INFLUENCE OF THE LENGTH OF A CYLINDER ON ITS AEOLIAN TONE LEVEL: MEASUREMENT AND MODELLING

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Abstract. The tonal noise generated by the flow over elongated cylinders is measured using microphones in the anechoic wind tunnel BETI of Institut Pprime. The effect of the length to diameter ratio of the cylinder is assessed by varying the diameter from 6 mm to 20 mm within the constant width (750mm), open jet, test section. The velocity is varied from 10 to 40 m/s, leading to a Reynolds number range of about 4,000 – 53,000. A proper normalization is needed to obtain a good collapse of experimental data from nearly 10 studies on the same evolution in 3 steps: for very short cylinders, the tone level does not depend on the length; for semi-long cylinders, it follows the fourth power of the length to diameter ratio; for very long cylinder, the length's influence vanishes in the form of a sound level asymptote. This sigmoidal evolution is noticed for both the circular section and the square section cylinders, and questions the classical modelling of the aeroacoustic process using compact, coherent segments of cylinder associated with a coherence length to account for spanwise phase loss. Literature data from numerical simulation or experiment using end-plates are included in the analysis too.

1 INTRODUCTION

The overall goal of this work [1] is the specific influence of shape on aeroacoustics. We choose the simple case of long cylinders as a model for airframe noise. For such a configuration, the flow is determined by the regime, in terms of Reynolds number (Re) and Mach number (Ma), and by the geometry of the body, in terms of cross-section shape and span ℓ . For almost all the shapes, and at the majority of unsteady regimes, the flow is characterised by periodic vortex shedding, which generates a tonal acoustic radiation. The adimensionalized frequency of the tone is the Strouhal number (St), and its level has been modelled

in the literature by [2–7]:

$$\bar{P}^2(r) = \frac{\rho_0^2 U_\infty^2 \text{St}^2 \ell_c C_L^2}{16 c_0^2 r^2} \quad (1)$$

where $\bar{P}^2$ is the acoustic pressure energy in the transverse direction, ρ_0 and c_0 are the density and speed of sound, respectively, in the ambient, U_∞ is the inflow velocity, r is the microphone distance from the cylinder. The two remaining quantities are key ingredients of the aeroacoustic efficiency: C_L' is the root mean-square of the sectional lift coefficient and ℓ_c is the spanwise correlation length. In this work, we have questioned the factor $\text{St}^2 \ell_c C_L^2$ from an aeroacoustic design point of view, that is asking about what we could tell to designers, who have neither the time nor the mean to conduct computational aeroacoustics, about what will happen in the acoustic field if they change the geometry.

With this approach in mind, several investigations has been combined including numerical [8–11], theoretical [12, 13] and experimental [14, 15] approaches. The analysis of the microphone signals for different diameters of a circular cylinder lead us to notice a specific influence of span to diameter ratio on the noise level, which is the subject of the present paper.

This is crucial for numerical simulations, and that is how it matches the scope of this symposium about aeroacoustic modelling and numerical simulation. A typical situation occurs when a 2D simulation is conducted, or a 3D one over a relatively short span. In order to validate the simulation, it is compared with experimental data of far-field pressure. But how can the acoustic field from a 2D simulation be compared with measurements? And, in general, the span is longer in the experiment than in the 3D simulation... To enable such comparisons, some correction methods [16–19] have been elaborated to extrapolate the simulation to the span used in the experiment. These correction methods are based on the concept of coherence length of the fluctuating lift, and on adding the contribution of elementary segments of the actual cylinder, with phase relationships depending on retarded time and on whether a segment is shorter or longer than the coherence length. That is why an experimental investigation of the influence on span on aeroacoustic radiation is conducted and used to assess the typical curves obtained with these correction methods.

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The paper is organised as follows: in Section 2 are introduced the present measurements in aeroacoustic wind tunnel. Then available experimental data of noise level emitted by the circular cylinder flow are discussed in Section 3. In Section 4, the influence of length to diameter ratio exhibited by this data is described and compared to the behavior of correction methods. The bad news is that they are different, but this opens the way to a modelling challenge...

2 MEASUREMENTS IN AEROACOUSTIC WIND TUNNEL

The cylinder is fixed in the open-jet section of BETI which is the aeroacoustic wind tunnel of Institut Pprime, as shown in Figure 1. The upstream velocity was between 10 and 40 m/s. The most important parameters here are the exit nozzle, square section side of 70 cm, the anechoic chamber cutoff frequency around 200 Hz, and the microphone distance is one meter. The acoustic pressure signal is recorded during one minute at the sampling frequency of 12.8 kHz. The noise spectra are estimated using Welch periodogram method, with a frequency resolution of 1.56 Hz.

The cylinder is larger than the jet so its effective length is close to that of the jet itself, that is $\ell \approx 70$ cm. The diameter d is varied from 6 to 20 mm, which leads to a range of 35 to 117 for the span to diameter

Figure 1: Photo of the anechoic chamber of the wind-tunnel BETI - Institut Pprime, France (left), and diagram of the experimental setup with the microphone array (right). The lower wall of the collector is extended in order to adapt the setup for a fully open jet configuration.

ratio ℓ/d . Six values of the inflow velocity U_∞ were considered in the wind tunnel range, up to 40 m/s, which corresponds to a very low Mach number (from 0.03 to 0.12). In terms of Reynolds number, these values of the diameter and velocity lead to a range from 4,000 to 50,000, when taking $1.5 \times 10^{-5} \text{ m}^2/\text{s}$ for the kinematic viscosity of air. However, in order to ensure that the three-dimensionalization of the flow be similar, only the cases with a Reynolds number higher than 10,000 were considered in the analysis of the influence of span. The Strouhal number being around 0.2, the tone frequency ranges from 100 Hz to a little bit more than 1 kHz. Again, in the analysis of the influence of span, we had to select the cases with a tone frequency above 250 Hz in order to avoid a bias in the tone level estimation due to the anechoic chamber frequency cutoff.

As an overview of the measurement results, the power spectral density for the different diameters with the flow at 20 m/s is shown in Figure 2 (left). Note that the Reynolds number is different between the curves. The spectra are qualitatively similar, with a well marked peak at Strouhal number 0.2. Two harmonics are well visible. Moreover, Figure 2 (right) is based on the influence of the flow rate on the overall sound pressure level (OASPL), that is the integration of the power spectra over the frequencies. It is well fitted by the sixth power law derived by Curle using a compact source assumption.

3 REVIEW AND NORMALISATION OF LITERATURE DATA

In order to compare literature and present results, a proper normalisation of the data is needed to account for the different setup and parameters. Consistently with the theoretical formula (1) shown in the introduction, we considered a scaled sound pressure energy $\bar{p}^2$, which is the squared acoustic pressure, corrected by the microphone distance to diameter ratio, and divided by the dynamic head, and the Mach number to recover the U_∞^6 power law, namely:

$$\bar{p}^2 = \left(\frac{r}{d}\right)^2 \frac{\bar{p}^2(r)}{\rho_0^2 U_\infty^4} \frac{c_0^2}{U_\infty^2} \quad (2)$$

The other quantities from (1) that depend on the regime are hard to measure in the same campaign or have weaker influence of the sound radiation for a given shape at similar Reynolds number. A corresponding

Figure 2: Acoustic pressure power density spectrum for the flow over circular cylinder at $U_\infty = 20$ m/s (left), and overall sound pressure level as a function of flow velocity (right). In the legends, the quantity in millimeters is the diameter d and that in parenthesis is the length to diameter ratio ℓ/d . Both graphs are for microphone 4, see Figure 1 (right).

level in dB is defined as usual:

$$SSPL = 10 \log_{10}(\bar{p}^2) \quad (3)$$

Regarding the criteria for comparison, one may consider the overall sound pressure level (OASPL), the level at the peak frequency or the energy contained within a band around the peak. Within the frame of this paper, only results for the OASPL are presented, while a complete discussion including the two other criteria is given in [1]. With the above normalisation (2) and fixing the spectral quantity, the remaining variables in the theoretical formula (1) are the span ℓ , the coherence length ℓ_c , and the lift fluctuation C_L .

In Table 1, are listed these studies reporting aeolian tone OASPL that we have been aware of. Naturally, the two main categories are the experiments and the simulations. Important parameters to consider when making comparisons are the microphone distance, the velocity, and, as we will see, the length to diameter ratio and the end-condition in the experiments. As illustrated in Figure 3, this can be open, as for the present measurements, when the cylinder is longer than the jet. When it is shorter, or when one end is free for a mounted cylinder, then the setup is called a finite cylinder. Finally, some investigations use end plates, and then the setup is called closed.

Now that the present measurements has been described and the tools for comparison with literature have been set up, the influence of length to diameter ratio is investigated in the next section.

Figure 3: Classification of experimental configurations listed in Table 1.

Table 1: Studies reporting OASPL for circular cylinder flow, in chronological order within each configuration defined in Figure 3.

		reference	r , m	d , mm	U_∞ , m/s	Re	ℓ/d
Open jet measurements							
[20]	▽	Reyell et al. (1977), experimental	2.438	19.05	70.08	89,000	25.3
[21]	○	Iglesias et al. (2016), experimental	1.4	12	20-50	16,400 – 41,100	22
	□	present, experimental	1	6-20	10-40	4,000 – 53,333	35-116.67
Finite or mounted cylinder							
[22]	+	King & Pfizenmaier (2009), experimental	1.4	20	32-69	42,400 – 91,400	2-35
[23]	:	Morreau & Doolan (2013), exp. - wall-mounted	0.515	6	25-35	10,000 – 14,000	1.6-22.6
Closed wind tunnel or cylinder with end-plates							
[24]	●	Fink et al. (1976), experimental	2.25	51	31-125	105,000 – 258,000	15.43
[25]	◀	Iida et al. (1996), experimental	1.000	40	3.75-52.5	10,000 – 140,000	12.5
[6]	▼	Casalino & Jacob (2003), experimental	1.380	16	20	22,000	18.75
[26]	★	Sueki et al. (2010), experimental	2.000	25-45	27.7	46,000 – 83,000	13.33-24
Numerical simulations							
[27]	*	Cox et al. (1998), 2D URANS - fully correlated	2.438	19.05	68.00	90,000	5-26.3
[28]	■	Orselli et al. (2009), 2D URANS - fully correlated	2.430	19	71.05	90,000	2.5-25.3
[28]	▶	Orselli et al. (2009), 3D LES - corrected	2.430	19	71.05	90,000	25.3
[29]	×	Karthik et al. (2018), 3D LES + FW-H	1.400	20	64	84,770	3-35
[30]	+	Du & Sun (2019), 3D DNS + periodic FW-H	2.438	19	68	1,000	4-248

Figure 4: Influence of span to diameter ratio on the overall, scaled sound pressure level measured in circular cylinder flow. For experimental setups of the cited works, see Table 1. The full line is the sigmoid law (4). Dashed lines show the ℓ/d fourth power slope.

4 INFLUENCE OF LENGTH TO DIAMETER RATIO

4.1 Experimental data

The relevancy of the present scaling (2) can be noticed in Figure 4 where the data has been reported from experimental study only. There is a noteworthy collapse of the data on the same evolution for the “open” and “finite” configuration (the data for “closed” configurations are discussed hereafter). In particular, the two studies for finite cylinders of different length [22, 23] (+, •) show very similar values, which are interestingly corroborated by two experiments (∇ , $\circ$) for fixed length. The present data ($\square$) does not lay in the same range of span to diameter ratio, however it allows to complete the description of the influence of this geometrical parameter. The latter goes in three steps: for short span, namely $\ell/d \leq 10$, the scaled level appears almost constant; there, the sound radiation may be dominated by 3D dynamics at cylinder end or interaction with the boundary layer [23]. For $10 \leq \ell/d \leq 30$, a very strong increase of SSPL with increasing span is noted, which may corresponds to a dominance of the tonal radiation associated with lift fluctuation at the shear-layer flapping frequency. For longer cylinders, present data shows a saturation of the SSPL, possibly due to destructive interferences between source regions along the span.

This three-step evolution can be modelled by a sigmoid function, that is an algebraic growth between two constants:

$$\log_{10}(\bar{p}^2) = \frac{\pi}{1 + \beta \left(\frac{\ell}{d}\right)^{-\gamma}} + \log_{10}(\bar{p}_0^2) \quad (4)$$

with $\beta \approx 11,630$, $\gamma = -3$ and $\bar{p}_0^2 \approx 3.559 \times 10^{-4}$, obtained by non-linear regression [1]. Although the quality of the regression is good, there is some dispersion. In particular, the influence of velocity is not

fully accounted by the sixth power law, resulting in level differences for the same span to diameter ratio in most of all the experiments.

One surprising result is the slope of the curve in the intermediate range, that is for cylinders 15 to 30 diameter long. The fourth power slope bounds the data quite well, while the maximum slope of the sigmoid curve is even greater. Before discussing this further, the data from experiments using end plates, that is the closed configuration, shall be considered. Available data is only for the intermediate spans, but, as shown in Figure 4, the scaled level is systematically higher than for the finite or open configuration of same span to diameter ratio. This level increase has been explained in the literature by a stabilizing effect of end plates on the flow [22, 31] or by an acoustic effect such as reflexion and image sources. In spite of this level difference due to the setups, the influence of span seems to remain unchanged. The fourth power slope is very clear for the data from Sueki *et al.* [26] (★), which is also well consistent with that from Casalino & Jacob [6] (▼). The two other studies [24, 25] (•, ◀) reported results for a single span at different velocities, leading to more dispersion, but they do not contradict the trend.

This fourth power slope is surprising because the classical formula (1) leads to a maximum slope of two, yet this would only be obtained if the lift were in phase all along the span. Actually, ℓ_c , the spanwise correlation or coherence length is rather of a few diameters at these regimes. This means that the theory behind this formula misses something about the influence of span or about the link between span, spanwise coherence and sectional lift.

4.2 Assessing models and correction methods

The present framework, using pressure level normalisation and use of the span to diameter ratio as parameter, allows to put on the same graph data from different experiments as well as from numerical simulations, as proposed in Figure 5. For clarity, the experimental values for closed configurations have been removed from the plot. However, by comparison with Figure 4, it can be seen that numerical simulations generally return higher levels than the closed configuration itself. This may be attributed to the artificial increase of phasing resulting from the short simulated span and the turbulence model.

Nevertheless, Orselli *et al.* [28] found a similar trend with ℓ/d (Fig. 8 Stn. [30]) but with a higher value of the acoustic level for large spans that has been obtained in the present measurements (◻). But these three studies (*, ■, +) that tested different spans reported levels that follow a square law, consistently with the method they used to extrapolate their 2D or short span flow simulation to larger span acoustic prediction. Moreover, the value reported by Orselli *et al.* [28] using a correction method (▶) is consistent with a linear increase of the scaled level with ℓ/d adjusted for a same radiation of the segment used for the flow simulation.

Finally, only the recent 3D simulations of finite cylinders by Karthik *et al.* [29] (×) seem to return a higher slope for intermediate spans like that noticed in the experiments.

5 CONCLUSION

While investigating the influence of cross section shape on aeolian tone level, a very strong influence of the span itself has been unearthed. Three distinct behaviors have been observed, being the medium cylinder range ($10 < \ell/d < 30$) the most driven one by the cylinder span. For all regions in graph, observed trends do not align with classical compact cylinder noise description. It should be remarked that the sigmoid evolution with high slope for intermediate spans has been noticed for the square cylinder too,

Figure 5: Influence of span to diameter ratio on the overall, scaled sound pressure level reported in experimental and numerical studies. For material and methods of the cited works, see Table 1. The full, green line is the sigmoid law (4). Dashed lines and dash-dotted line show the ℓ/d second and first power slope, respectively. Full, grey line for visual aid only.

with the same constant for short bodies [1]. The described asymptote for $\ell \rightarrow \infty$, discussed previously only in numerical extrapolations of short, fully phased cylinders, indicates an advantageous behaviour when considering the noise emission of very long cylinders like cables.

Back to the classical formula (1), the span could influence the acoustics through coupled modification of the correlation length and the sectional lift fluctuation. Or the present observations may be considered as

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