NONLINEAR BEHAVIOUR OF TWO-WHYTE STONE WALLS

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Abstract. Engineers work hard to convert the highly uncertain and nonlinear behavior of historic masonry structures into something that can be understood with mathematical certainty. Therefore, practical and also accurate structural analysis techniques are still needed for the preserve the historical monuments as a huge cultural heritage. In this context, determining the mechanical properties of historical walls under in-plane and out-of-plane lateral loadings is one of the most important aim. This study aims to investigate the three dimensional (3D) nonlinear behaviour of stone walls subjected to a combination of lateral and vertical loads using appropriate constitutive numerical modeling. For this purpose, a simplified micro modeling approach has been proposed for the 3D nonlinear finite element analysis (NLFEA) of stone wall. The dry-stone masonry wall from the literature has been used in the verification step for the proposed model. After that, the new two-whyte stone wall has been constructed in accordance with the original material characteristics derived from the experimental studies and tested under shear compression. Finally, numerical results of NLFEA and experimental results of walls have been compared. It was observed that the numerical analysis results are well matched with the experimental ones.

1 INTRODUCTION

Masonry historic structures represent architectural cultural heritage of great historical importance in Turkey. They have been used for public and residential buildings in the past several thousand years. A great number of well-preserved old masonry structures still exist proving that this form of construction can successfully resist loads and environmental impact [1]. Conventionally, most major buildings were solid walled structures with the walls bearing directly on the ground. Historical masonry structures are exposed to horizontal and vertical
loads and atmospheric influences throughout their entire life. These structures are composed of many layers and due to the weak connections between the weak materials and gaps, the masonry walls in these structures tend to leave the building. For this reason, damages, cracks, gaps may occur as a result of environmental impacts in historical masonry structures and even dangerous situations can occur [2]. Since these damages are directly related to the loads affecting the structure, it is very important to investigate the complex and nonlinear behavior of the structures by numerical analysis [1,3–5].

The primary aim of this study is to present an effective modeling procedure for the stone masonry walls under shear and compression. For this purpose, in the first part of this study, the mechanical properties of stone and mortar samples provided from a historical masonry structure in Turkey have been determined at laboratory conditions. Then, the two-whyte stone wall which have nominal dimensions 1010x1005x280 mm (lenght x height x width) have been constructed in the laboratory of Yildiz Technical University in accordance with the original material characteristics derived from the experimental studies. In order to evaluate the nonlinear behaviour of two-whyte stone wall, these wall have been tested under shear-compression. Then this experimental study has been modelled in ABAQUS-6.14 package [6]. An experimental study conducted by Lorenco et. al., which involved dry stone masonry walls under a combination of vertical preloading, and in-plane horizontal shear loading has been selected for the verification of the numerical modeling technique. After that, experimental and numerical results of constructed in laboratory were compared.

2 NUMERICAL AND CONSTITUTIVE MODELING

A number of experimental and analytical studies have been conducted on the behavior of masonry shear walls to reach a comprehensive understanding of complex masonry behavior [[1,3,7–12]]. Proposed theoretical models for implementation to finite element analysis of masonry generally require a large number of material parameters that are difficult to measure easily and reliably. For this reason, several attempts have been made to express the stress-strain relationships of the masonry and its constituents using different modeling techniques such as micro-modeling, homogenization approach and macro-modeling. The common approach is to treat masonry as a continuous medium with the exception of micro-modeling. Micro-modeling should describe the masonry, mortar and the interaction behavior between them. It has been revealed in literature that micro models are more suitable for modeling small structures and the studies in which the interaction between mortar-stone and/or failure modes are important. On the other hand, in macro models, the structural elements are modeled as homogeneous (brick/stone and mortar are modeled together) and the stress-strain relations and fracture surfaces of these elements are described first. Macro models are more useful for larger structures and when the behavior of the entire structure is investigated. In this study, micro modeling technique is adopted for nonlinear analysis of masonry stone walls.

Multi-axial stress states defines the constitutive behavior of the structures such as masonry walls, RC panels, confined columns or elements beyond the elastic range. The basic elastoplastic constitutive models, i.e Mohr-Coulomb (MC) and Drucker-Prager (DP) are widely adopted in constitutive modeling materials, like concretes, soils and rocks [4,13]. Drucker-Prager (DP) yield/break criterion is the most practical mathematical form of the von-Mises criterion used for concrete, metal and stone type materials, and takes into account both
hydrostatic pressure and deviator stress effects at the highest strength (Figure 1)[9]. According to the DP yield criteria, the yield surface can be expressed as follows [6]:

\[ f(I_1, J_2) = \alpha \cdot I_1 + \sqrt{J_2} - k = 0 \]  

(1)

where \( \alpha \) and \( k \) values are material constants and these values depend on the internal friction angle (\( \phi \)) and cohesion (\( c \)) values in the MC criterion. Internal friction angle (\( \phi \)) and cohesion (\( c \)) values can be expressed as [6]:

\[ \alpha = \frac{2 \sin \phi}{\sqrt{3}(3 - \sin \phi)} \quad k = \frac{6c \cos \phi}{\sqrt{3}(3 - \sin \phi)} \]  

(2)

The MC criterion takes into account the effect of hydrostatic pressure. The MC yield surface is in the form of a hexagonal cone in the deviatoric stress plane. Figure 2 shows yield surface in the principal stress space and \( \pi \) plane [9]:

The MC criterion shows the linear envelope curve obtained from the shear strength of the
material against the applied normal strength [9]. This relationship is expressed as follows [6]:

\[ \tau = c - \sigma \tan(\phi) \]  

(3)

where \( \tau \) is shear strength, \( \sigma \) corresponds to normal stress which is negative in compression, \( c \) is cohesion and \( \phi \) is the internal friction angle. From Mohr's circle [6]:

\[ \tau = \sigma \cos \phi \quad \sigma = \sigma_m + s \sin \phi \]  

(4)

Substituting for \( \tau \) and \( \sigma \), multiplying both sides by \( \cos \phi \), and reducing, the Mohr-Coulomb model can be written as [6]:

\[ s = \sigma_m \sin \phi - c \cos \phi = 0 \]  

(5)

where \( s \) is half of the difference between the maximum principal stress, \( \sigma_1 \), and the minimum principal stress, \( \sigma_3 \) (and is, therefore, the maximum shear stress),

\[ s = \frac{1}{2}(\sigma_1 - \sigma_3) \]  

(6)

and \( \sigma_m \) is the average of the maximum and minimum principal stresses, and \( \phi \) is the frictional angle [6]:

\[ \sigma_m = \frac{1}{2}(\sigma_1 + \sigma_3) \]  

(7)

3 SOFTWARE IMPLEMENTATION OF PROPOSED CONSTITUTIVE MODEL

Three dimensional (3D) finite element models have been used for stone masonry walls. Masonry constituents, e.g. stone and mortar, are assumed to be isotropic elasto-plastic obeying DP criterion and modeled separately with eight-node brick element (C3D8) [6]. Besides, the mortar thickness and the brick–mortar interface are lumped into a surface to surface interaction while the dimensions of the brick unit are expanded to keep the geometry of a masonry structure unchanged (Figure 3) [6]. In this modeling technique, a surface interaction consist of normal behaviour and tangential behaviour [6]. Constitutive model mentioned above has been used for the numerical simulations of sample stone masonry walls.

![Figure 3: Simplified micro-modeling technique and surface to surface contact [6]](image)

Lourenco et. al. [3], tested 1000x1000x200 mm dry stone masonry walls under a combination of vertical preloading, and in-plane horizontal shear loading (Figure 4). Brick dimensions were used as 200x200x100 mm and 100x100x100 mm in this tests. Two connected hydraulic jacks (N) were placed on the wall while the shear load was applied to the
wall by a horizontal hydraulic jack (P). In this study, the vertical load levels adopted for the tests were 30, 100, 200, and 250 kN. These load values lead to compressive normal stresses of 0.15, 0.50, 1.00, and 1.25 MPa, respectively. A numerical simulation of the tested stone walls was carried out with the Abaqus software [6]. Mechanical properties for test wall and values adopted for FE analyses are given in Table 1, respectively. Both simulation model and laboratory test results agreed very well (Figure 5). Also deformed shape of the experimental and numerical model of the wall was given in Figure 6 [3].

**Table 1.** Comparison of Experimental and Numerical Parameters

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Experimental [3]</th>
<th>Numerical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight (kN/m³)</td>
<td>25</td>
<td>25</td>
</tr>
<tr>
<td>Young's Modulus (MPa)</td>
<td>1202</td>
<td>2000</td>
</tr>
<tr>
<td>Poisson's ratio</td>
<td>0.2</td>
<td>0.2</td>
</tr>
<tr>
<td>Friction angles</td>
<td>32</td>
<td>32</td>
</tr>
<tr>
<td>Dilatancy angles</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Flow stress ratio</td>
<td>-</td>
<td>0.8</td>
</tr>
<tr>
<td>Yield stress (kPa)</td>
<td>-</td>
<td>9000</td>
</tr>
<tr>
<td>Friction coefficient</td>
<td>0.39</td>
<td>0.39</td>
</tr>
<tr>
<td>Vertical load (kN)</td>
<td>250</td>
<td>250</td>
</tr>
</tbody>
</table>

![Figure 4: Experimental setup of dry stone masonry wall [3]](image)

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5
Figure 5: Comparison of experimental and numerical analysis results

Figure 6: Experimental and numerical comparison of failure mechanism [3]

In the experimental part of this study, the two-whyte stone masonry wall with dimensions of 1010x1005x280 mm were produced in accordance with the orginal material characteristic (Figure 7). The constituents and mix proportions of produced mortar were selected to be compatible with historical lime based mortar specimens. Mechanical parameters of two-whyte stone masonry wall are given in Table 2. The specimen sizes used in mechanical experiments for stone (cylindrical) are different from stone which used in the two-whyte masonry stone model wall. Assuming that the increase in size increases defects (cracks, gaps, etc.) in the specimen, Young’s modulus and uniaxial compressive strength values have been decreased in numerical analysis (Table 2).

At the 28th day after the construction, the wall was subjected to increasing lateral load under a constant, uniformly distributed vertical load. The loading apparatus consisted of a
2000 kN and 500 kN capacities hydraulic rams for vertical and horizontal loading, respectively. Instrumentation included two load cells and four displacement transducers (Figure 8). Vertical pre-compression distributed loading of 1.06 MPa was applied to the top surface of a steel plate with a thickness of 3.5 cm located on the center of wall. Lateral loading was then applied at a rate of 0.6±0.1 kN/s. For repairing and strengthening issues, the stone test wall was not loaded to failure (total destruction was not proposed). As shown in Figure 8, when a stair step crack appeared and extended diagonally across the wall, the test was stopped. Finally, experimental and numerical analysis results of two-whyte masonry wall were compared (Figure 9). Also deformed shape of the numerical model of the two-whyte masonry wall was given in Figure 10.

Table 2. Experimental and Numerical Parameters of two-whyte stone masonry wall

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Experimental (stone brick)</th>
<th>Numerical (stone brick+mortar)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weight (kN/m²)</td>
<td>25</td>
<td>25</td>
</tr>
<tr>
<td>Young's Modulus (MPa)</td>
<td>13000</td>
<td>5000</td>
</tr>
<tr>
<td>Poisson's ratio</td>
<td>0.28</td>
<td>0.28</td>
</tr>
<tr>
<td>Friction angles</td>
<td>52</td>
<td>52</td>
</tr>
<tr>
<td>Dilatancy angles</td>
<td>-</td>
<td>10</td>
</tr>
<tr>
<td>Flow stress ratio</td>
<td>-</td>
<td>0.8</td>
</tr>
<tr>
<td>Yield stress (kPa)</td>
<td>49000</td>
<td>10000</td>
</tr>
<tr>
<td>Friction coefficient</td>
<td>-</td>
<td>0.5</td>
</tr>
</tbody>
</table>

Figure 7: Geometry for the two-whyte stone masonry wall
Figure 8: Experimental set-up

Figure 9: Comparison of experimental and numerical analysis result for two-whyte masonry wall
4 CONCLUSIONS

In the present paper, Drucker-Prager (DP) type plasticity is proposed to model the in-plane non-linear structural behavior of stone walls. In order to evaluate the accuracy of proposed simplified micro modeling technique, numerical results of a nonlinear finite element analysis (NLFEA) are compared with the test results of two walls. The following conclusions are drawn from the results:

1. The material parameters of DP criterion for both masonry units and mortar that are considered separately as isotropic and homogeneous materials is expressed in terms of the cohesion and the internal friction angle of Mohr-Coulomb (MC) criterion in this study. Therefore, the surfaces of both DP and MC yield criteria are made to coincide along the compression meridian.

2. For dry stone and two-whyte stone masonry walls, cracks mostly follow along cement mortar joints in a stair step manner.

3. Comparison of the wall responses subjected to vertical and lateral loads between analytical and experimental results, especially for dry stone masonry wall, indicates reasonable agreement except the shape of the load-displacement curves for both mortar joint and dry joint masonry after peak point. The reason for this is that there exists no gradually developing damage defined in the elasto-plastic model.

REFERENCES


