Euglenids exhibit an unconventional motility strategy amongst unicellular eukaryotes, consisting of large-amplitude highly concerted deformations of the entire body (euglenoid movement or metaboly). A plastic cell envelope called pellicle mediates these deformations. Unlike ciliary or flagellar motility, the biophysics of this mode is not well understood, including its efficiency and molecular machinery. We quantitatively examine video recordings of four euglenids executing such motions with statistical learning methods. This analysis reveals strokes of high uniformity in shape and pace. We then interpret the observations in the light of a theory for the pellicle kinematics, providing a precise understanding of the link between local actuation by pellicle shear and shape control. We systematically understand common observations, such as the helical conformations of the pellicle, and identify previously unnoticed features of metaboly. While two of our euglenids execute their stroke at constant body volume, the other two exhibit deviations of about 20% from their average volume, challenging current models of low Reynolds number locomotion. We find that the active pellicle shear deformations causing shape changes can reach 340%, and estimate the velocity of the molecular motors. Moreover, we find that metaboly accomplishes locomotion at hydrodynamic efficiencies comparable to those of ciliates and flagellates. Our results suggest new quantitative experiments, provide insight into the evolutionary history of euglenids, and suggest that the pellicle may serve as a model for engineered active surfaces with applications in microfluidics.

Uncellular microorganisms have developed effective ways of locomotion in a fluid, overcoming fundamental physical constraints such as the time reversibility of low Reynolds number (Re) hydrodynamics (1). Amongst eukaryotes, most species swim beating cilia or flagella. Yet, through a long evolutionary history, some protists have developed unconventional functional strategies, accomplished by highly diverse subcellular structures (2). A notable example is the euglenoid movement, or metaboly, executed by some species of euglenids (3). This peculiar motility mode is characterized by elegantly concerted, large amplitude distortions of the entire cell with frequencies of about \( f \approx 0.1 \) Hz (4). Euglenids have attracted the attention of scientists since the earliest days of microscopy, when van Leeuwenhoek referred to them in 1674 as microscopic motile “animalcules” that were green in the middle, which challenged the classification of organisms into animals and plants (5). More recently, metaboly has inspired models for artificial microswimmers (6), although even its locomotory function remains unclear. In contrast with flagellar or ciliary motion, the euglenoid movement has not undergone close biophysical scrutiny, and fundamental questions remain open, including a precise understanding of the actuation mechanism leading to the body shape changes, or its hydrodynamic efficiency. Because all euglenids move primarily with their flagella, it is difficult to discern the role of the body distortions in the observed motion.

Euglenids are abundant in a wide range of aquatic environments and, with typical sizes from tens to hundreds of micrometers, are easily observed by optical microscopy. They display a striking diversity in terms of morphology, nutrition (phagotrophs, phototrophs, osmotrophs), and motility, making of euglenids an excellent system to study evolution (7, 8). As other protists, they cannot resort to cell specialization to accomplish vital functions. Instead, they encapsulate all the functionality required for survival in a single cell, with an elaborate machinery revealed by ultrastructural studies. Euglenids are enclosed by a striated surface with two opposing poles called pellicle. The pellicle, the major trait of morphological diversity in the group, is a cortical complex consisting of the plasma membrane, a set of interlocking proteinaceous strips, microtubules, and tubular cisternae of endoplasmic reticulum arranged along the strips (3). The ability of euglenids to undergo metaboly has been correlated with the morphology of the pellicle. Flexible pellicles possess a large number of articulated strips (a few tens) often wrapped helically around the cell, whereas rigid pellicles can have as few as four fused strips arranged either helically or along the meridians of the cell. Some euglenids exploit their body flexibility to merely round up, elongate, or gently bend. Here, we focus on the most extreme oscillatory motions displayed by some species.

Detailed observations of *Euglena fusca*, possessing a pellicle decorated by easily traceable particles, have shown that shape changes are accompanied by sliding between adjacent pellicle strips (9, 10); as the shape changes, the pellicle strips retain their length and width, but change their helicity. This mechanism is consistent with the commonly observed twisting motions around the long axis of the cell accompanying metaboly. These pellicle rearrangements are thought to be driven by the sliding of microtubule complexes relative to the proteinaceous strips and controlled by calcium sequestration in the tubular cisternae of endoplasmic reticulum. Although the molecular motor has not been identified, the active motions are thought to be fueled by ATP (11). Further experimental interrogation of metaboly with modern biophysical techniques is still lacking.

The euglenoid movement confronts us with far reaching biological and biophysical questions. One such issue is the competitive advantage of metaboly. Although metaboly is an oddity in microscopic locomotion, it has persisted through natural selection coexisting within individuals with flagellar motility in a significant part of the phylogenetic tree of euglenids. Another intriguing aspect of metaboly is the operation of the distributed machine that elegantly and robustly executes the body motions, and that may inspire man made active envelopes. As a first step, our goal here is to understand the kinematics and hydrodynamics of the euglenoid movement. For this purpose, we quantitatively analyze movies of metaboly recorded by others, representative of common observations by protistologists and physical scientists interested in motility (4). We examine these recordings with statistical learning methods. We then propose a model for the pellicle kinematics, which establishes a precise connection between distributed actuation and shape changes. Finally, we assess...
by numerical simulations the hydrodynamic features of the euglenoid movement.

Quantitative Observations

Data and Methods. We start from video recordings of four photo synthetic specimens, labelled euglenid #1 through #4, three of which are of the genus *Eureptiella*, and the fourth belongs to either a *Euglena* or a *Eureptiella* species. We assume that these euglenids remain essentially axisymmetric as they undergo met aboly, in agreement with their general description (12) and with detailed scrutiny of the movies studied here (see Fig. S1). Therefore, they can be described by their generating curve in the symmetry plane.

From the viewpoint of low Re locomotion, a swimming stroke is a closed path in shape space, which needs to be nonreciprocal to accomplish net motion. We next propose a method to identify and parametrize such a path for further quantitative examination (see Fig. 1). In recent years, statistical learning methods have been increasingly used to understand stereotyped animal behavior, see, e.g., related studies on the motility of *Caenorhabditis elegans* (13, 14). Because the stroke is expected to be a nonlinear manifold of dimension one, here we resort to a nonlinear dimensionality reduction technique called Isomap (15). This method identifies nonlinear correlations of high dimensional data points (here snapshots of the cells describing their shape) by embedding them in low dimensions in a geometry preserving manner.

First (Fig. 1A), we gather the collection of shapes adopted by each euglenid by segmenting and aligning the video frames. We represent numerically the shape of each frame by fitting a spline curve to the boundary of the aligned segmentation. Second (Fig. 1B), we identify the geometric structure underlying the set of shapes (*i*) with Isomap. We embed the shapes in 2D (*ii*) to examine the nature of the path described by the euglenids in shape space. Because the shape ensemble is essentially a one dimensional loop, we further embed the shapes in a periodic 1D segment labelled by τ (*iii*), where the frames are ordered by shape proximity. With the 1D embedding, we parametrize the geometric stroke smoothly (ν). This procedure filters some of the noise while closely following the data; see Fig. S2 *A* and *B*. The resolution of the result is limited by optical artifacts and images out of focus, which bias the segmentation, and possibly by slight departures from axisymmetry. Yet, the quality of the numerical stroke is sufficient for quantitative examination (see Movie S1).

Because our method is based on geometric similarity, τ measures arc length in shape space rather than physical time. The hydrodynamic efficiency depends on geometric similarity, τ measures arc length in shape space rather than physical time. Therefore, they can be described by their generating curve in the symmetry plane.

Results. We find that nonlinear dimensionality reduction reveals vividly the signature of low Re swimming for each of the four euglenids, with well defined nonreciprocal paths in shape space over the many cycles captured in the movies (Fig. 2 and Fig. S3A). Different specimens perform geometrically distinct strokes (Fig. S2C), and, for a given specimen, each stroke is executed multiple times with the same pace; i.e., the relation between τ and t is nearly the same over several strokes (Fig. 2B and Fig. S3D). With the numerical stroke at hand, we first examine elementary features such as the surface area $S(\tau)$ and the volume $V(\tau)$ enclosed by the pellicle. We express volume in nondimensional terms as the reduced volume $v = 6\sqrt{\pi}V/\mathcal{S}^{3/2}$, the ratio between the cell volume and the volume of a sphere with the same surface area. Thus, $v$ ranges between 0 to 1. We find that the surface area of the four euglenids remains nearly constant along the stroke, with deviations below 5% (Fig. S3C). This observation is consistent with the hypothesis that pellicle deformation is mediated by relative sliding of pellicle strips, which retain their length and width (9). Such a deformation is called simple shear in continuum mechanics, and preserves area locally. The small area deviations may be due to the systematic errors in

![Fig. 1](https://www.scipedia.com) Quantitative analysis of the movies: method. (A) The frames are segmented and aligned to obtain images of $F_a$ containing information about the shape alone, devoid of translation, rotation, or textures. A B spline curve, given by its control polygon $P_a$ (black circles), is fitted to the boundary of $F_a$ and is a generating curve of the axisymmetric representation of the pellicle. Original frame image courtesy of Richard E. Triemer. (B) The segmented and aligned frames (*i*), representative of the shapes adopted by the cell, are embedded in low dimensions by a nonlinear dimensionality reduction technique called Isomap (15). The algorithm maps each frame to a low dimensional point (circles in *ii* and *iii*, color labeling chronological order), so that the intrinsic distance between frames (shape dissimilarity) is preserved as much as possible by the low dimensional representation. The embedding in the plane (*ii*), shows that the stroke is a closed nonreciprocal path in shape space. Consequently, it can be most compactly described by embedding the frames in a periodic 1D segment (*iii*), from which we parametrize the stroke as a function of τ by interpolation (*iv*) with smooth basis functions $w_a(\tau)$. At any given τ, the synthetic stroke is a weighted average of the curves fitting video frames whose 1D embedding is in the vicinity of τ. The parameter τ is not proportional to physical time, ignored by the manifold learning algorithm, but rather to arc length in shape space. See SI Text, section Video Processing and Parametrization of the Stroke, for technical details.

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Fig. 2. Quantitative analysis of the movies: results. (A) Two dimensional embedding of a stroke plotted against video frame number, showing the shape and pace uniformity of the stroke over several realizations. Isomap identifies similar shapes from different realizations (here about four cycles) and yields a single geometric stroke. (B) Pseudo time parameter \( t \) against normalized physical time \( t' \) during three full strokes represented in different colors, showing that path in shape space is traveled with a well defined pace (here, euglenid #3). The black line shows the fit used to reparameterize time. (C) Reduced volume, \( \nu \), as a function of time during two strokes. We distinguish two distinct motility styles: a volume changing style for euglenids #1 and #2, and a volume preserving style for euglenids #3 and #4. See Fig. S3 for the full data.

Fig. 3. Pellicle kinematics theory. (A) Surface strain (the \( 2 \times 2 \) matrix \( C \)) is derived assuming simple shear along the strips, \( \gamma \), acting on a reference pellicle. The reference pellicle configuration (iii) is defined by a shape and a pellicle conformation, given by the tangent vector fields \( s_0 \) and \( m_0 \), along the strips and perpendicular to them, or by the angle \( \phi_0 \) between the pellicle strips and the surface parallels. (ii) Ultrasound of the pellicle (transmission electron micrograph from ref. 7, Copyright 2001 The Society for the Study of Evolution), and depletion of the sliding between adjacent strips causing the pellicle shear. (B) Surface strain, \( C \), is now derived by comparing a reference configuration, (iii), given by \( r_0(\lambda) \) and \( z_0(\lambda) \), where \( \lambda \) is the body coordinate, and a deformed configuration (iv), given by \( r(\lambda), z(\lambda) \) and the azimuthal displacement relative to a fixed direction \( \psi(\lambda) \). The red point denotes a material particle attached to the pellicle, and \( \gamma' \) denotes differentiation with respect to \( \lambda \). Matching the microstructural (A) and the shape derived (B) expressions for the strain, we find equations relating pellicle shear, pellicle deformation, shape changes, and internal forces.

We obtain a first expression for \( C \), depending on the reference pellicle orientation and the pellicle shear, Fig. 3A. On the other hand, comparing the reference state with a new configuration, given by \( r(\lambda), z(\lambda) \), and the azimuthal displacement \( \psi(\lambda) \), we obtain a second expression for \( C \); Fig. 3B. Matching the two expressions, we find the relation between the global deformation \( C \) and the local shear \( \gamma(\lambda) \).

Here, we have obtained from the movies a trajectory of shapes, \( r(\lambda, t) \) and \( z(\lambda, t) \). The theory then provides expressions for the associated azimuthal displacement \( \psi(\lambda, t) \) and the pellicle shear \( \gamma(\lambda, t) \), from which in turn we evaluate the full velocity field and the deformation of the deformed pellicle along the stroke. The theory can also be used to evaluate the deformed pellicle shape and helicity resulting from a prescribed pellicle shear \( \gamma(\lambda, t) \) acting on a reference configuration, although we do not explore here the design of strokes.

The theory imposes a constraint on the shapes achievable from a given reference pellicle; namely, \( r_0 / r_0 \geq |\sin \phi_0| \). Consider a reference pellicle with strips parallel to the meridians; i.e., \( \phi_0(\lambda) = \pi/2 \). Then the shape at instant \( t \) is accessible from the reference pellicle if \( r(\lambda, t) \geq r_0(\lambda) \), consistent with the fact that the parts of flexible pellicles display strips with almost no helicity. We can access all the shapes of the stroke by defining \( r(\lambda) \) as the smallest radius adopted by the material parallel \( \lambda \), and integrate \( z(\lambda) \) from local area preservation. This procedure defines an optimal reference pellicle for each euglenid, which achieves the observed shapes with minimal pellicle shear at every point; we adopt this reference pellicle in the absence of detailed imaging.

Results. Fig. 4 summarizes the application of our theory to the four euglenids, highlighting the link between distributed actuation, pellicle configuration, and shape. The reconstructed pellicle shears \( \gamma(\lambda, t) \) of the four euglenids exhibit distinct patterns, but...
also common features. A bump of high pellicle shear near the head of the cell (snapshot a) travels toward the tail (snapshots b and c). This traveling shear bump reflects in the shape as a bulge that moves from head to tail, reminiscent of peristaltic movements. When it reaches the tail, the shear bump decays while a new one appears at the head (snapshot d) before the cycle closes. Euglenid #1 exhibits the bluntest pattern and shape trajectory, and only reaches pellicle shears of 250%. In contrast, Euglenid #4 shows shears of pellicle shears, reaching 340%, with a corresponding well defined bulge that slides along a cylindrical body of nearly constant radius. Some species of osmorrophic genera, such as *Asaia* and *Distigma*, exhibit a similar swimming style to the photo synthetic euglenid #4. With an estimated pellicle width of \( w \approx 250 \text{ nm} \), we predict a sliding displacement between adjacent strips of up to \( \delta \approx 850 \text{ nm} \) for this euglenid. By differentiating the map of \( \gamma(t, t) \) in Fig. 4, we find that \( \dot{\gamma} \) reaches 20%/Hz, leading to a maximum sliding velocity of \( \delta = 20w \approx 500 \text{ nm/s} \), consistent with the velocities of molecular motors along microtubules (17, 18). The similarity between our pellicle reconstructions and observations of flexible pellicles, with a clear correlation between radius and pellicle orientation, is remarkable.

**Hydrodynamics of the Stroke**

Combining the movie processing and the theory for the pellicle kinematics, we compute the surface velocity during the strokes, and analyze the hydrodynamics by placing the model euglenids in a Newtonian fluid. With a typical size of 50 \( \mu \text{m} \) and a stroke frequency \( f \approx 0.1 \text{ Hz} \), we estimate \( \text{Re} \approx 10^{-4} \). We solve the Stokes equations with a boundary integral method, and the linear velocity along \( z \) and the azimuthal spin of the cell are calculated from the self-propulsion condition (19); see SI Text, section Hydrodynamics, for details. We assume that volume changes are accommodated by a uniform normal permeation velocity. The fluid velocity at the pellicle is then the surface velocity plus the permeation velocity, which is not very significant even for the volume changing euglenids #1 and #2 (see Fig. S6).

Table 1 summarizes the kinematic features and swimming performance of the four euglenids (see Table S1 for additional data). We evaluate the swimming performance with the linear displacement in one stroke \( U \) (measured in units of body length \( 2R = \sqrt{s^2} / s \), and with Lighthill's efficiency \( \text{Eff}^\text{ligh} \). The conventional notion of efficiency is defined as the ratio between the power needed to drag the swimmer at the average velocity \( U / T \) and the average power exerted by the swimmer on the surrounding fluid, \( \bar{W}_{\text{int}} \). To account for volume change shape continuously, we consider \( \text{Eff}^\text{out} = 6\pi \eta RW^2 / P^\text{out} \), where \( \eta \) is the fluid viscosity. We find that all euglenids move by a few tenths in a body length in one stroke, and exhibit efficiencies in the order of 1%. With the typical frequencies of metaboly, the swimming speeds are very low, \( U \approx 1 \text{ m/s} \), between one and two orders of magnitude smaller than during flagellar locomotion. Remarkably, the hydrodynamic efficiency is comparable to that estimated for ciliates and flagellates (20). We find that euglenid #1 is the slowest and least efficient swimmer, followed by #2 and #3, with comparable performance, and finally #4 is the best, with a displacement of 40% of the body length per stroke and \( \text{Eff}^\text{out} = 2.0\% \). The table suggests that swimming performance is correlated with maximum pellicle shear. The best swimmer is a volume preserving specimen with the lowest reduced volume, \( P_{\text{out}} \).
Fig. 5. Stroke hydrodynamics of euglenid #4. (A) Flow pattern around the pellicle at selected instants along the stroke. The fluid velocity field in the symmetry plane is indicated by blue arrows, and the azimuthal component is shown with isocurves, where green is zero, blue negative, and red positive. (B) Relationship between actuation and forward motion, where the vertical axis is the body coordinate \( \lambda \) for the color map of \( \gamma(\lambda, t) \) and \( t \) position (average between the head and the tail) in units of body length for the curve in blue. Both the actuation pattern and the forward motion clearly delineate a power and a recovery phase in the stroke.

Discussion

Our study suggests many new questions. A number of quantitative experiments could test and complement our theory. A detailed kinematical picture of the pellicle during metabolism can be obtained in vivo by light microscopy under ultraviolet illumination (23), while particle image velocimetry (24) can resolve the hydrodynamics and shed light on the inflow and outflow management of volume-changing euglenids. Our observation about the volume variations challenges the predominant conceptual models of swimming at low Re (6, 25), although swimmers permeating fluid across a fixed body shape have been analyzed (26). It is not clear if volume changes are passive, as a consequence of the pellicle deformation, or if these two phenomena are regulated in concert. Experiments on extracted cell models suggest that the euglenid movement is mediated by a spatiotemporal nonuniform calcium stream that triggers the pellicle activity (11). This mechanism could chemically drive water perforation, which may enhance the exchange of nutrients and wastes. It is known that photosynthetic euglenids can acquire nutrients by osmotrophy.

Having established that metabolism is a component motility mode, the evolutionary benefit of such a large biological investment remains unclear when coexisting with flagella, an alter- native theories suggest that the earliest ancestors, rigid and feeding on small bacteria, developed a flexible pellicle to engulf larger eukaryotic prey. Photosynthetic species evolved from phagotrophic algae, and some of these lost the pellicle flexibility by strip fusing (8). Presumably, the pellicle flexibility may have found a secondary utility, besides mediating in eukaryotic motility, and may have persisted because of this in photosynthetic euglenids such as those studied here, as well as in some osmotrophy. The benefit of metabolism may be related to the stirring of the cytosol or the surrounding medium, or to locomotion. Inter estingly, many euglenids live in interstitial, soil rich, or eutrophic water, suggesting that metabolism may be particularly well suited to move in “difficult” conditions such as confined environments, or in media of complex rheology, known to affect flagellar efficiency (20, 27). This hypothesis is supported by a marine phototrophic species, lacking emergent flagella but exhibiting strong metabolism, known to migrate vertically through the sand of the benthic zone in diurnal cycles (28). Thus, the heterogeneity of the biophysical traits of metabolism could complement the morphological and molecular data used in current phylogenetic studies of euglenid, and provide new clues about their evolutionary history.

Besides complementing experimental observations to obtain a complete kinematical picture of metabolism, the theory for the pellicle deformation provides the background for further biophysical studies. It is possible to optimize the pellicle shear to achieve maximal efficiency, and investigate the role of volume constraints or different dissipation metrics. Similar studies have brought new insight for cilia (29), flagella (30, 31), and model swimmers...
undergoing full body distortions (22, 32, 33). Furthermore, the theory can be used to compute the resisting forces, arising from the internal and external friction and from the pellicle bending elasticity, that need to be overcome by metabolic activity.

The pellicle suggests itself as an appealing design concept for an active material (34). The local actuation of the pellicle produces a local strain incompatible with the current geometry, which is only realizable by further curving and producing shape changes (35). Similar concepts of material as machine relying on martensitic materials have been put forth (36, 37), and actually operate in biological organisms such as the tail sheath of bacteriophage T4 (38). Viewed as an active surface, the pellicle exhibits an interesting balance between shape flexibility and controllability, which explains why metaboly is such an elegantly con
certed motion as compared, e.g., with the amoeboid movement. The pellicle has a single degree of freedom available for the local surface deformation, the pellicle shear, which nevertheless is sufficient to realize a wide family of shapes. Observations show that flexible eucliden can perform bending and torsional maneuvers of remarkable agility, including sharp turns. A general theory considering nonuniform pellicle shears in the azimuthal direction may delimitate the possibilities of this shape actuation concept, which may find applications in artificial microswimmers or peristaltic micropumps.

Conclusions

We have provided a detailed biophysical analysis of the eucliden movement, a widely appreciated but poorly understood motility mode of euclidens. We have developed a statistical learning methodology to analyze strokes and applied it to four movies recorded by others. We have established the shape and pace uniformity of the strokes, and have parametrized the motions in a computer model. Some euclidens exhibit very large variations of their body volume during the stroke, while others keep their volume constant. A kinematical theory, assuming that the cell surface deforms by simple shear along pellicle strips, provides a precise link between distributed actuation and shape changes, explains common observations about the pellicle helicity, and provides the input for hydrodynamics. Metaboly is found to be a slow but efficient motility mode in water, which enhances stirring of the cytosol and the surrounding fluid, and may be advanta
geous in granular or complex media.

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