AN IMMERSED BOUNDARY METHOD BASED FLUID-STRUCTURE INTERACTION SOLVER WITH APPLICATIONS IN ENERGY HARVESTING

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Abstract. We present the development of an in-house fluid-structure interaction (FSI) solver and employ the solver for state-of-the-art applications in energy harvesting. An implicit partitioned approach is utilized to couple a sharp-interface immersed boundary method based flow solver and a finite-element method based structural solver. The code validations are presented for large-scale flow-induced deformation and vortex-induced vibration of an elastically mounted circular cylinder. We employ the FSI solver for analysis of vortex-induced vibration (VIV) of a cylinders, with different cross-sections. The suppression and agitation of VIV for different cylinders are discussed along with lock-in characteristics. An energy harvesting model is utilized to estimate the power generated per unit mass and it was found that the galloping of the D-cylinder is useful for broadband energy harvesting for a wide range of reduced velocities.

1 INTRODUCTION

Flow-induced vibration (referred as FIV hereafter) is an area of interest for many researchers due to its ubiquitous presence in several engineering problems. Most of the applications include FIV suppression to prevent the possible catastrophic damages being caused on the system. In the last decade, another application of FIV in wind and water based energy harvesting has been studied. The conventional wind energy harvesters or wind turbines operate in a very confined range of wind speeds (3 to 25m/s[1]). Despite being highly efficient, the logistics constraints and the hazardous effects on the residing living beings[2], limit the use of wind turbines in very narrow region of the wind velocity. Similarly, the most commonly used water based energy harvesters i.e., hydroelectric power plants, mostly depend on the reservoir creation over a flowing water body, which alters surrounding ecosystem. An FIV based system does not require stagnating flowing water body and has relatively less moving parts, it may overcome the previously mentioned limitations. Another important application of FIV based devices is improve the convective heat transfer. The vortices produced during FIV could interact with heated wall and improve

the transfer by reducing the thermal boundary layer thickness [3].

In the context of the energy-harvesting, Rostami and Armandei [4] have extensively reviewed the energy harvesting potential of FIV based systems. The energy is harnessed from the FIV system, primarily, in two ways. First way is using an electromagnetic coil mounted on the vibrating body to harvest electrical energy from the relative motion of the magnet and coil [5]. A second way is mounting piezoelectric energy harvester on the surface of the deforming body [6]. A comparative study done by Soti et al. [7] shows a very good agreement of average power for the constant damping energy harvesting model, with a more complex electromagnetic energy harvesting model. Therefore, for a simplistic analysis, energy harvesting potential of the systems has been investigated using the constant damping energy harvesting model. Bearman, in his notable review [8], concluded that a study of various different shapes is necessary to explore the complete potential of FIV system. Additionally, the study by Zhang et al. [9] shows significant improvement in energy harvesting potential with changing shapes of the elastically mounted structure. Therefore, the present study focuses on the the energy harvesting potential of various cross-sections. The comparison of energy conversion efficiency and power extraction has been performed to illustrate the best cross-section of the body, based on the specific applications and constraints. The simulations are performed at $Re = 200$, assuming a two-dimensional flow.

In order to computationally tackle the above-mentioned problems, immersed boundary method is a good candidate and challenging problems including those with large-scale flow-induced deformation. Such cases have been successfully simulated with reasonable fidelity in previous studies [10]. In the present work, we employ a validated fluid-structure interaction (FSI) solver to demonstrate the energy harvesting by elastically mounted circular, D-section and inverted D cylinder. First, we briefly present the governing equations and code validations of the FSI solver (section 2 and 3) and next, we present simulation set up, FIV response and associated energy harvesting potential (section 4) of the the three cylinders considered.

2 GOVERNING EQUATIONS

The present study utilizes an in-house sharp-interface immersed boundary method based Fluid-Structure interaction solver. The governing equations in fluid domain include incompressible continuity and Navier-Stokes equation expressed in non-dimensional form as

$$\frac{\partial u_i}{\partial x_i} = 0 \quad (1)$$

$$\frac{\partial u_i}{\partial t} + u_j \cdot \frac{\partial u_i}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{1}{Re} \frac{\partial^2 u_i}{\partial x_j \partial x_j} \quad (2)$$

The structural vibration is modeled using single degree of freedom approximation in non-dimensional form as

$$\ddot{y} + \frac{2\pi\xi}{Ur} \dot{y} + \frac{4\pi^2}{Ur^2} y = \frac{F^*}{m^* A_s^*} \quad (3)$$

The central difference discretized equations are solved using a fractional step Van-Kan method. The convective term is solved using Crank-Nicolson scheme and the diffusive term is solved using Adam-Bahsforth method. The pressure poisson equation is solved using the geometric multigrid method. A one-way coupling is introduced from fluid to structural using a sharp-interface immersed boundary coupling.

Figure 1: Schematic of the proposed FSI benchmark by Turek and Hron [17].

The structural equations are solved using Eulers method, and flow field is updated with new structural boundary coordinates. The details of computational method can be found in [11, 12]. The method has been extended for large scale deformations [13] and thermal buoyancy effects [14] during fluid structure interaction. An implicit partitioned approach is utilized to couple a sharp-interface immersed boundary method based flow solver and a finite-element method based structural solver. The implicit coupling has been accelerated using a dynamic under-relaxation scheme [15].

3 CODE VERIFICATION

The in-house solver has been verified for flexible as well as elastically mounted rigid structure. In our previous studies [15, 16], the solver was validated against the FSI benchmark, proposed by Turek and Hron [17], in which a thin, finite thickness, elastic splitter plate is attached to the lee side of a circular rigid cylinder, subjected to laminar flow (Figure 1). In this two-dimensional benchmark, Reynolds numbers (Re), based on cylinder diameter is 100 and the flow induces a wave-like deformation in the plate, and it attains a periodic self-sustained oscillation. The comparison of computed time-varying displacement of the tip of the plate with published data is shown in Figure 2. The plate exhibits self-sustained large-scale flow-induced deformation and therefore this benchmark is well-suited to test the fidelity on an FSI solver. Next, an elastically mounted circular cylinder placed in a cross-flow, in the presence of a constant damping. The maximum displacement amplitude, lift force and phase difference are plotted in Figure 3 and show good agreement with the results of Leontini et al. [18].

4 RESULTS AND DISCUSSION

Elastically mounted cylinders of different cross-sections, namely, circular, D-section and inverted D-section have been considered at $Re = 200$ with constant mass ratio $m^* = 10$. Reduced velocity Ur has been varied in the range of [2, 11.5]. The domain size of $47D \times 30D$ and grid size of $0.02D$ have been selected for the current study. This size is based on the previous studies [19, 3], performed on similar systems and utilizing the same in-house solver. The structure is located at $15D \times 15D$ from the bottom left corner of the considered domain (Figure 4). The left wall is imposed with uniform inlet flow with velocity $u = 1$. The top and bottom wall are imposed with free slip boundary conditions to approximate an open domain flow. The right wall is imposed with a developed flow or convective boundary condition. The simulation setup along with boundary conditions is shown in Figure 4.

Figure 2: Comparison of computed displacement of the tip of the elastic plate with data of Turek and Hron [17]. Adapted from Manjunathan and Bhardwaj [16].

Figure 3: Comparison of (a) A_{max} , (b) C_{Lmax} and (c) ϕ calculated using in-house solver for circular cylinder at $Re = 200$, $m^* = 10$ and $\xi = 0.01$ with data of Leontini et al. [18].

Figure 4: Schematic of simulation setup used in the present study.

The maximum amplitude of the vibration of various cross-sections has been plotted with varying reduced velocities in Figure 5. The D section cylinder shows significantly higher vibration amplitude as compared to inverted D and circular cylinder. The primary reason is the onset of galloping for D section cylinder [20]. Additionally, the inverted D section cylinder shows nearly same amplitude vibrations as the circular cylinder. This implies that the same amplitude of inverted D-section cylinder can be obtained with half of structural material.

The non-dimensional power output shows maximum power generation for circular cylinder, despite its amplitude of vibration being significantly smaller than the D section cylinder (second frame, Figure 5). This caused by the capability of high inertia structures to sustain high damping coefficients at same damping ratio. However, a higher power generation per unit mass is observed for D-section cylinder of the structural material (third frame, Figure 5). This aspect is important if material cost is significant. Additionally, the reduction in power generated by D-section cylinder is much lower with increasing Ur , as compared to the circular cylinder. This implies that the D-section cylinder could be used as a broadband energy-harvester. The inverted D section cylinder generates similar power per unit mass as the circular cylinder. Further, the energy conversion efficiency is computed per unit fluid power present in the area swept by the structure (fourth frame, Figure 5). While D-section cylinder exhibits the largest amplitude of vibration, the efficiency is not the largest and lower than that for the circular cylinder. The energy efficiency is the highest for the circular cylinder for $4.5 < Ur < 6.5$ and D-section provides a reasonably larger efficiency over a wide range of reduced velocity.

5 CONCLUSIONS

We have reported the development of an fluid-interaction interaction (FSI) solver based on sharp-interface immersed boundary method and finite-element method. The code validations were carried for large-scale

Figure 5: Amplitude response (first frame), power output (second frame), power output per unit structure mass (third frame) and energy conversion efficiency (fourth frame) of the different cross-section cylinders considered in the present work.

flow-induced deformation of a splitter plate and vortex-induced vibration of an elastically mounted cylinder on a linear spring in laminar flow. These tests demonstrate the fidelity of the solver proposed. The solver has been employed to understand the flow-induced vibration response of elastically mounted cylinders of different cross-sections. We have found that the D-section cylinder shows significant increase in the amplitude for a wide range of reduced velocity as compared to circular and inverted D-cylinder. The large amplitude vibration at larger reduced velocity for the D-section cylinder is attributed to galloping behaviour. The cylinders were tested for the potential of energy harvesting and D-section was found to generate the largest power per unit mass for a wide range of the reduced velocity, among the three cylinders considered. Our study provides insights while designing broadband energy harvester capable for high power generation.

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