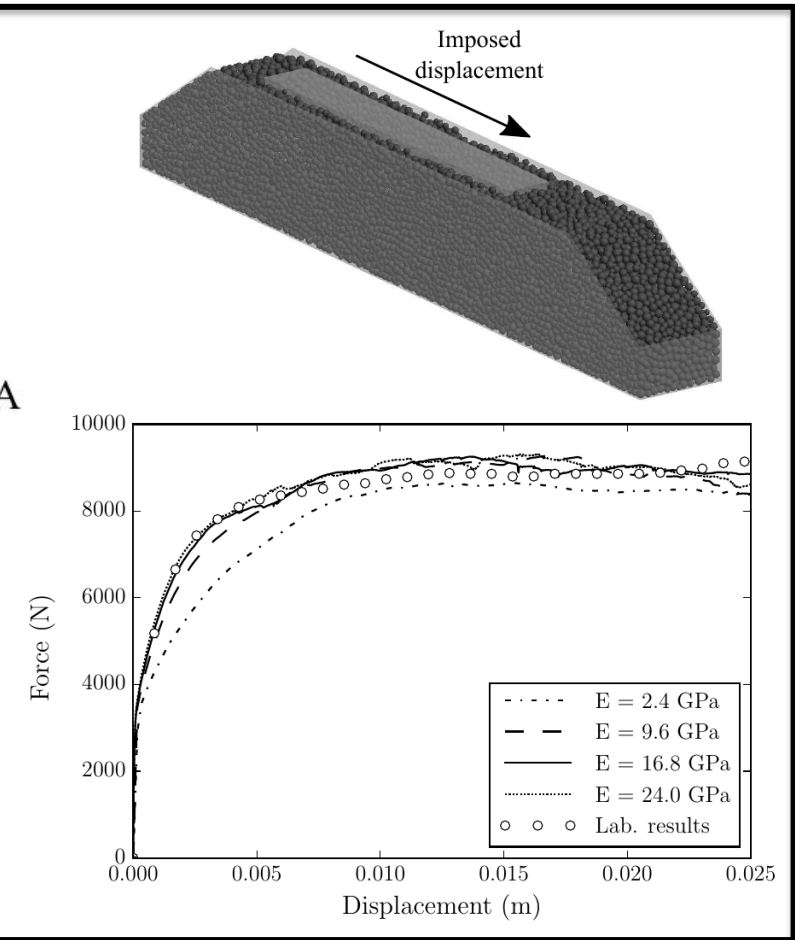
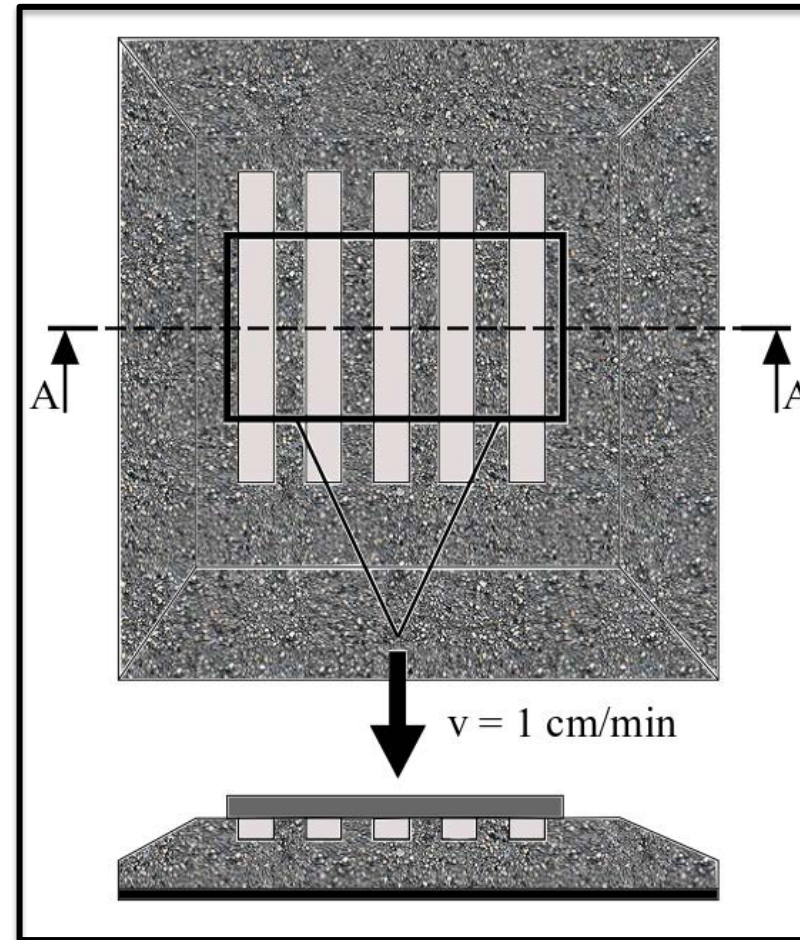
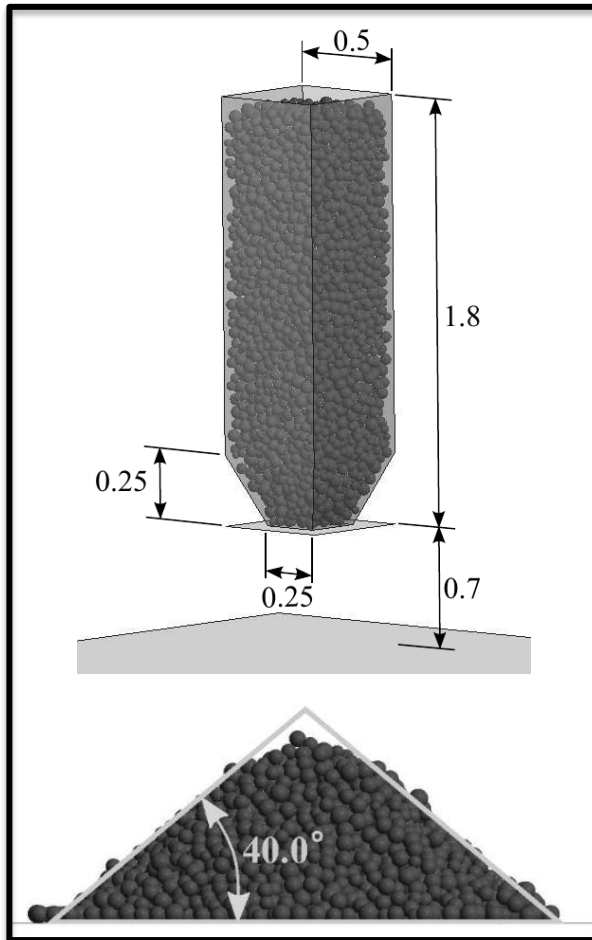
<https://github.com/KratosMultiphysics/Kratos>
<http://gid.cimne.upc.es/>



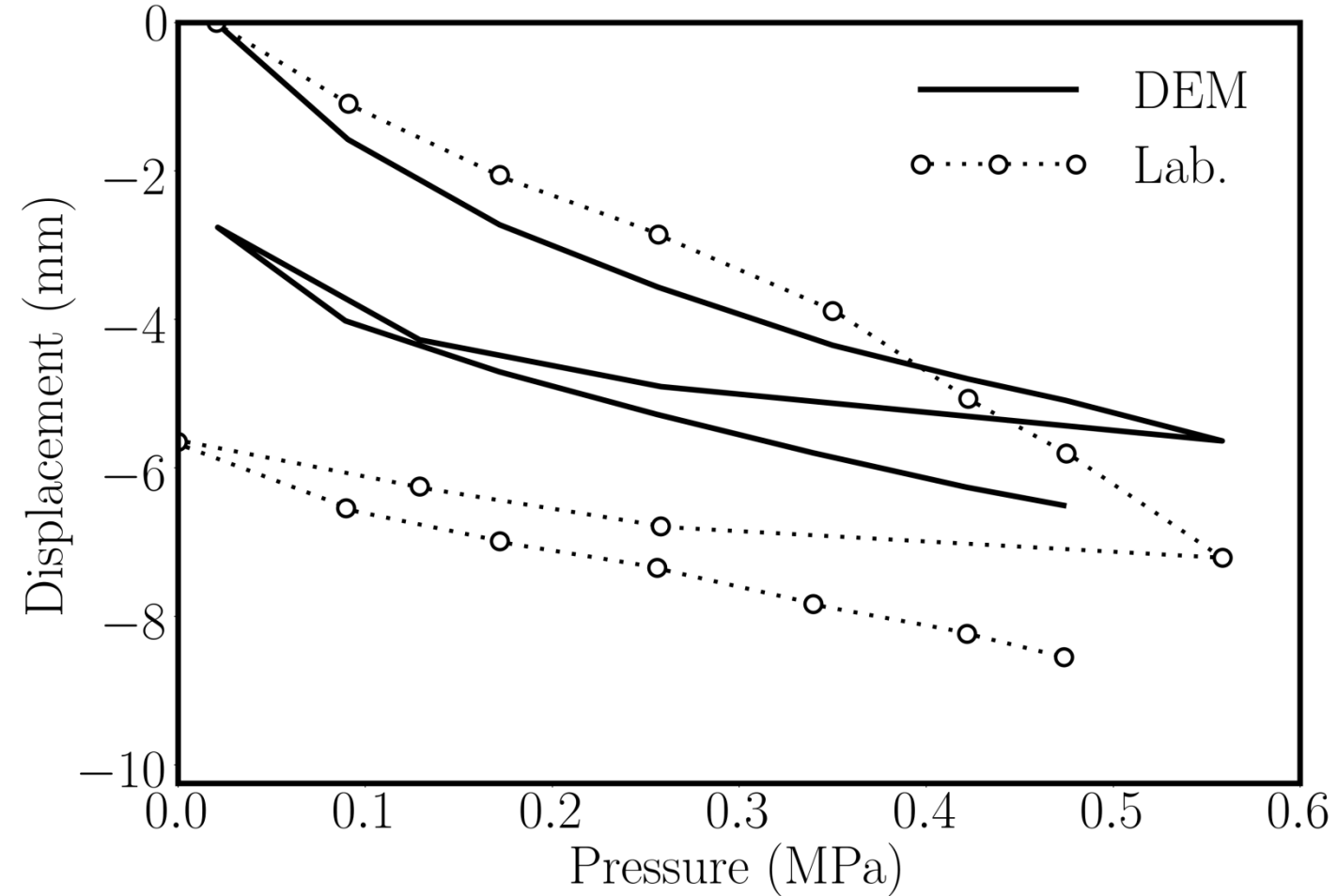
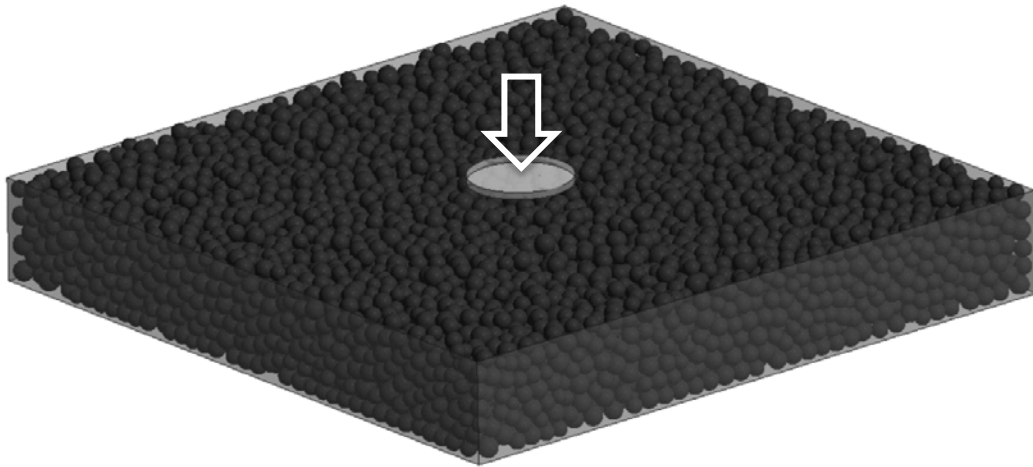
Ballast | Sleepers | Rails, bearing plates | Boundary walls | Subballast |
| Full scale railway track tests | Summary and ongoing work



Good results applying the Hertz-Mindlin contact model

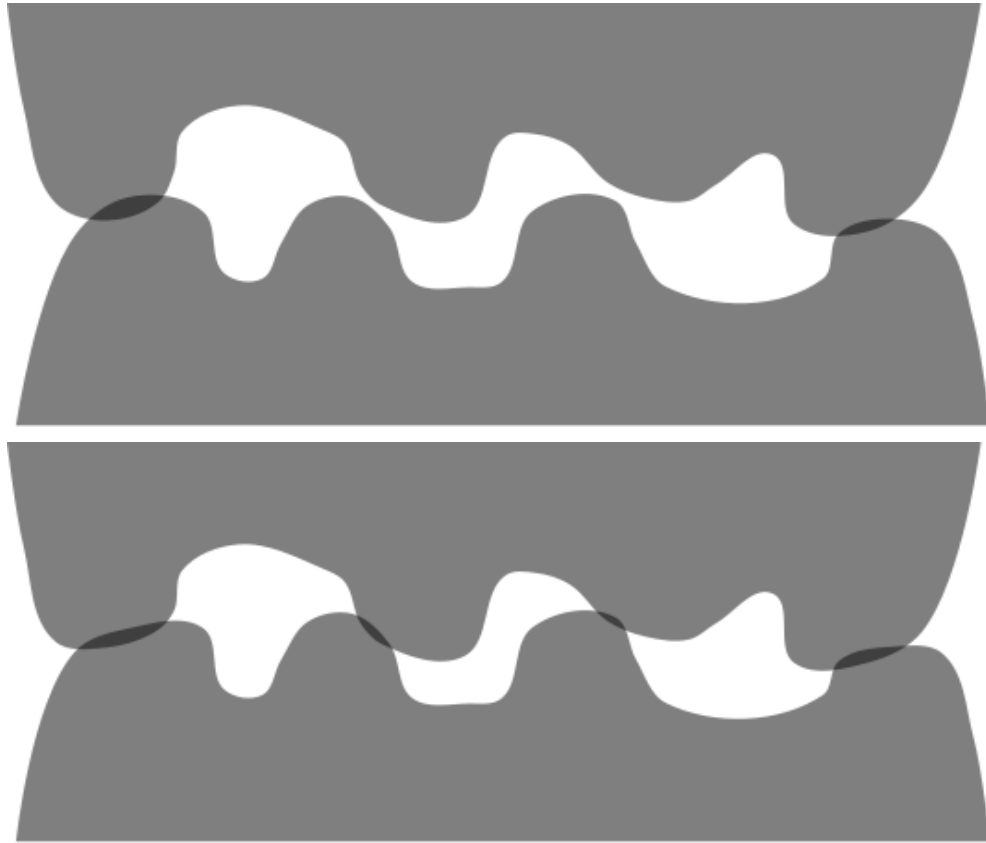


Ballast | Sleepers | Rails, bearing plates | Boundary walls | Subballast |
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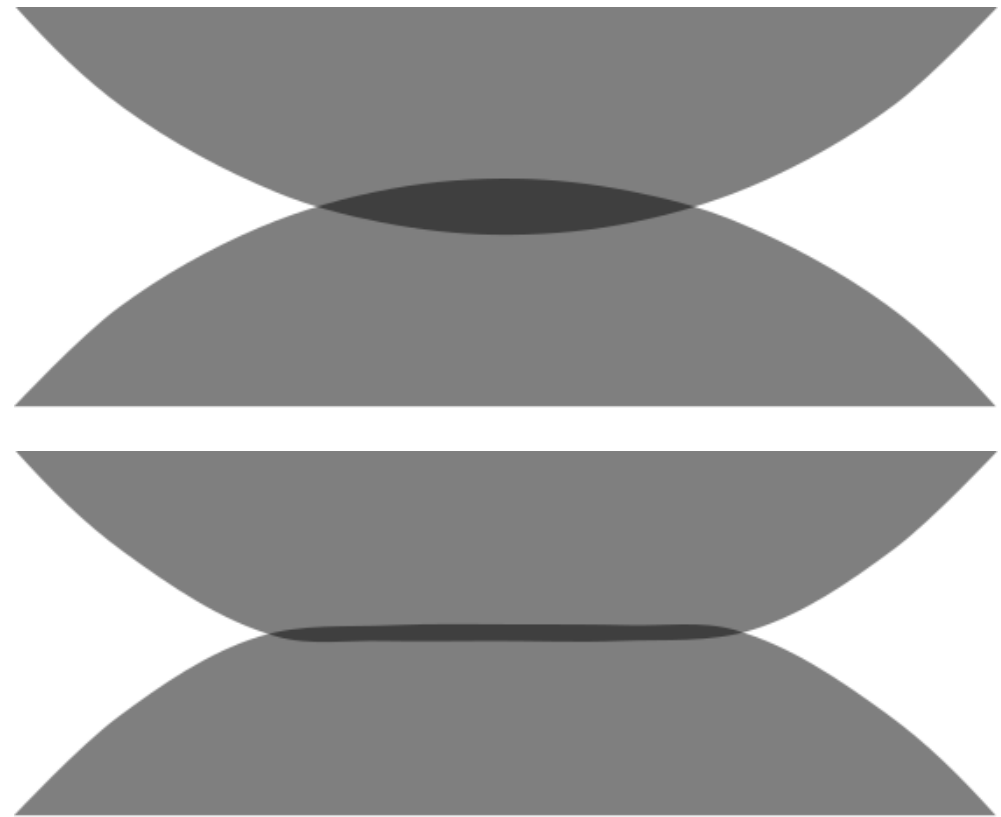


Paderno C. Simulation of ballast behaviour under traffic and tamping process. PhD Thesis 2009.

Hertzian contact model: contact stiffness depends on the contact volumen but does not take into account edge breakage

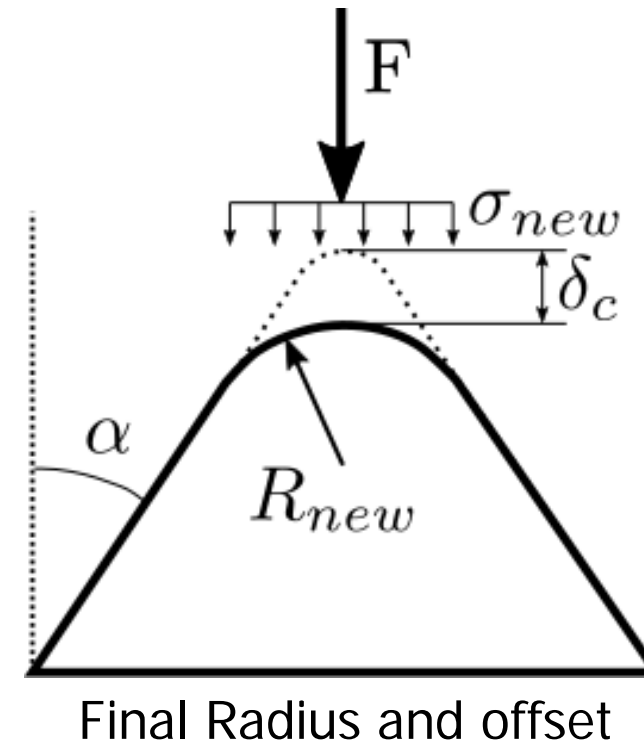
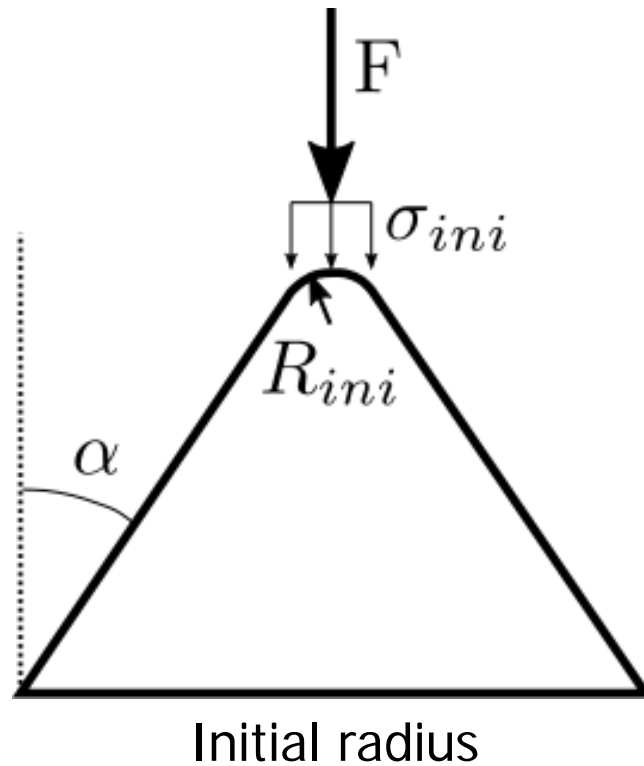


Real contact geometry



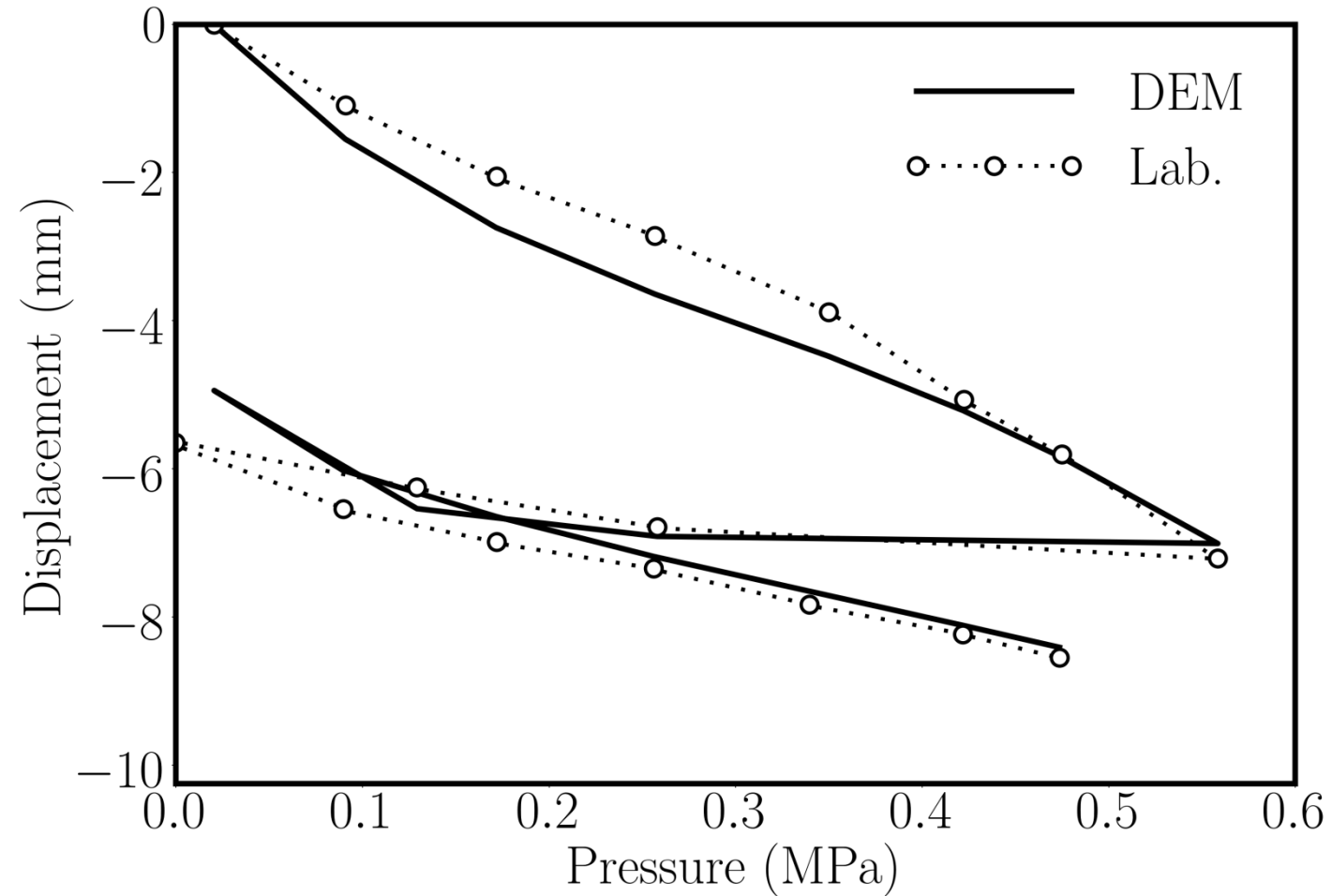
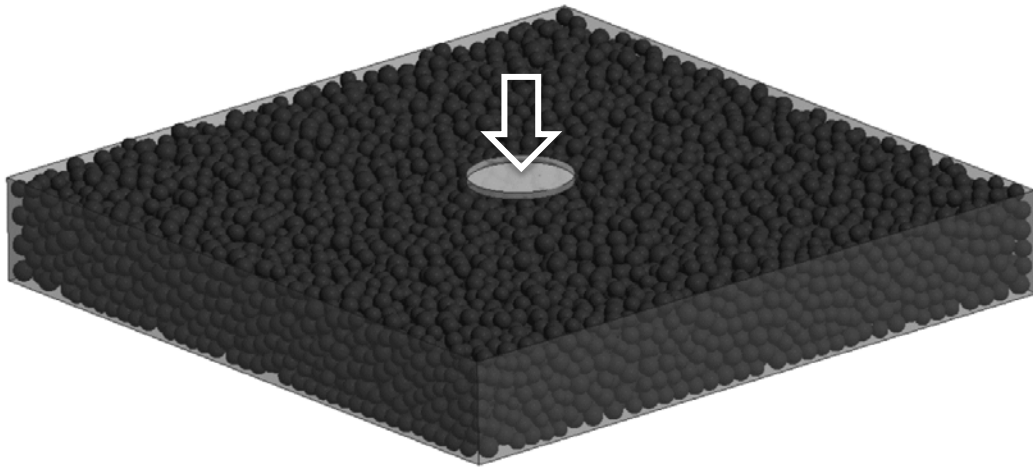
Numerical contact geometry

Conical damage contact model: accounts for edge breakage
 Two new material properties to define: Maximum stress and α

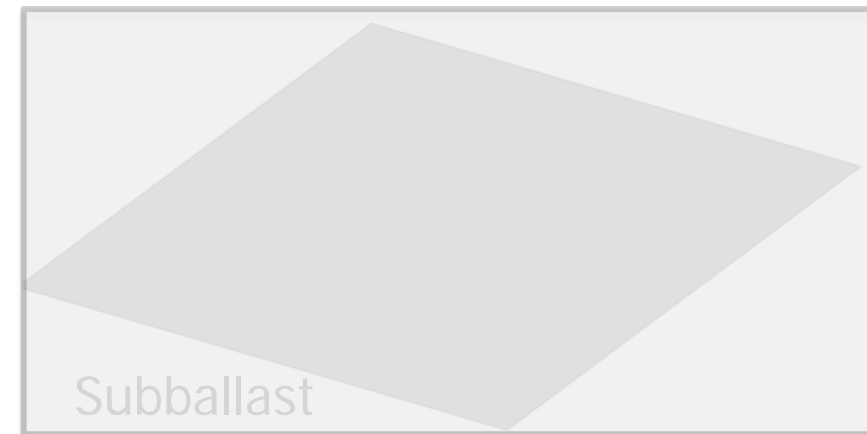
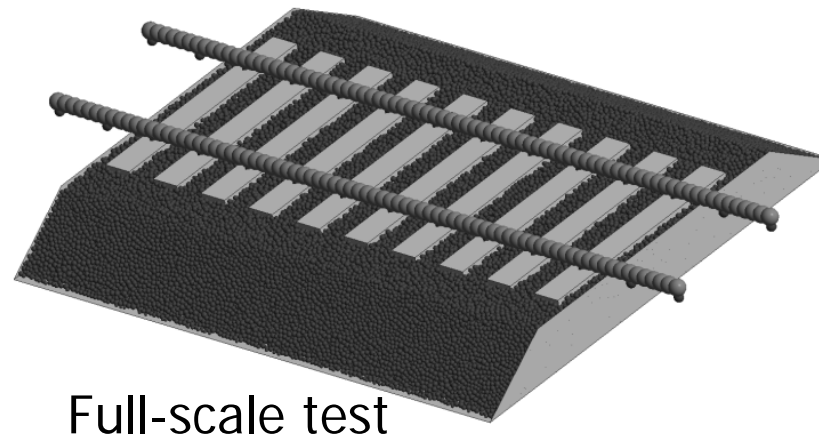
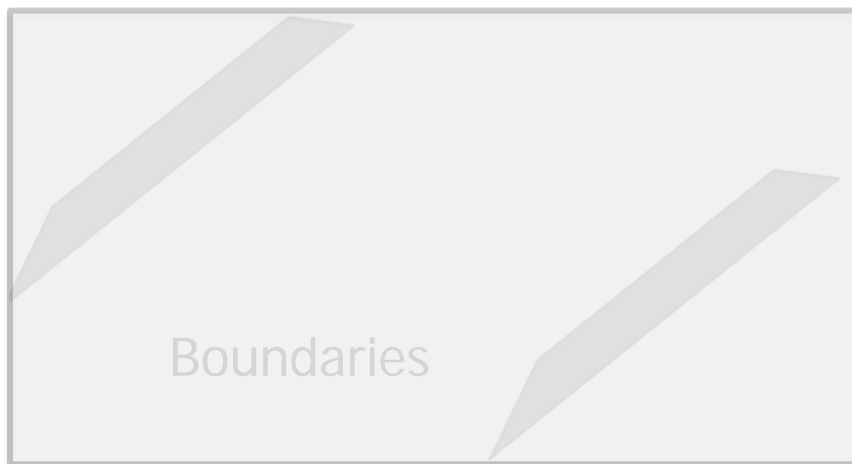
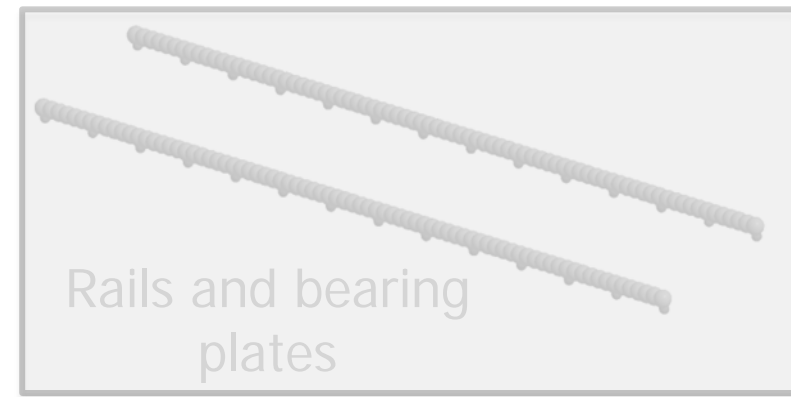
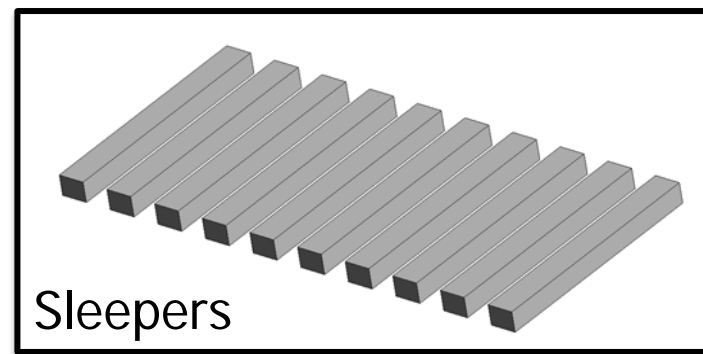
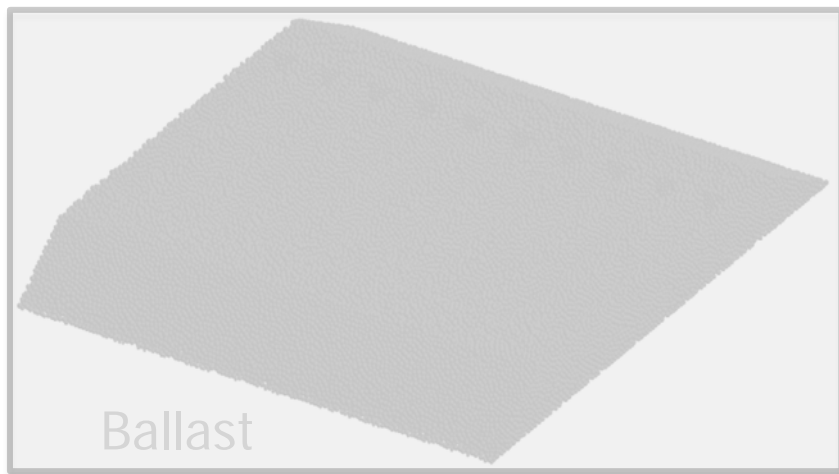


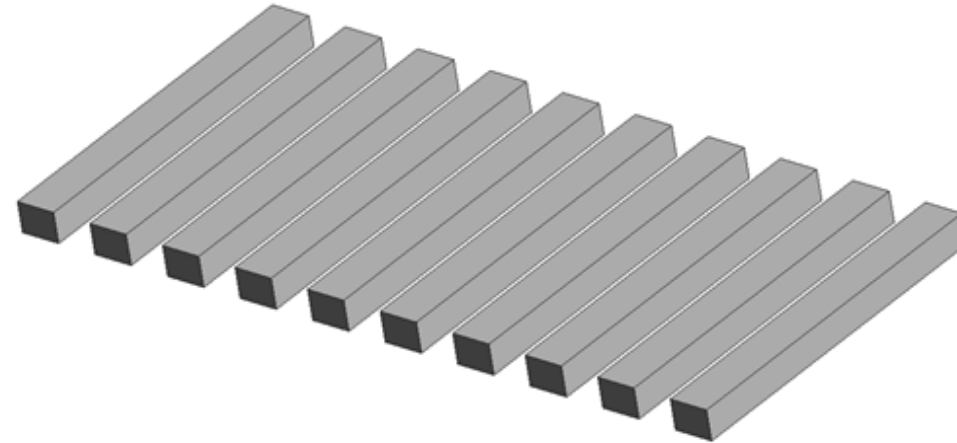
Harkness, J., Zervos, A., Le Pen, L., Aingaran, S., & Powrie, W. (2016). Discrete element simulation of railway ballast: modelling cell pressure effects in triaxial tests. *Granular Matter*, 18(3), 65.

$\sigma_{max} = 500$ MPa
 $\alpha = 89.4$ degrees



Paderno C. Simulation of ballast behaviour under traffic and tamping process. PhD Thesis 2009.





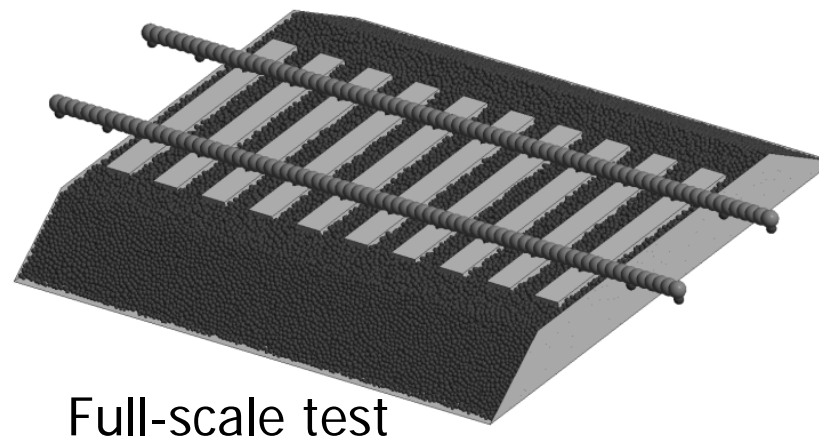
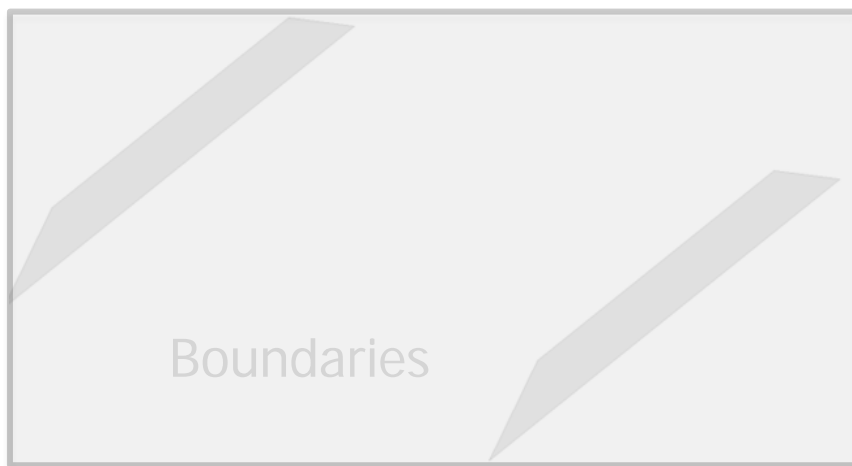
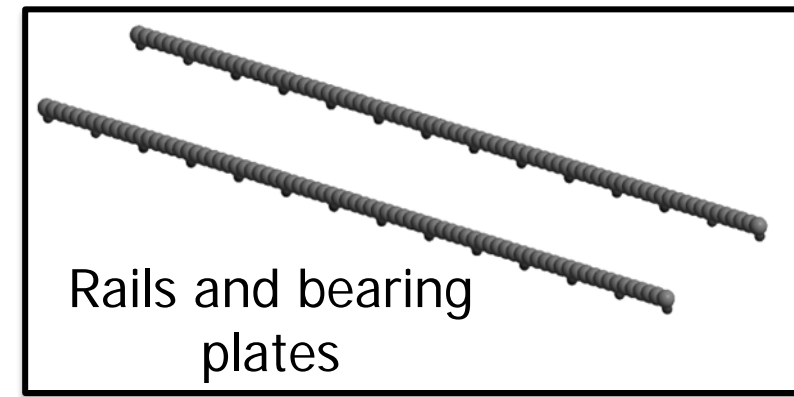
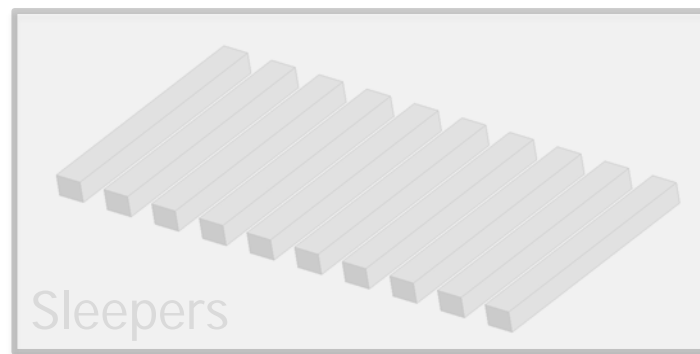
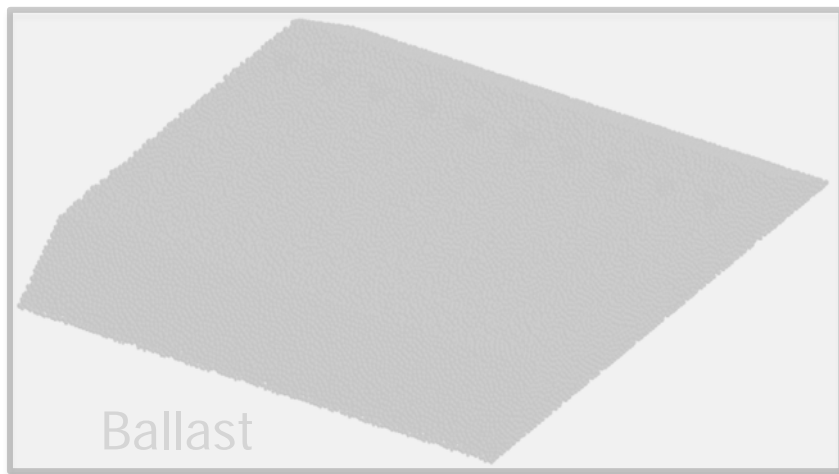
Rigid bodies and simplified geometry

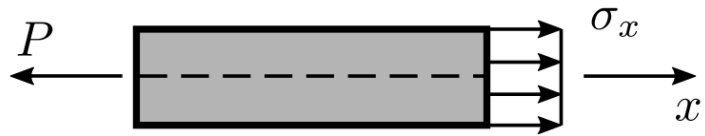
Sleepers contact parameters

Young modulus = 30 Gpa (prestressed concrete)

Friction coefficient = 0.7247*

*Zand, J. van't, & Moraal, J. (1997) Roads and Railways Research Laboratory Technical University of Delft

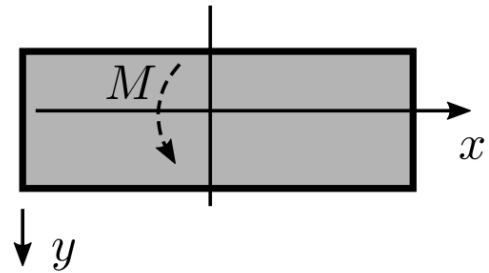




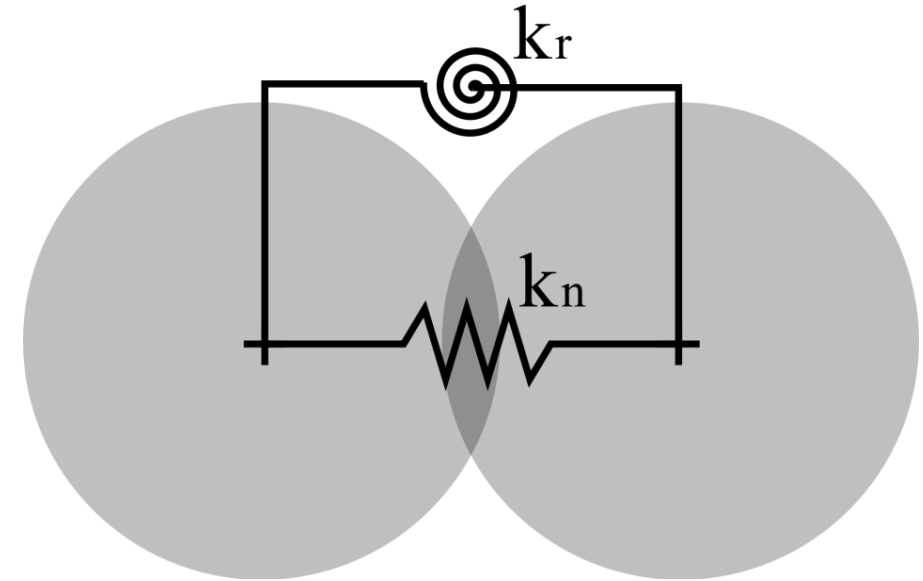
Axial loading: $\sigma_x = \frac{P}{A}$

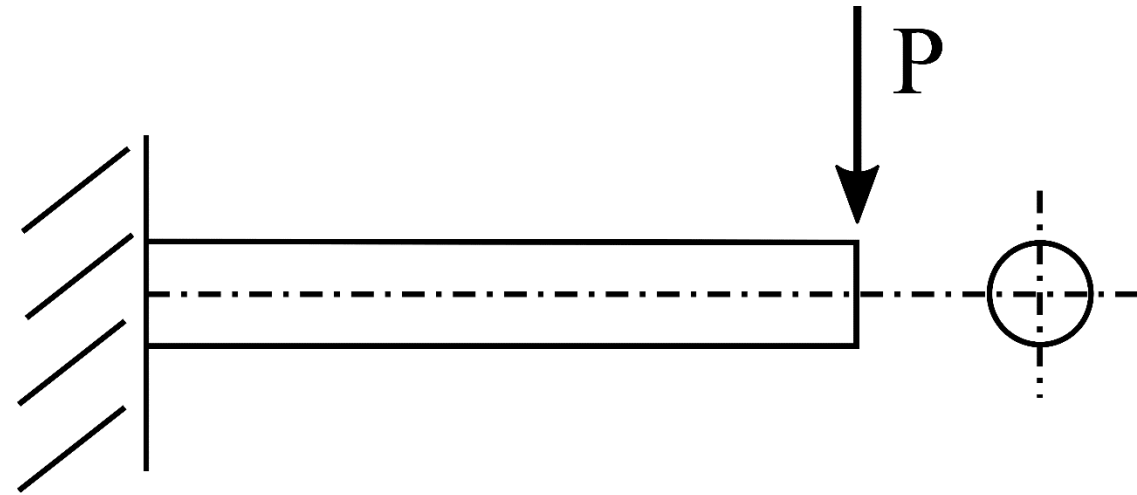


Torsion: $\tau = \frac{T\rho}{J}$

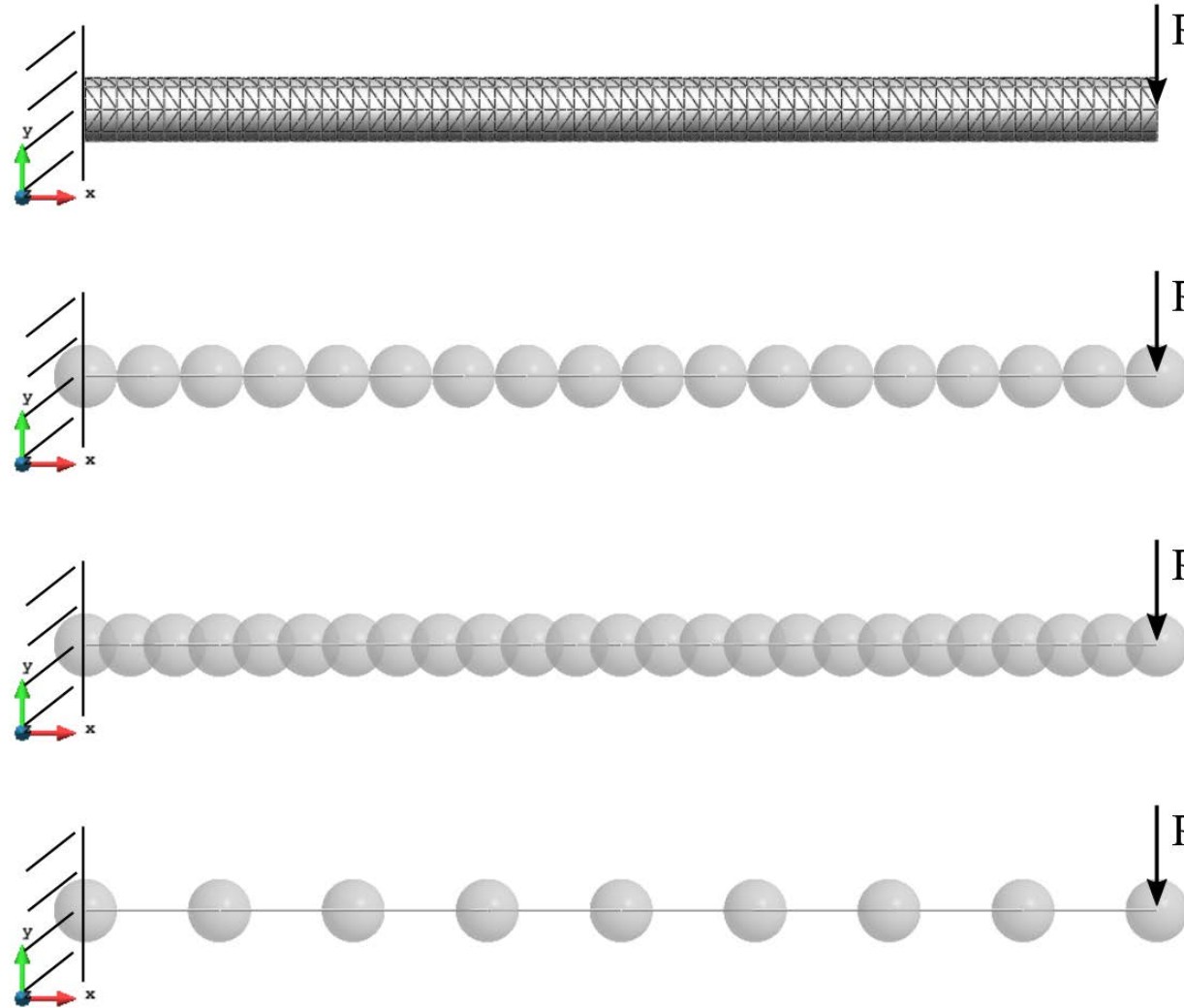


Bending: $\sigma_x = -\frac{My}{I}$





Large deformations
 Non-linear problem } Analytical solution unknown ⇒ FEM

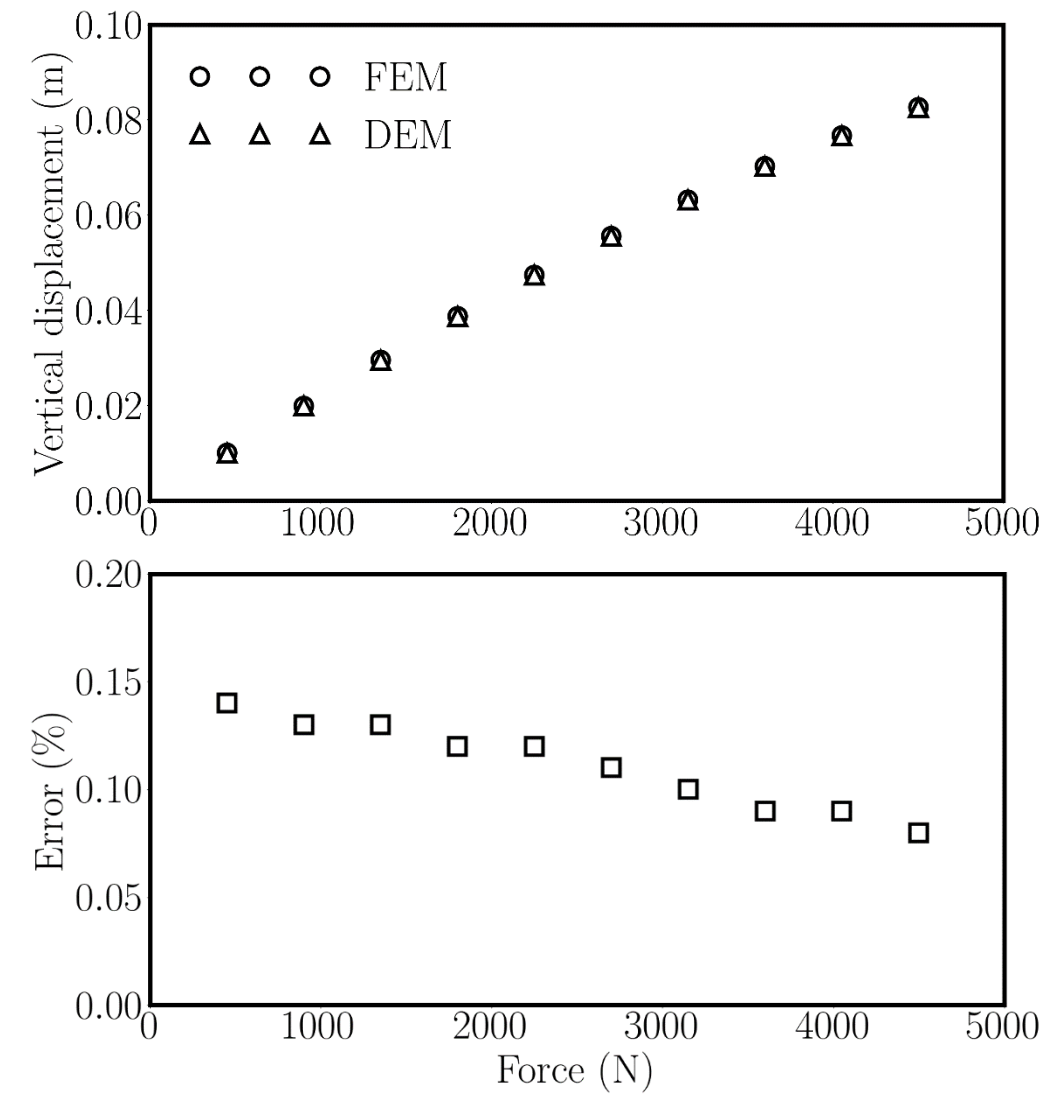
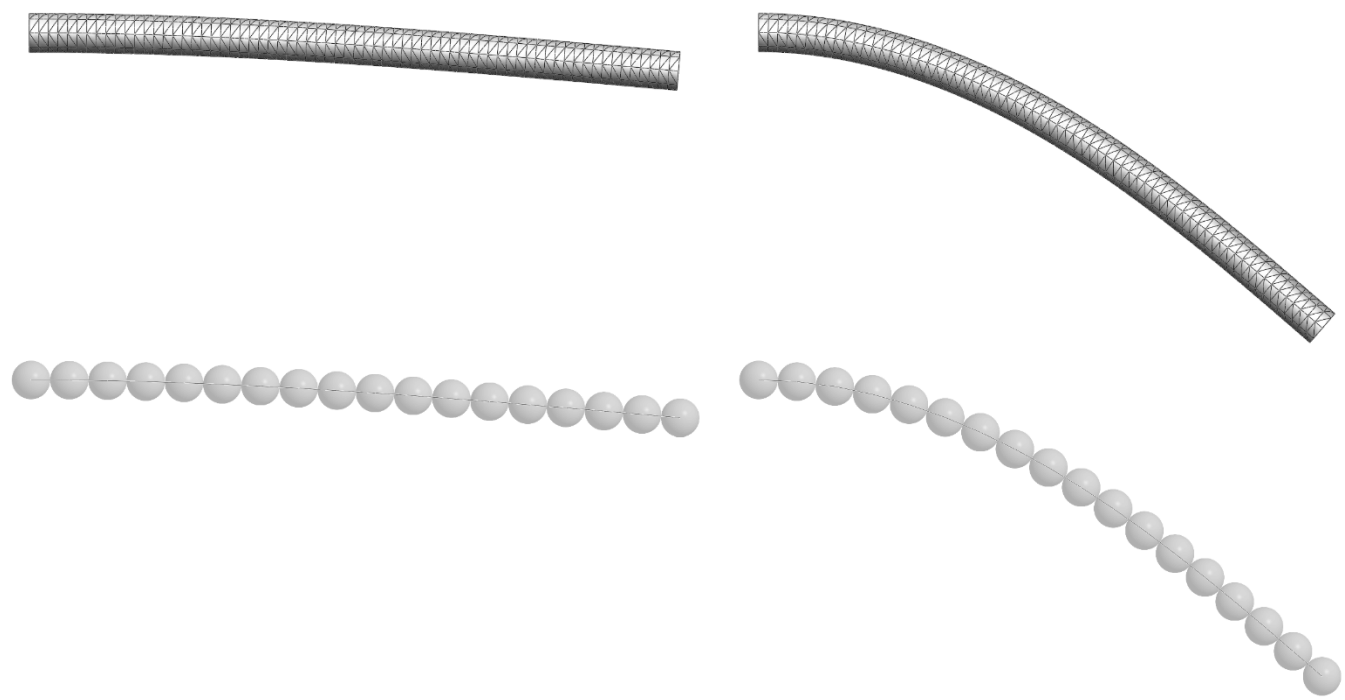


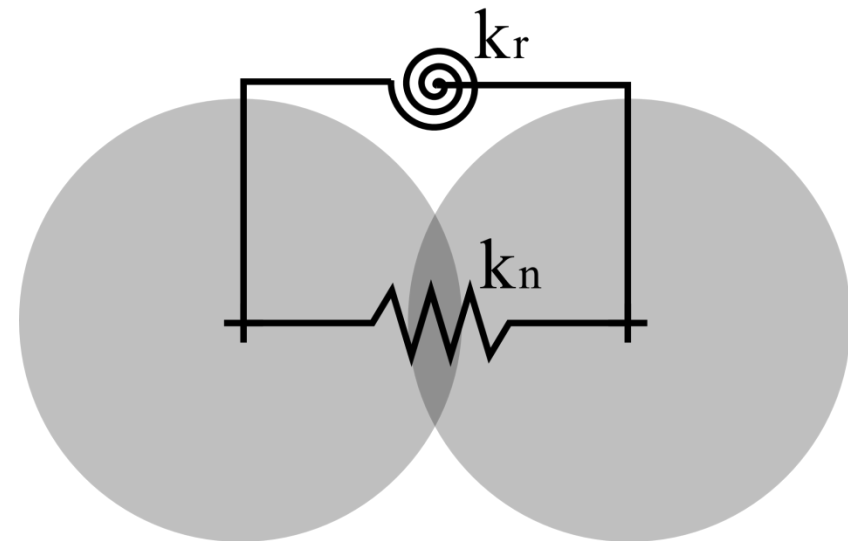
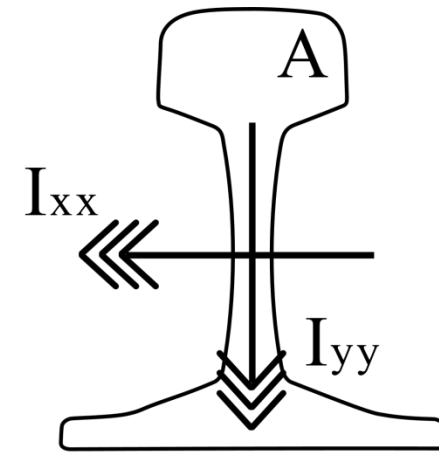
Ballast | **Sleepers** | Rails, bearing plates | Boundary walls | Subballast |
 | Full scale railway track tests | Summary and ongoing work

$E = 117.21 \text{ GPa}$, $\nu = 0.35$,
 $L = 0.204 \text{ m}$ and $R = 0.006 \text{ m}$

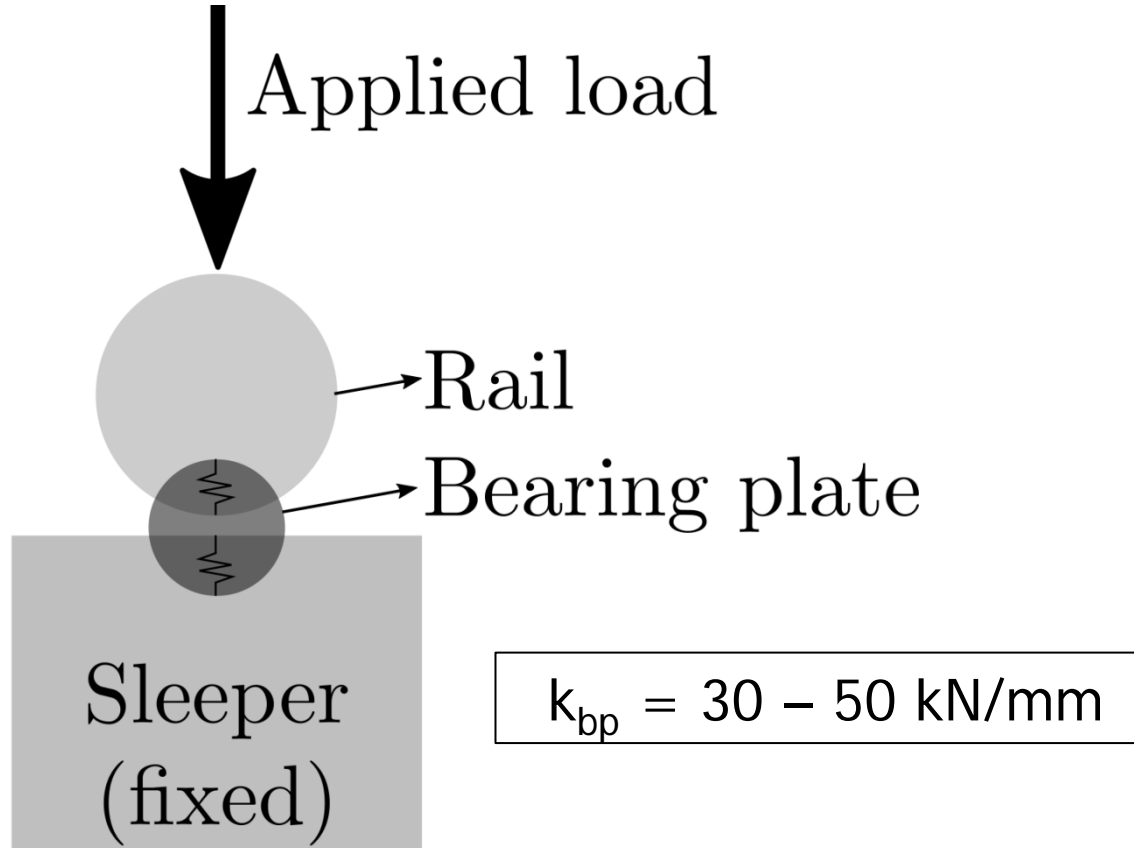
$P = 450 \text{ N}$

$P = 4500 \text{ N}$

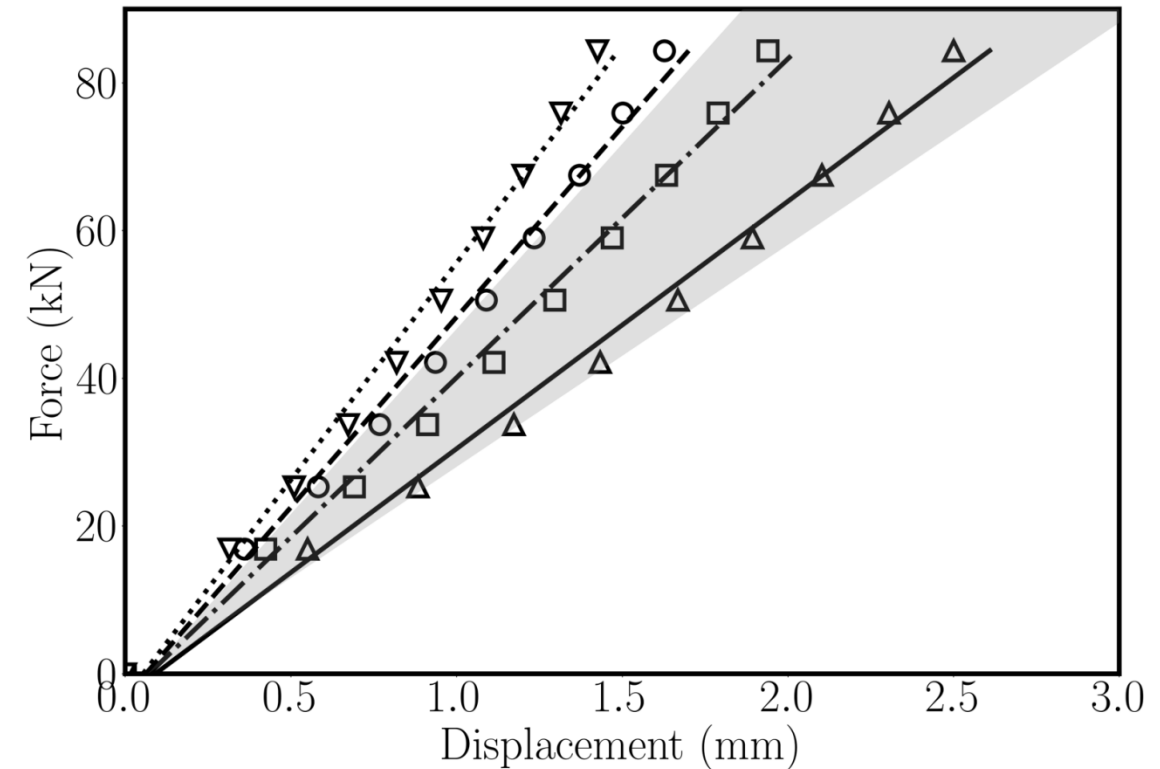




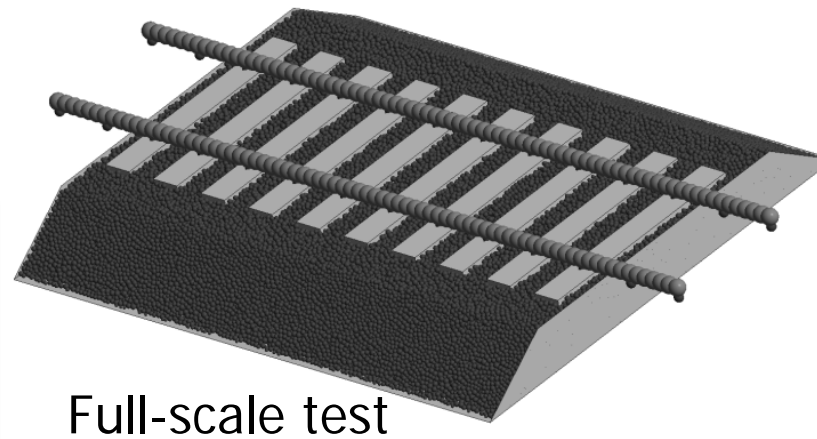
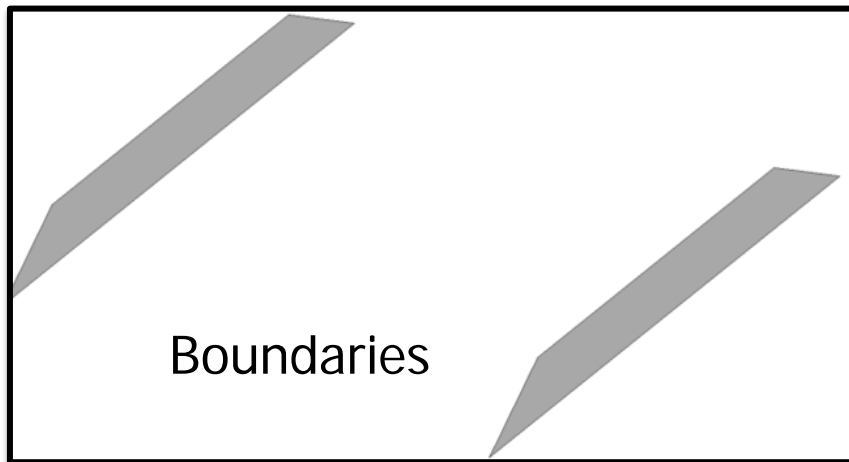
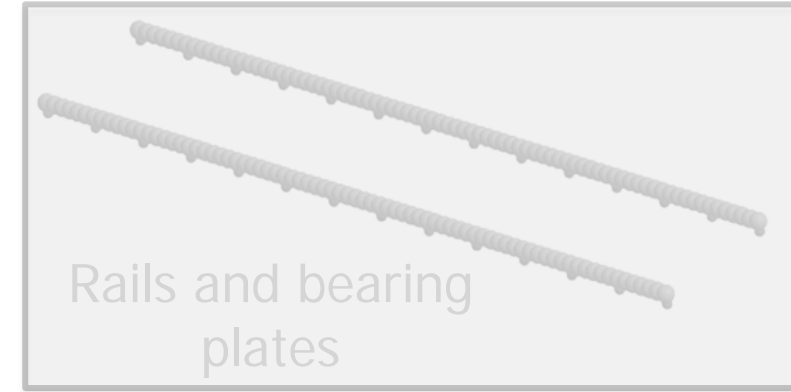
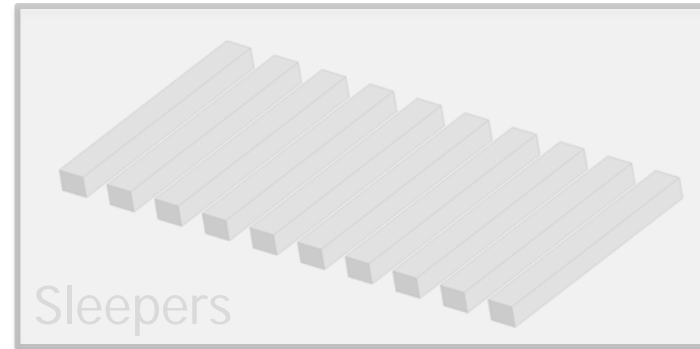
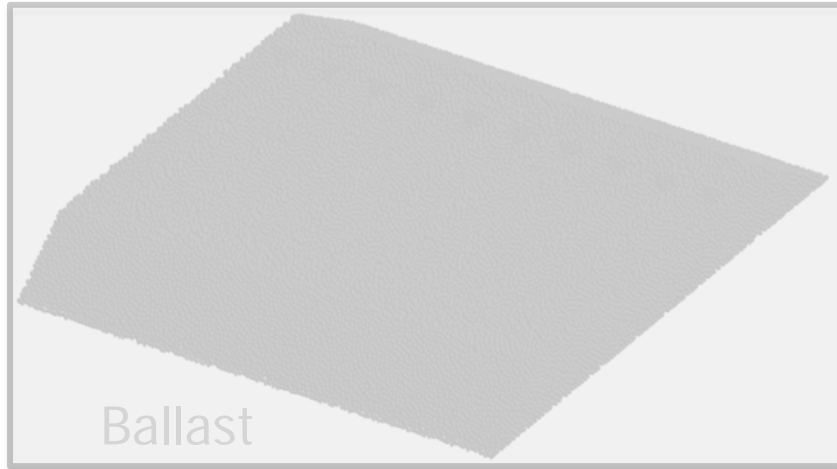
Ballast | **Sleepers** | Rails, bearing plates | Boundary walls | Subballast |
 | Full scale railway track tests | Summary and ongoing work

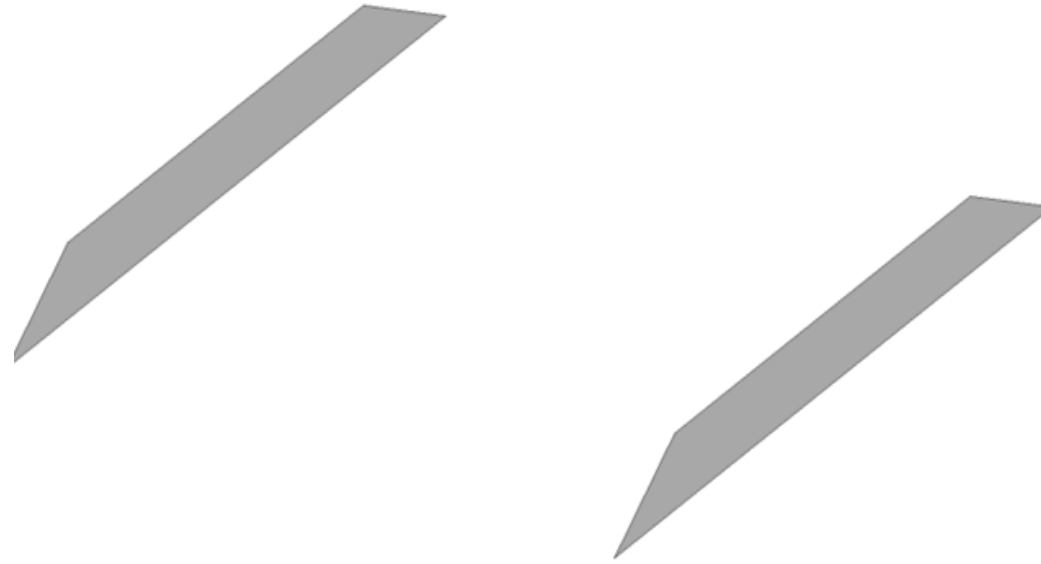


Δ	Δ	$E_{bp} = 2 \text{ GPa}$	—	$k_{bp} = 33.51 \text{ kN/mm}$
\square	\square	$E_{bp} = 3 \text{ GPa}$	- - -	$k_{bp} = 43.18 \text{ kN/mm}$
\circ	\circ	$E_{bp} = 4 \text{ GPa}$	- - -	$k_{bp} = 51.50 \text{ kN/mm}$
∇	∇	$E_{bp} = 5 \text{ GPa}$	$k_{bp} = 58.81 \text{ kN/mm}$



Pita, A. L., Teixeira, P. F., & Robusté, F. (2004). High speed and track deterioration: the role of vertical stiffness of the track. Proceedings of the Institution of Mechanical Engineers, Part F: Journal of Rail and Rapid Transit, 218(1), 31-40.



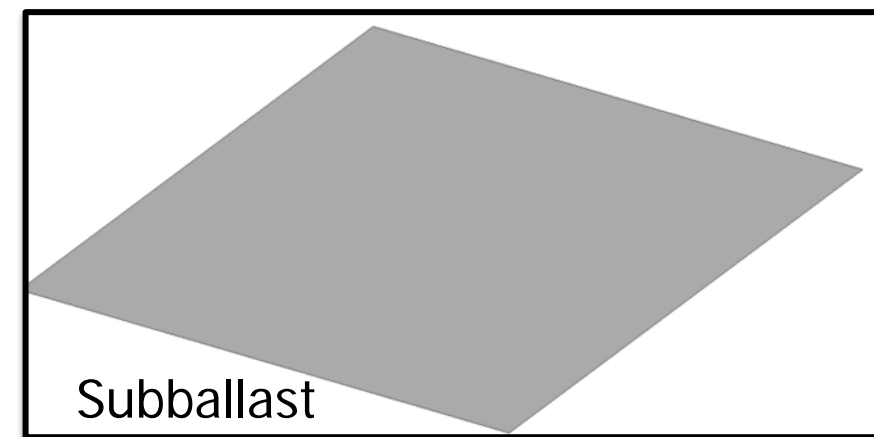
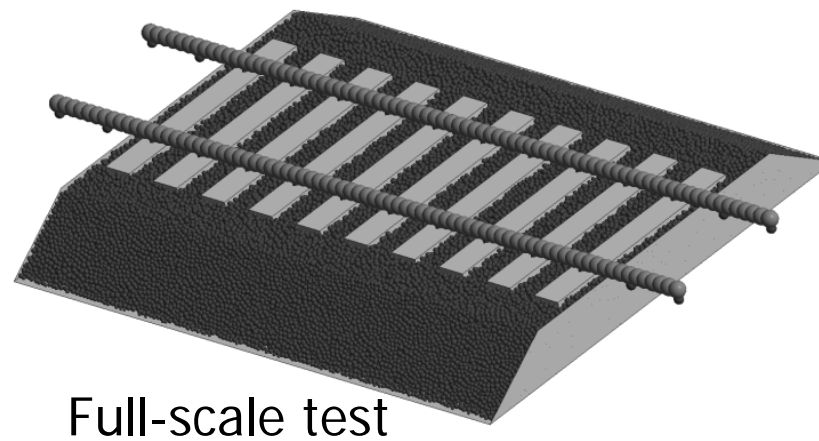
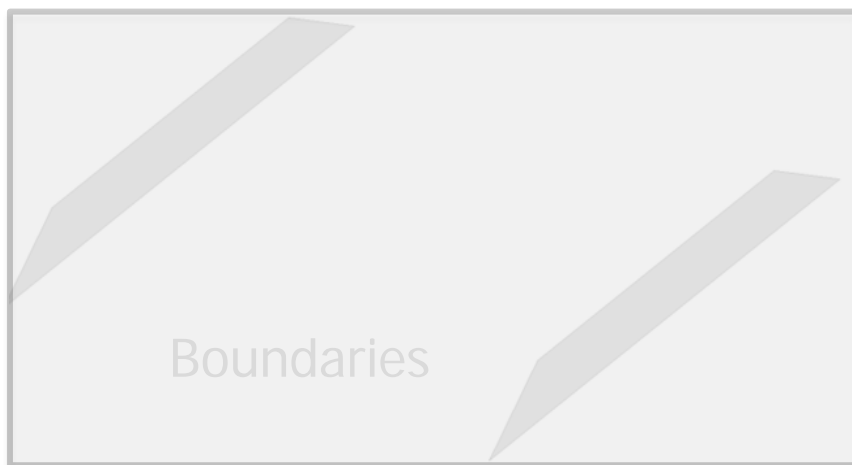
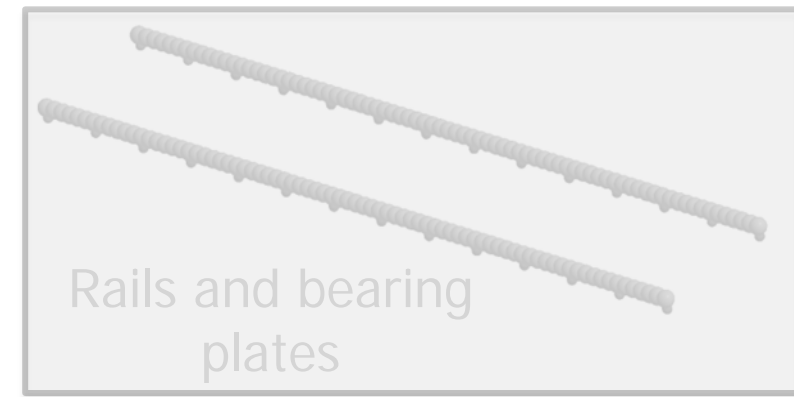
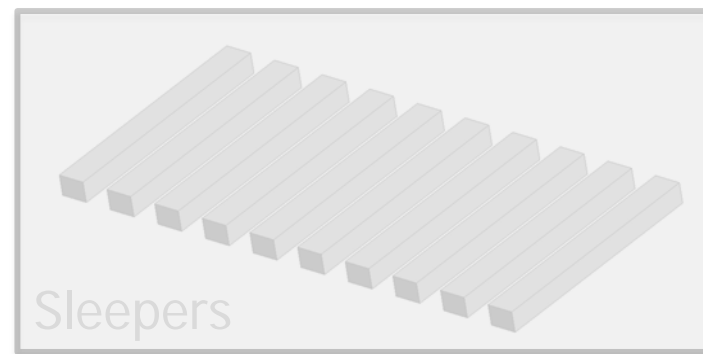
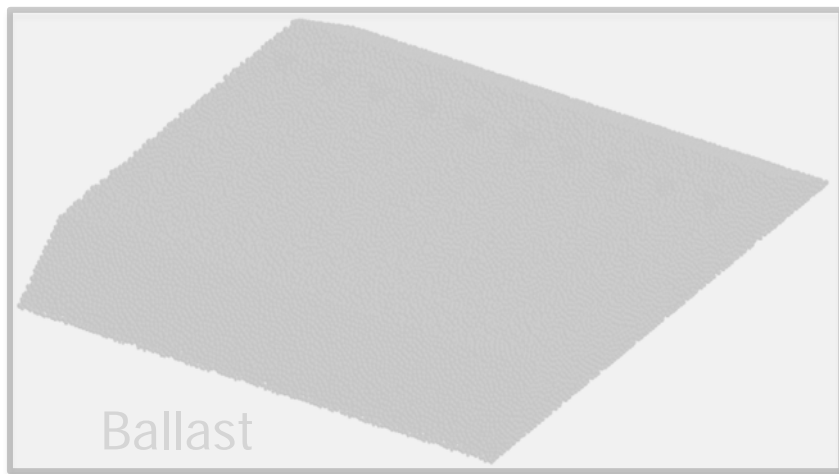


Contact between ballast and boundary walls

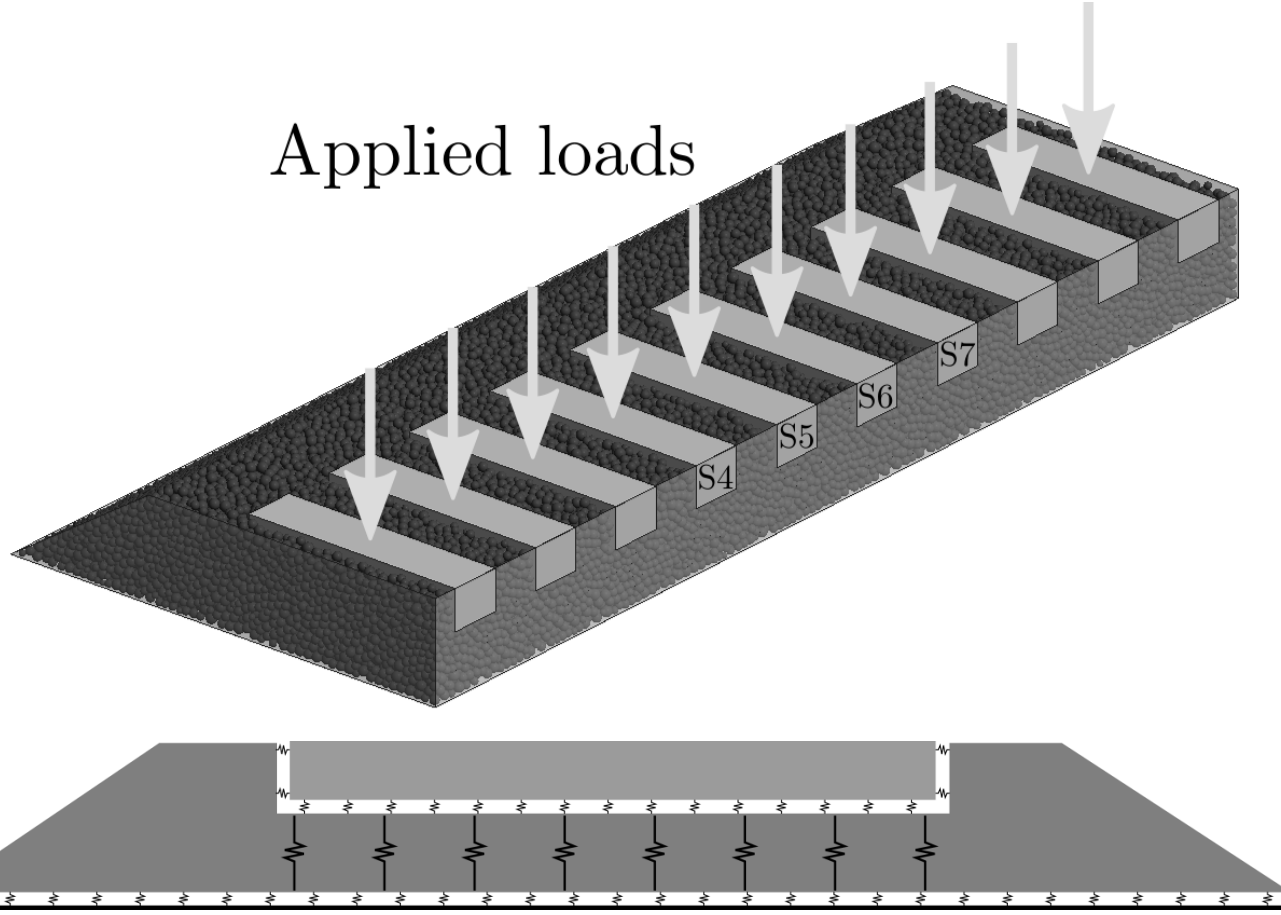
Young modulus = 200 Mpa*

Friction coefficient = 0.0 ("mirrored particles")

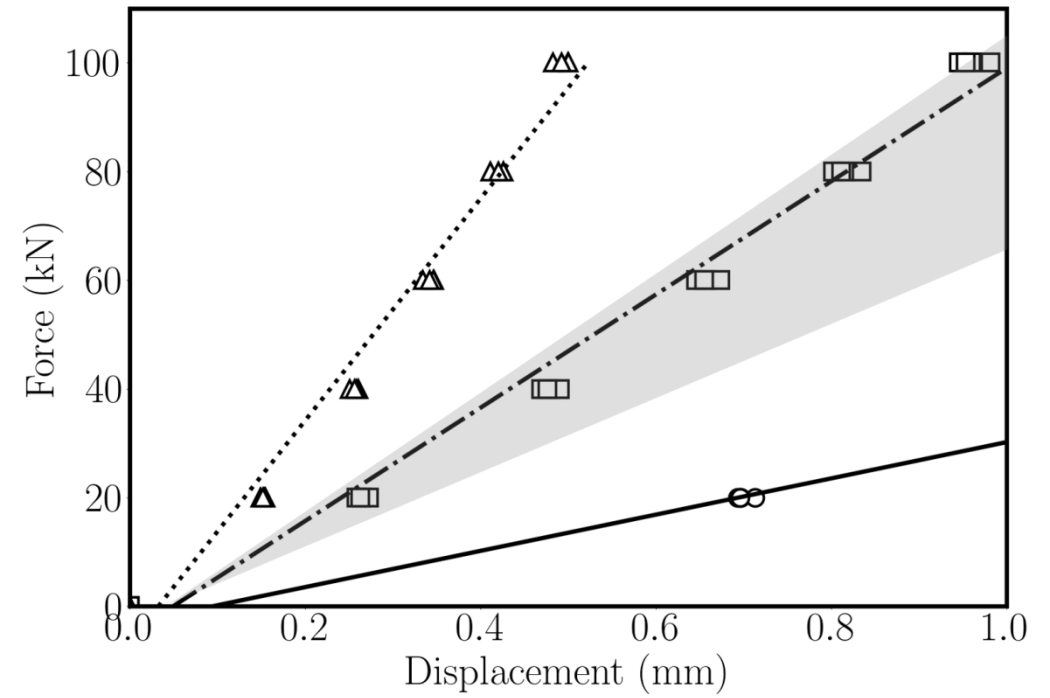
*Paderno, C. Simulation of ballast behaviour under traffic and tamping process. 9th Swiss Transport Research Conference. 2009.



Applied loads

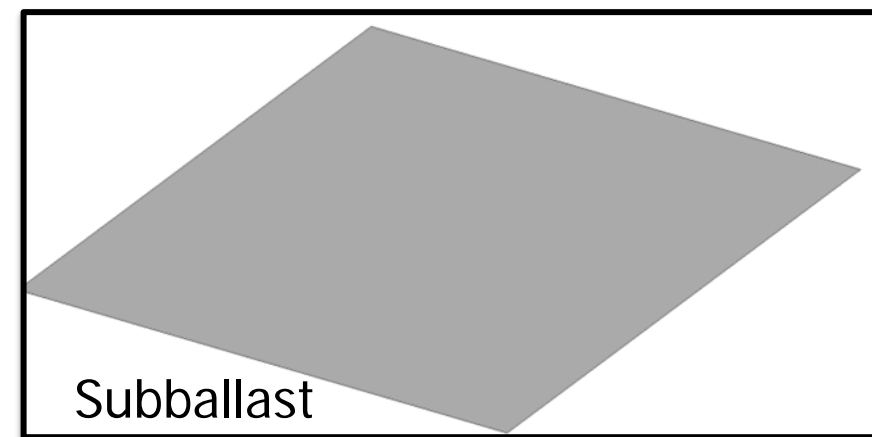
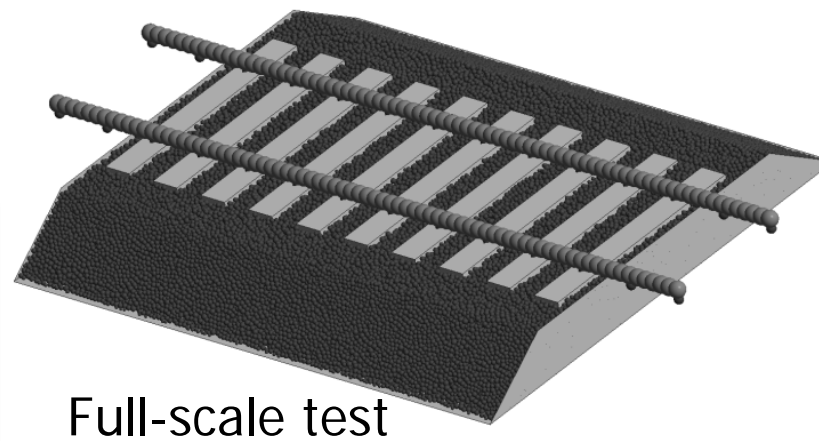
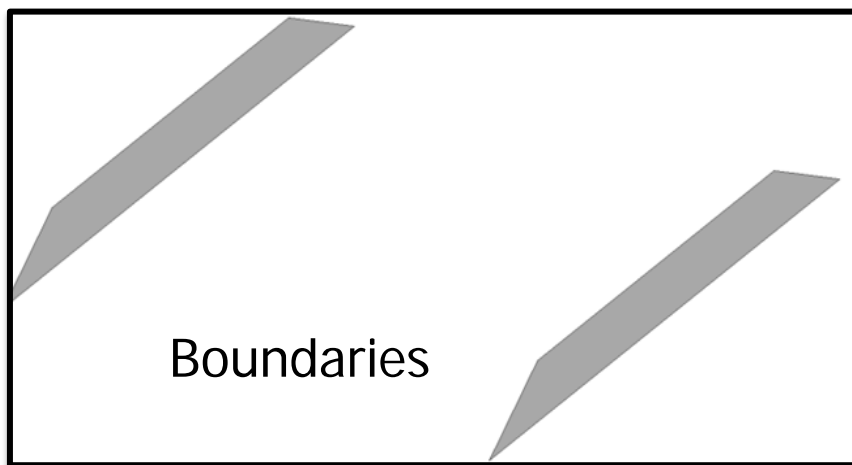
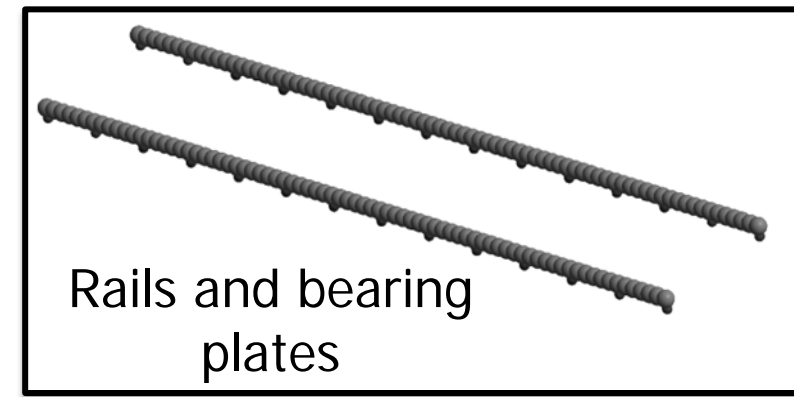
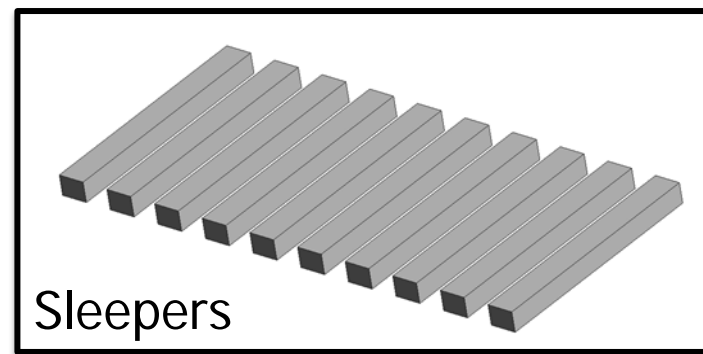
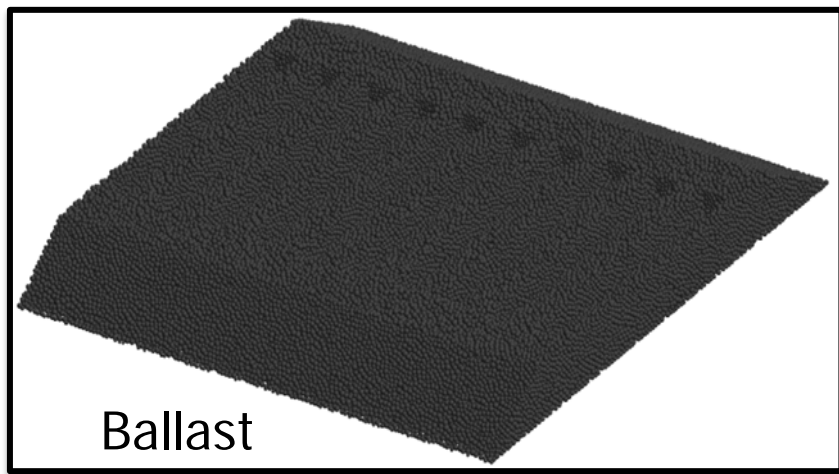


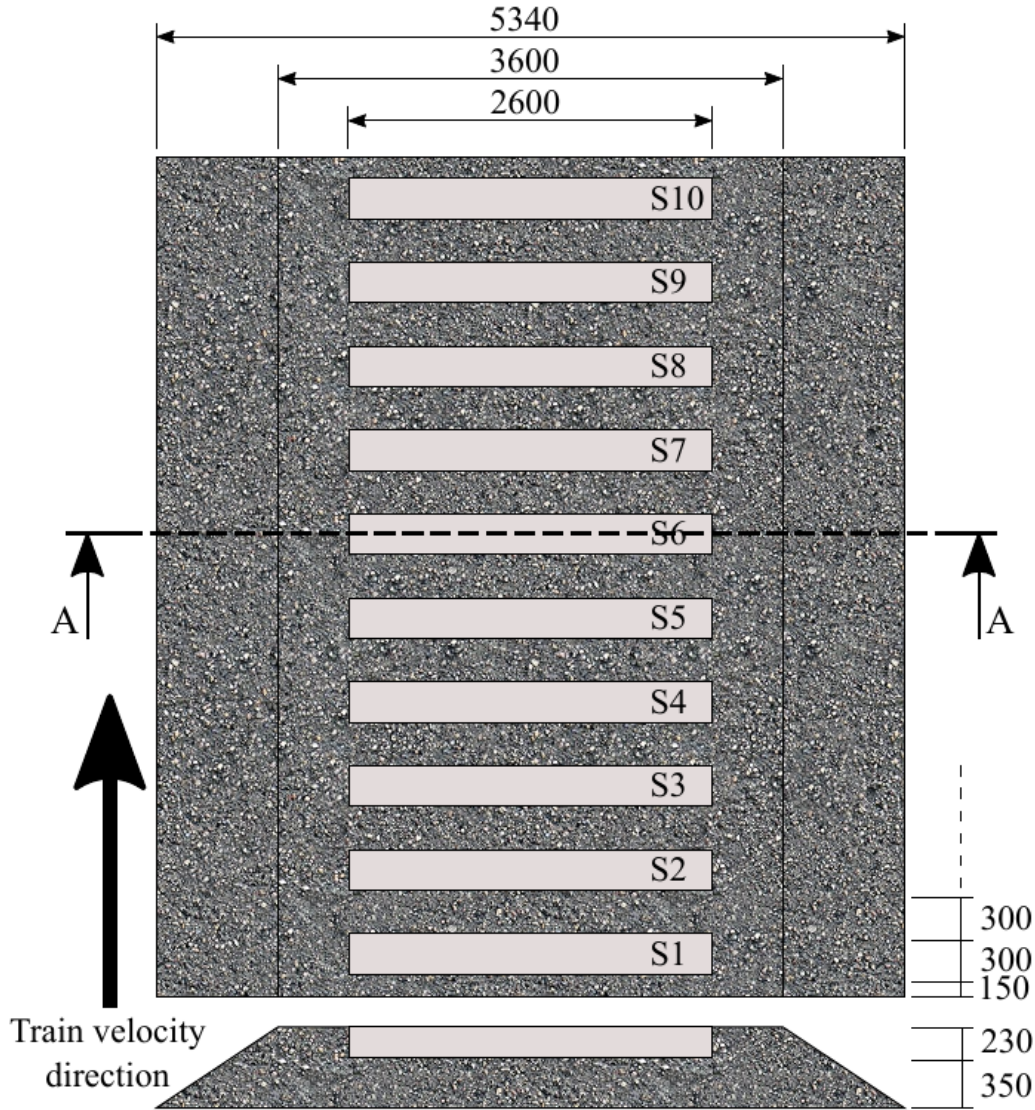
○ ○	$E_{sub} = 3 \text{ MPa}$	—	$k_{sub} = 33.34 \text{ kN/mm}$
□ □	$E_{sub} = 30 \text{ MPa}$	- - -	$k_{sub} = 104.17 \text{ kN/mm}$
△ △	$E_{sub} = 300 \text{ MPa}$	$k_{sub} = 204.14 \text{ kN/mm}$



$k_{sub} = 70 - 110 \text{ kN/mm}$

Pita, A. L., Teixeira, P. F., & Robusté, F. (2004). High speed and track deterioration: the role of vertical stiffness of the track. Proceedings of the Institution of Mechanical Engineers, Part F: Journal of Rail and Rapid Transit, 218(1), 31-40.





- Scenario 1: Well compacted track
- Scenario 2: Poorly compacted track
- Scenario 3: Fouled track (less friction* and larger contact volume between particles)

*Huang, H. & Tutumluer, E. (2011). Discrete Element Modeling for fouled railroad ballast. *Construction and Building Materials*, 25 (8) 3306–3312.



$Q = 168732 \text{ N}$

$v = 250 \text{ km/h}$

$R = 4000 \text{ m}$

$A = 77.45 \text{ cm}^2$

$I_{xx} = 3217 \text{ cm}^4$

$I_{yy} = 524 \text{ cm}^4$

Axle load

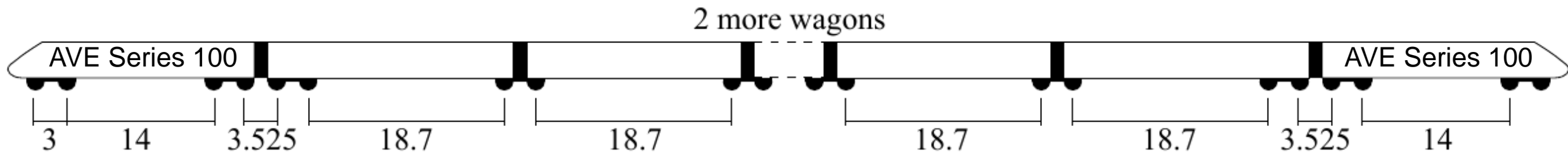
Velocity of the train

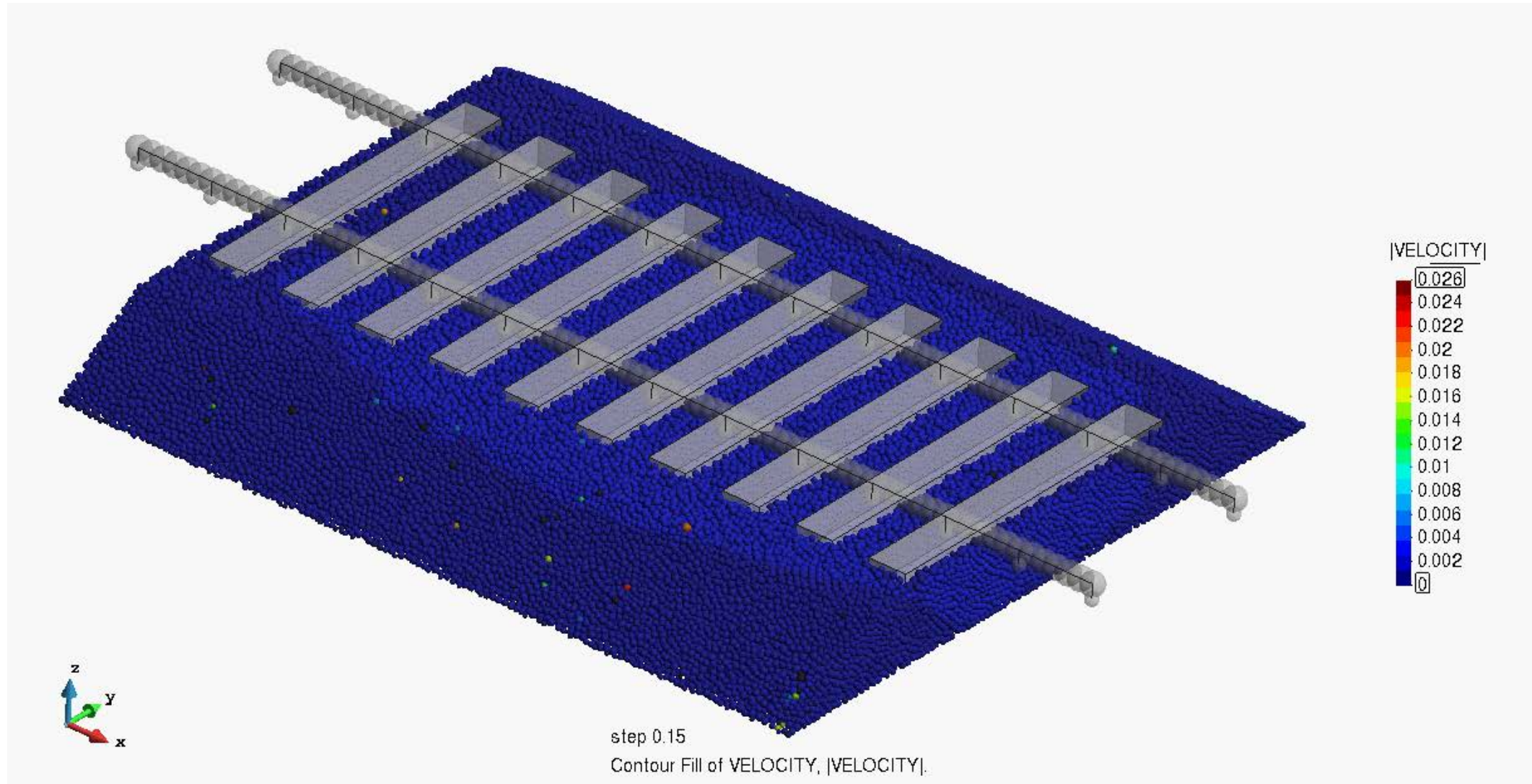
Radius of the curve

Rail cross section

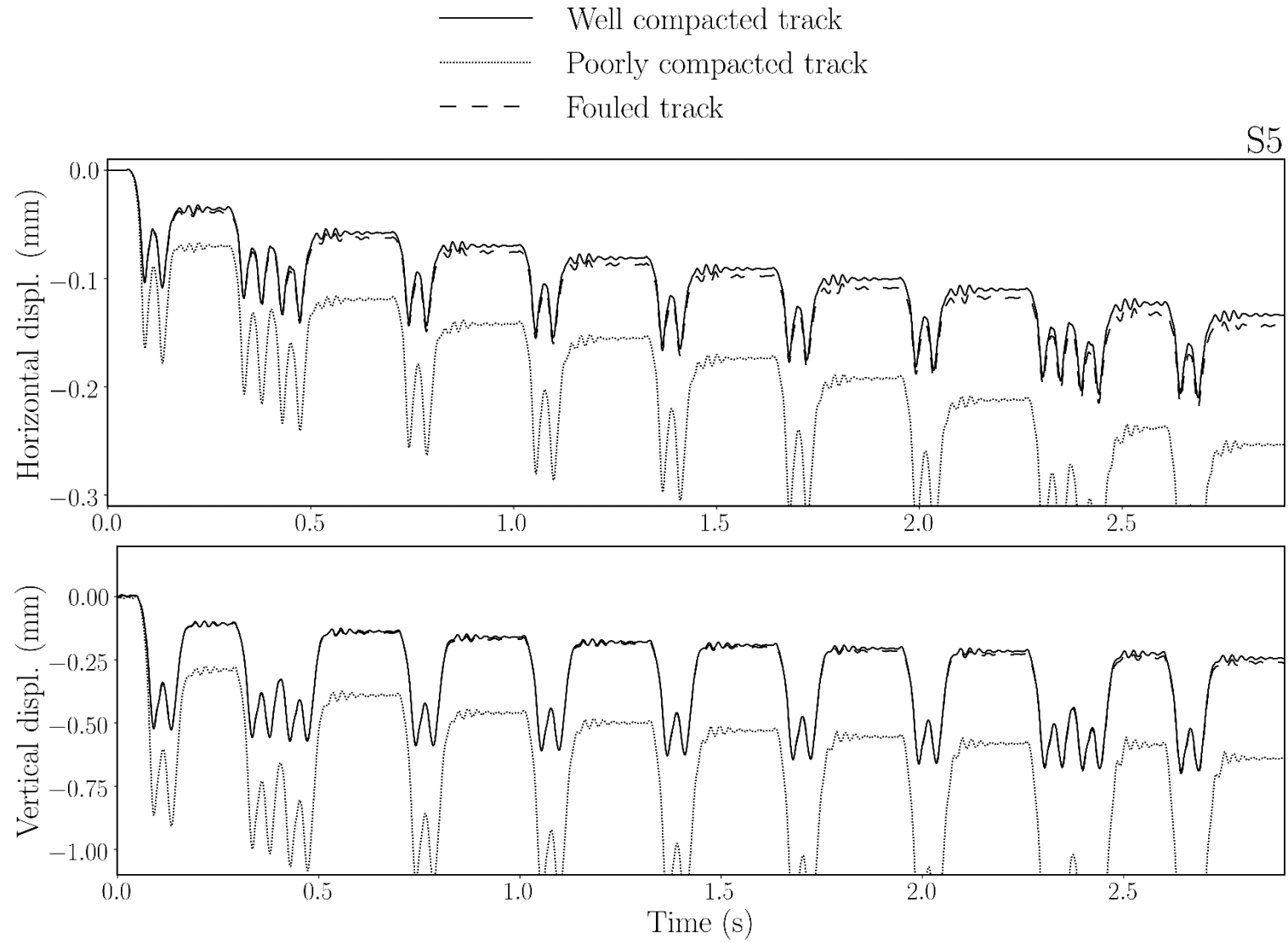
Moment of inertia horizontal axis

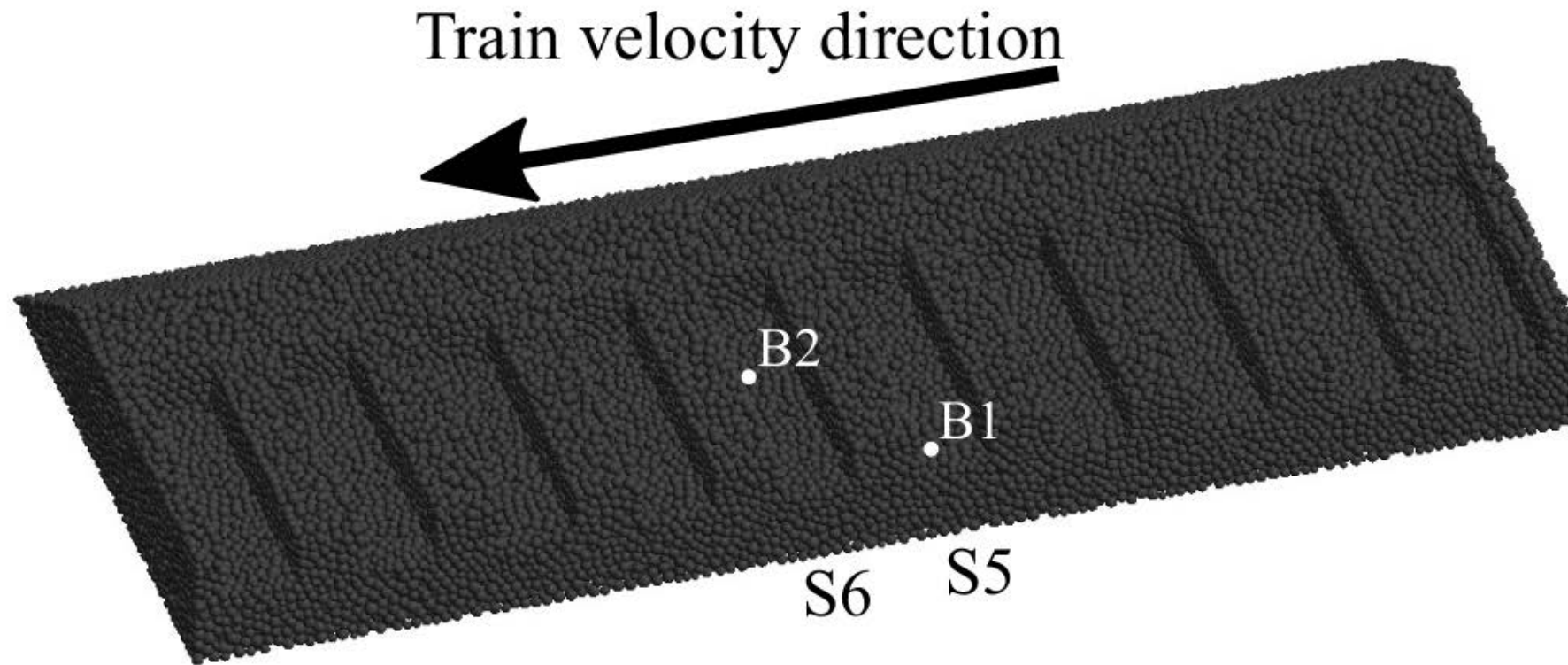
Moment of inertia vertical axis

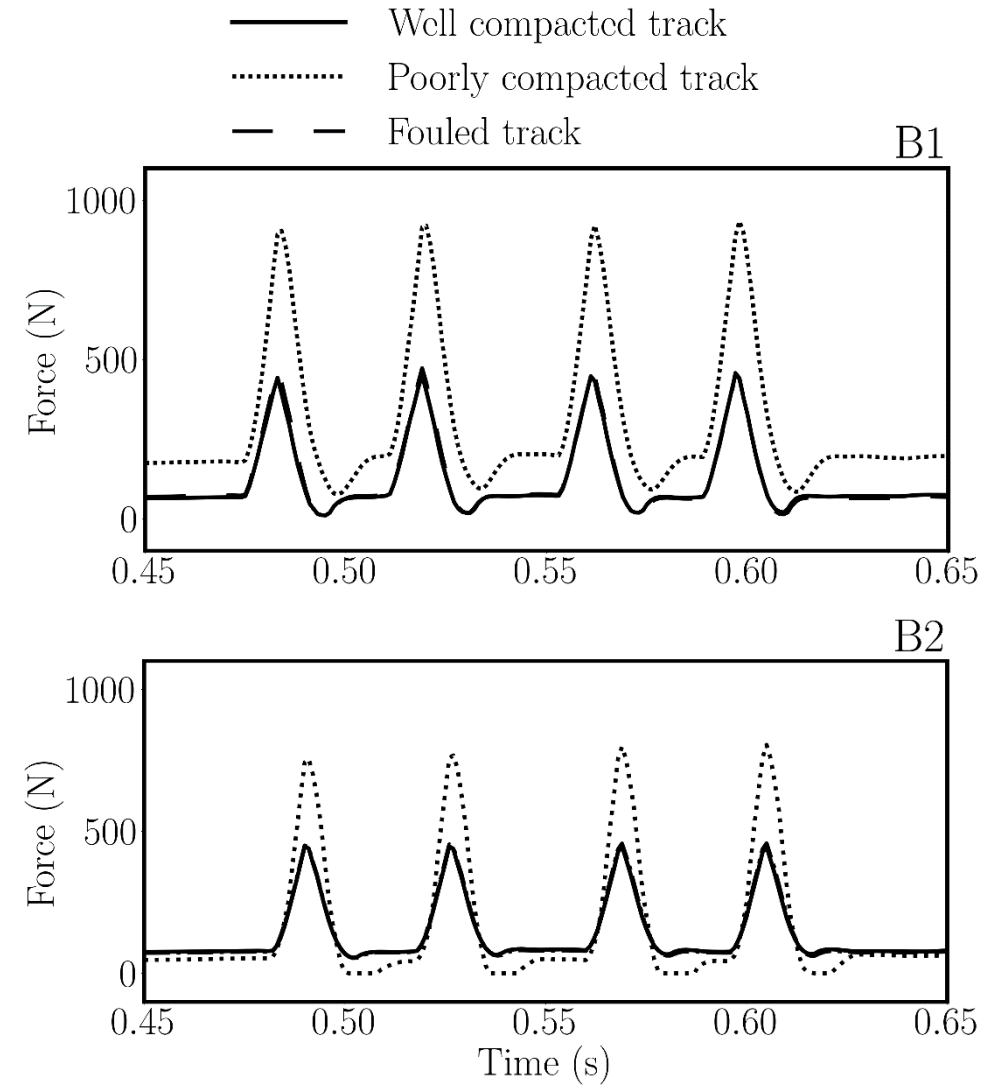
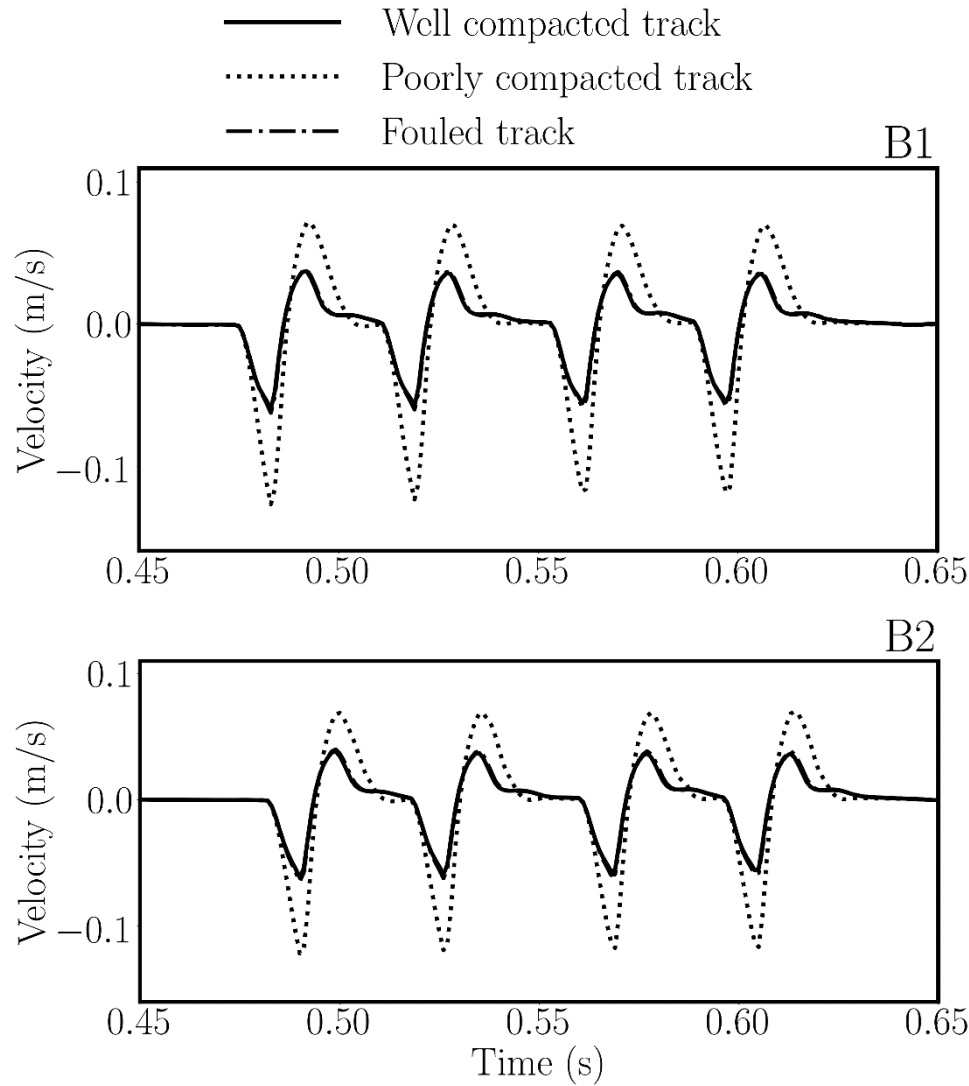




Ballast | Sleepers | Rails, bearing plates | Boundary walls | Subballast |
 | **Full scale railway track tests** | Summary and ongoing work







Summary and ongoing work

- Spherical particles are useful for evaluating the macroscopic behaviour of the track (not valid, for example, to analyse the distribution of contacts)
- The DEM can accurately reproduce the behavior of rails and bearing plates making easy the coupling with railway ballast discrete particles
- The numerical tool presented allows the user to test different situations:
 - Ballast granulometry or properties
 - Sleepers design
 - Bearing plates and rails

RESILTRACK (Resilience of Railway Infrastructures Against Climate Change)



- Analysing how to measure track deflections in a real railway track section (high-speed if possible)
- Searching more data to validate conical damage parameters and ballast fouling conditions
- Testing other particle geometries (clusters of spheres) more similar to ballast particles

Thank you for your attention!

Questions?

jirazabal@cimne.upc.edu