

SEISMIC EVALUATION OF CONCRETE DAMS VIA CONTINUUM DAMAGE MODELS

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SUMMARY

In this paper a general methodology for the analysis of large concrete dams subjected to seismic excitation is outlined. It is valid both for gravity dams (2D representation) and arch dams (3D representation). The method allows for non-linear material behaviour of the dam, "transparent fictitious boundaries" for properly dealing with in-coming and out-going seismic waves, and an efficient procedure to deal with dam-soil-fluid interaction. The mechanical behaviour of concrete is modelled using an isotropic damage model which allows for tension and compression damage, and exhibits stiffness recovery upon load reversals. Emphasis is placed in the treatment of fluid-structure interaction, regarding both formulation and efficiency aspects. A gravity dam and an arch dam are analysed subjected to artificially generated earthquakes of different intensities, and the results are used to study the degree of (un)safety of the dams.

1. INTRODUCTION

The safety evaluation of concrete dams subjected to severe seismic actions poses several difficulties to the structural analysts because it involves the solution of a complex non-linear coupled problem. The first, but not the only, difficulty is the highly non-linear mechanical behaviour of concrete in these situations, which inevitably include fracture under tension with triaxial states of stress and repeated load-unload reversals. Of course, there is a wide variety of different material models for concrete that could be used in these studies. The available literature includes models based on the theories of hypoelasticity, hyperelasticity, plasticity, fracture mechanics, plastic-fracture, or continuum damage, to name only some of the more popular ones. The present work will make use of a *continuum damage model* to characterize the mechanical behaviour of concrete. The Continuum Damage Theory was firstly introduced by Kachanov¹ in the context of creep-related problems, but it has afterwards been accepted as valid alternative to deal with complex material behaviour. It is nowadays used for materials so different as metals, ceramics, rock and concrete, and

within a wide range of applications (creep, fatigue, progressive failure, etc.). The reason for its popularity is as much the intrinsic simplicity and versatility of the approach, as well as its consistency, based on the theory of thermodynamics of irreversible processes. Among the different possibilities that such a framework offers²⁻⁸, this work will make use of an *isotropic damage model*, with only two scalar internal variables to monitor the local damage under tension and compression, respectively. This will provide a simple constitutive model which, nevertheless, is able to capture the overall non-linear behaviour of concrete displayed under seismic loading, including the strain-softening response and the stiffness degradation and regradation observed under multiple stress reversals. Furthermore, the model can be implemented in a strain-driven form which leads to an almost closed-form algorithm to integrate the stress tensor in time. This is a most valuable feature for a model intended to be used in large scale computations^{5,9}.

Seismic analysis of a dam is a fluid-structure interaction problem. These coupled problems are of great importance in many branches of engineering. In earthquake engineering the problem is usually augmented because in most cases the foundation must be taken into consideration, yielding a fluid-structure-soil model to be solved. This is a typical coupled problem. In fact, it is the archetypical example of a class of coupled problems where interaction occurs at the interface between different physical domains. Here, neither the structure nor the fluid can be solved independently of the other: motion of the structure depends on the hydrodynamic pressures at the interface, and pressures in the fluid depend on the normal acceleration at the wet wall. It must also be considered that earthquake excitation reaches the structure travelling through the soil region around the structure. This means that soil-structure interaction has to be modelled in some way. In this work a block-iterative technique is used to deal with the discrete fluid-structure coupled problem¹⁰⁻¹³. This has proved to be a simple and natural approach, as well as computationally efficient, particularly when the non-linearity and the coupling are treated within the same iteration loop. Both formulation and efficiency aspects of this approach will be briefly discussed in the following sections.

Finally, it must be remarked that in these analyses both the water in the reservoir and the soil in the foundation are semi-infinite unbounded domains. For static or quasi-static loading, a fictitious boundary at a sufficient large distance from the structure can be introduced in the computational model. The physical domain is hence "cut off", expecting that from the practical point of view, the structural response will not be affected. However, for dynamic loading this procedure cannot be used. The fictitious boundary would reflect out-going waves back into the domain of interest, spoiling completely the computed solution for any practical purpose. Thus, it is necessary to model appropriately the fictitious boundaries to allow the in-coming seismic waves to enter into the domain, as well as to ensure that the out-going waves are not reflected. The necessary treatment of the boundary conditions in the computational model to account for this will also be discussed below.

From the computational point of view, there are three different physical phenomena to be modelled in the seismic analysis of a concrete dam: the structural behaviour of the dam (the final goal of the analysis), the mechanical behaviour of the soil (both as the supporting medium of the dam and as the transmitting medium of the seismic waves), and

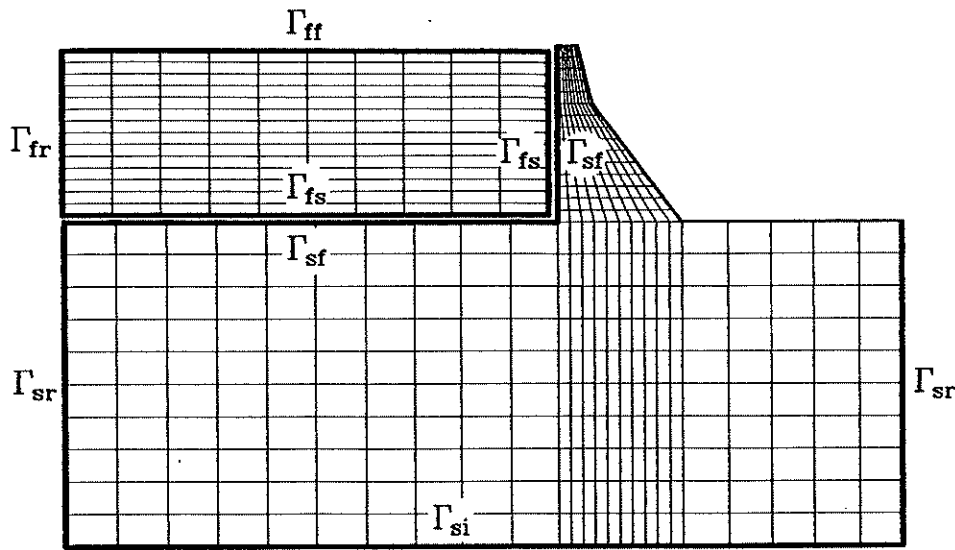


Figure 1. Computational model showing the dam with the foundation and the reservoir

the behaviour of the water in the reservoir (as a transmitting medium of acoustic waves travelling from and towards the up-stream wall of the dam). Therefore, the computational model includes the following elements (see Figure 1):

- A displacement based non-linear dynamic model for the dam. As commented above, the non-linear behaviour is accounted for here by means of a simple and computationally efficient constitutive equation belonging to the family of the so-called 'continuum damage models'. It is also necessary to include appropriate structure-fluid interaction boundaries.
- A displacement based linear dynamic formulation for the soil. Here, 'transparent' boundaries (for out-going and in-coming seismic waves) have to be included.
- A pressure based wave propagation formulation for the water in the reservoir. Additionally, appropriate 'transparent' (out-going waves) radiating boundaries, fluid-soil and fluid-structure interaction boundaries and free surface boundaries need to be included.

Having these general features in mind, the paper is organised as follows. Section 2 describes the structural computational model, with especial reference to the boundary conditions and the constitutive model. Section 3 describes the computational model for the fluid phase of the problem (water in the reservoir). Section 4 deals with the coupled fluid-structure problem, with emphasis on its block-iterative solution. Section 5 discusses some alternatives for approaching the seismic evaluation of concrete dams. Sections 6 and 7 present the application of the proposed methodology to the seismic analysis of a gravity and an arch dam, respectively. Section 8 closes the paper with some conclusions on the proposed methodology.

2. STRUCTURAL COMPUTATIONAL MODEL

2.1 Dynamic equilibrium equation

Without going into details, the semidiscrete dynamic equilibrium equation for the structural part of the model (dam+foundation), arising from the standard Galerkin spatial discretization, reads¹⁵:

$$\mathbf{M}_s \ddot{\mathbf{a}} + \mathbf{C}_s \dot{\mathbf{a}} + \mathbf{S}(\mathbf{a}) = \mathbf{f}_s \quad (1)$$

where subscript s refers to the solid phase in the problem. The notation involved in Eq. (1) is as follows. The mass and damping matrices are \mathbf{M}_s and \mathbf{C}_s , $\mathbf{S}(\mathbf{a})$ is the vector of internal forces in the solid ($\mathbf{S}(\mathbf{a}) = \mathbf{K}_s \mathbf{a}$ if a linear constitutive model is adopted, where \mathbf{K}_s is the stiffness matrix), \mathbf{f}_s is the vector of external forces (including the seismic and the interaction forces, see below for details), $\mathbf{a} = \mathbf{a}(t)$ is the vector of nodal displacements unknowns and the dot denotes differentiation with respect to time t . If the displacements \mathbf{u} inside a finite element are interpolated in the standard way given by the shape functions \mathbf{N}_s and the nodal displacements \mathbf{a} , the expressions for matrix \mathbf{M}_s and vectors $\mathbf{S}(\mathbf{a})$ and \mathbf{f}_s are easily obtained. The damping matrix accounts for both the natural viscous damping (assumed to be of Rayleigh type) and the radiation boundaries (see below for details).

2.2 Boundary conditions

In the solid domain (dam+foundation) there are three types of ‘especial’ boundaries to be considered in the fluid–structure problem (see Fig. 1):

- (a) Solid–fluid interaction boundary (Γ_{sf}): in the fluid–structure problem the coupling occurs through the interface surface, noted here as Γ_{sf} and Γ_{fs} if considered as belonging to the solid or the fluid, respectively. Defining a unit vector \mathbf{n} normal to this surface (pointing outwards from the solid), the nodal forces on the solid due to the pressure in the fluid can be computed as,

$$\mathbf{f}_{sf} = - \int_{\Gamma_{sf}} \mathbf{N}_s^T \mathbf{n} P d\Gamma = - \int_{\Gamma_{sf}} \mathbf{N}_s^T \mathbf{n} \mathbf{N}_f \mathbf{p} d\Gamma = -\mathbf{Q} \mathbf{p} \quad (2)$$

where subscripts s and f refer to the solid and the fluid, respectively. P is the pressure in the fluid, \mathbf{p} is the corresponding vector of nodal pressures and \mathbf{N} represent the shape function matrices. The rectangular matrix \mathbf{Q} is the coupling matrix. Note that if the pressure in Eq. (2) is the total pressure, the forces will include the hydrostatic effects.

- (b) Radiating or ‘transparent’ boundary (Γ_{sr}): It is possible to derive a fictitious boundary that will damp completely the elastic waves that reach it, providing these outgoing waves are plane and are propagating in a direction normal to the boundary^{12,14}. This boundary provides tractions which are proportional to the velocities in the medium, and, therefore, its effects after the spatial discretization process will be a contribution to the damping matrix of the system that can be written as,

$$\mathbf{C}_{sr} = \int_{\Gamma_{sr}} \mathbf{N}_s^T \mathbf{T}^T \mathbf{D}_r \mathbf{T} \mathbf{N}_s d\Gamma \quad (3)$$

where \mathbf{D}_r is a diagonal matrix depending on the density and the elastic constants of the solid, and \mathbf{T} is an appropriate transformation matrix depending on the orientation of the boundary. In the general case the given expression is only an approximation to a real absorbing boundary, but numerical experiments show that the error involved in this approximation is acceptable from an engineering point of view.

- (c) Radiating boundary with incoming wave (Γ_{si}): the fictitious boundary at the bottom of the model must be able to damp the out-going elastic waves and, at the same time, be able to allow the prescribed in-coming seismic waves to enter the domain. Under the same assumptions that for the previous case, the corresponding boundary will contribute to the damping matrix and to the vector of nodal forces. The corresponding expressions are^{12,14}

$$\mathbf{C}_{si} = \int_{\Gamma_{si}} \mathbf{N}_s^T \mathbf{T}^T \mathbf{D}_r \mathbf{T} \mathbf{N}_s d\Gamma \quad (4.a)$$

$$\mathbf{f}_{si} = 2 \int_{\Gamma_{si}} \mathbf{N}_s^T \mathbf{T}^T \mathbf{D}_r \mathbf{T} \dot{\mathbf{v}} d\Gamma \quad (4.b)$$

where $\dot{\mathbf{v}}$ is the prescribed in-coming velocity wave. Note that in this way the seismic input is introduced as a ‘natural’ condition in the model, in terms of the ground velocities. This is different from the traditional approach, where the seismic input is prescribed as a ‘forced’ condition, in terms of the ground accelerations. The advantage is that now we are able to write Eq. (1) in terms of the total displacements, velocities and accelerations in the structure, rather than ‘relative’ to the ground. The formulation is clearer in this way, and note that there will be no ‘forced’ boundary conditions (prescribed displacements) in the structural model.

Note that we have made explicit the expressions for the nodal forces due to the water and the seismic input. Apart from these the vector \mathbf{f}_s in Eq. 1 will typically contain only the system of self-weight nodal forces. It may also be remarked that in many applications is not necessary to make use of the fictitious boundaries of type (b). If the portion of foundation included in the computational mesh is large enough, these can be substituted by a ‘repeatability condition’, prescribing the displacements in the left-hand side of the model to be equal to those in the right-hand side^{12,25}. This is satisfactory for most of 2D and many 3D applications, although naturally this will always depend on the actual geometry of the problem.

2.3 Discretization in time. Algorithmic and natural damping

Due to the non-linearity introduced in the computational model through the constitutive equation for concrete, the internal force vector $\mathbf{S}(\mathbf{a})$ is a time-history dependent quantity. Therefore, the dynamic equilibrium equation (1) must be solved in the time domain, following a step-by-step procedure. There are several methods in the literature available for

the discretization and integration in time of such second order equations. In this work we will make use of the well-known and widely employed Newmark method, but others equally suitable would be the SS22 method, the α -method, or the Houbold's or Park's methods^{15,16}. Each of these methods has its own characteristics regarding stability and accuracy. It must also be remarked that because of the non-linear nature of Eq. (1) it will be most convenient to use any of the previous methods in a predictor-multicorrector form, using a scheme such as the Newton-Raphson method to linearize the equations for each time step of the time integration process^{12,17}.

Because the higher modes of semidiscrete structural equations are spurious subproducts of the discretization process and not representative of the governing partial differential equations, it is generally viewed as desirable, and often is considered absolutely necessary, to have some form of algorithmic damping present to remove the participation of the high-frequency modal components. This is even more crucial in non-linear analysis¹⁸. In terms of the Newmark method, the parameters γ and β determine the characteristics of stability and accuracy of the method. It is necessary to choose $\gamma > 1/2$ to introduce high-frequency dissipation. For a fixed γ one can choose $\beta = (\gamma + 1/2)^2/4$ to maximize this dissipation while retaining unconditional stability. However this leads to a drop to first order accuracy of the method. If this is not acceptable, the α -method can be used, which can introduce algorithmic dissipation while retaining unconditional stability and second order accuracy^{16,18}.

The energy dissipation due to tensile (and eventual compressive) damage is explicitly considered in the constitutive model for concrete. However, it will be seen that this does not contemplate energy dissipation in a load-unload-reload cycle, as it would be desirable under seismic excitation. This added damping effect may be heuristically considered via the damping matrix C_s . Due to the lack of experimental results on the damping mechanisms of mass concrete dams under seismic loading we will follow the usual finite element procedure of assuming a Rayleigh type of damping, i.e.,

$$C_s = aM_s + bK_s \quad (5)$$

which preserves the symmetry and positive-definiteness of matrices M_s and K_s . With this type of damping the damping ratio ξ_r corresponding to an undamped frequency ω_r is

$$\xi_r = \frac{1}{2} \left(\frac{a}{\omega_r} + b \omega_r \right) \quad (6)$$

The constants a and b are calibrated to provide the desired amount of damping in two selected modes of the dam, typically 3–10 % in the first and second modes. It is clear from Eq. (6) that the effect of the 'mass damping' will be negligible for the higher modes, while the 'stiffness damping' will severely damp them. It is therefore desirable to include in the computational model a significant part of 'stiffness damping', as this will help to damp out the high-frequency components of the response. It has to be remarked that as damage occurs inside the dam the stiffness will also be degraded. Thus, it may be discussed if the stiffness matrix in Eq. (5) should be the initial (elastic) one, or an updated tangent or secant matrix¹⁸. The question is open to different considerations, but for reasons of computational efficiency we will use a constant damping matrix in the present work.

2.4 Constitutive model for concrete

The Continuum Damage Mechanics Theory is based on the definition of the effective stress concept, which is introduced in connection with the hypothesis of strain equivalence²: the strain associated with a damaged state under the applied stress σ is equivalent to the strain associated with its undamaged state under the effective stress $\bar{\sigma}$. In the present work the effective stress tensor $\bar{\sigma}$ (second order) will assume the following form:

$$\bar{\sigma} = \mathbf{D}_0 : \epsilon \quad (7)$$

In this expression \mathbf{D}_0 is the usual fourth order linear-elastic constitutive matrix, ϵ is the second order strain tensor, and $(:)$ denotes the tensorial product contracted on two indices. As our aim is to use a scalar damage model, with separated internal damage variables for tensile and compressive stress contributions, a split of the effective stress tensor into tensile and compressive components is needed. In order to clearly identify contributions respecting to each one of these independent effective stress tensors, (+) and (-) indices will be extensively used, referring to tensile and compressive entities, respectively. In this work, the stress split will be performed as¹⁹:

$$\begin{aligned} \bar{\sigma}^+ &= \langle \bar{\sigma} \rangle = \sum_{i=1}^3 \langle \bar{\sigma}_i \rangle \mathbf{p}_i \otimes \mathbf{p}_i \\ \bar{\sigma}^- &= \langle \bar{\sigma} \rangle^- = \sum_{i=1}^3 \langle \bar{\sigma}_i \rangle^- \mathbf{p}_i \otimes \mathbf{p}_i \end{aligned} \quad (8)$$

where $\bar{\sigma}_i$ denotes the i -th principal stress from tensor $\bar{\sigma}$, \mathbf{p}_i represents the unit vector associated to its respective principal direction and the symbol \otimes denotes the tensorial product. The symbols $\langle . \rangle$ are the MacAuley brackets (thus giving the value of the enclosed expression when positive, and setting a zero value if negative), and symbols $\langle . \rangle^-$ are such that $\langle x \rangle^+ + \langle x \rangle^- = x$.

Hence, according to this stress splitting, the constitutive law proposed in this work can be explicitly defined¹⁹, rendering for the Cauchy stress tensor σ the final expression:

$$\sigma = (1 - d^+) \bar{\sigma}^+ + (1 - d^-) \bar{\sigma}^- \quad (9.a)$$

with

$$0 \leq d^+ \leq 1 \quad \text{and} \quad 0 \leq d^- \leq 1 \quad (9.b)$$

where d^+ and d^- are the tensile and compressive damage variables, respectively. Thermodynamic considerations about the non-negativeness of the dissipation¹⁹ demand that $\dot{d}^+ \geq 0$ and $\dot{d}^- \geq 0$. The model is completed with appropriate evolution laws for these internal damage variables.

In order to clearly define concepts such as loading, unloading, or reloading, a scalar positive quantity, termed *equivalent stress*, will be defined. This enables to compare different tridimensional stress states. With such a definition, distinct tridimensional stress states can be mapped to a single *equivalent* unidimensional stress test, which makes possible

their quantitative comparison. As a consequence of the stress split, an equivalent effective tensile norm $\bar{\tau}^+$ and an equivalent effective compressive norm $\bar{\tau}^-$ will be used. In the present work they will assume the following forms:

$$\bar{\tau}^+ = \sqrt{\bar{\sigma}^+ : \mathbf{D}_0^{-1} : \bar{\sigma}^+} \quad (10.a)$$

$$\bar{\tau}^- = \sqrt{\sqrt{3} (K \bar{\sigma}_{oct}^- + \bar{\tau}_{oct}^-)} \quad (10.b)$$

In Eq. (10.b) K is a material property which depends on the ratio between the uniaxial and biaxial compressive strengths of the concrete¹⁹ (a typical value for concrete is $K = 0.17$); additionally, $\bar{\sigma}_{oct}^-$ and $\bar{\tau}_{oct}^-$ are, respectively, the octahedral normal stress and the octahedral shear stress, obtained from $\bar{\sigma}^-$.

With the above definitions for the effective equivalent norms, two separated damage criteria g^+ and g^- will be introduced⁴, the former for tension and the latter for compression:

$$g^+(\bar{\tau}^+, r^+) = \bar{\tau}^+ - r^+ \leq 0 \quad (11.a)$$

$$g^-(\bar{\tau}^-, r^-) = \bar{\tau}^- - r^- \leq 0 \quad (11.b)$$

Variables r^+ and r^- are current damage thresholds, in the sense that their values control the size of the expanding damage surfaces. For the initial stage, that is, when no loading has yet been applied, values r_0^+ and r_0^- , assumed material properties, are attributed to these thresholds. As it can be deduced from definitions (10.a) and (10.b), Eq. (11.a) corresponds to a damage bounding surface which is a sphere centered at the origin in the space of principal undamaged tensile stresses⁹, and Eq. (11.b) defines a Drucker-Prager cone for compression. Eq. (11.a) states that tensile damage tends to increase if $\bar{\tau}^+ = r^+$, and so it will be initiated when for the first time $\bar{\tau}^+ = r_0^+$ (a similar reasoning can be applied for compression). Figure 2 shows the initial damage bounding surface resulting from the combination of both criteria in a biaxial effective principal stress space. Note the good qualitative agreement with the documented experimental results for concrete.

With these definitions, and after enforcement of the consistency conditions for loading-unloading-reloading situations via the Kuhn-Tucker relations, the kinematics of the tensile and compressive internal variables are defined as:

$$\dot{r}^+ = \dot{\bar{\tau}}^+ \geq 0 \quad \dot{d}^+ = \dot{r}^+ \frac{\partial G^+(r^+)}{\partial r^+} = \dot{G}^+(r^+) \geq 0 \quad (12.a)$$

$$\dot{r}^- = \dot{\bar{\tau}}^- \geq 0 \quad \dot{d}^- = \dot{r}^- \frac{\partial G^-(r^-)}{\partial r^-} = \dot{G}^-(r^-) \geq 0 \quad (12.b)$$

with G^+ and G^- being appropriate monotonically increasing functions derived from experimental observation. The particular forms assumed by the rate Eqs. (12.a) and (12.b) allow to specify the following damage evolution laws, after performing a trivial integration (with the initial condition of null damages):

$$r^+ = \max(r_0^+, \bar{\tau}^+) \quad d^+ = G^+(r^+) \quad (13.a)$$

$$r^- = \max(r_0^-, \bar{\tau}^-) \quad d^- = G^-(r^-) \quad (13.b)$$

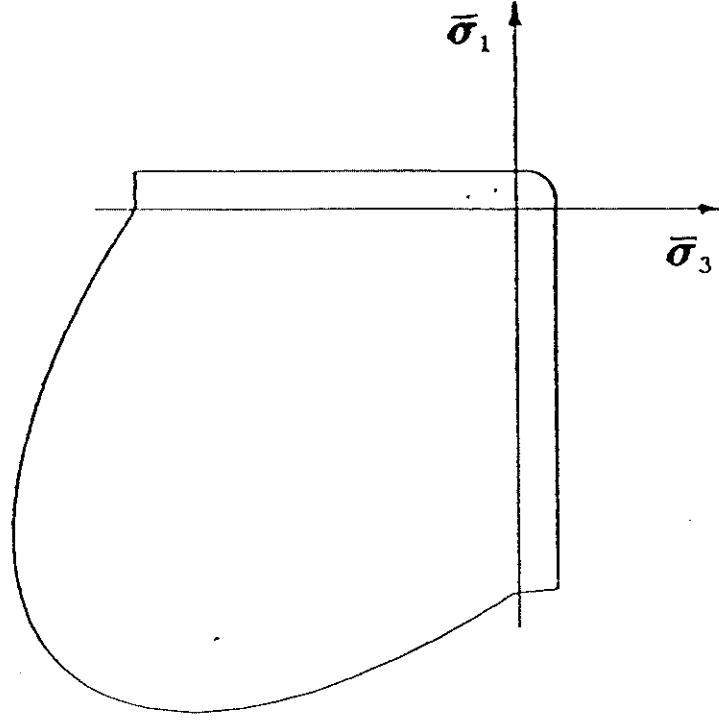


Figure 2. Initial damage bounding surface in a biaxial effective principal stress space

These equations put into evidence that the model is strain driven in a closed form: once the current strain tensor is known, damage variables can be easily evaluated, as they only depend on the equivalent norms $\bar{\tau}^+$ and $\bar{\tau}^-$, which are evaluated from ϵ . So, the selection for the particular forms of functions G^+ and G^- will determine the specific damage evolutions to be considered, and consequently some care must be devoted to this subject, so that a realistic representation of experimental behavior might be obtained. Anyway, the change from one particular set of evolution laws to a different one does not put any special problem, thus enabling this model to have substantial updating versatility.

For the present work, the following damage evolution rules will be adopted:

$$d^+ = 1 - \frac{r_0^+}{\bar{\tau}^+} e^{A^+ (1 - \frac{\bar{\tau}^+}{r_0^+})} \quad (14.a)$$

$$d^- = 1 - \frac{r_0^-}{\bar{\tau}^-} (1 - A^-) - A^- e^{B^- (1 - \frac{\bar{\tau}^-}{r_0^-})} \quad (14.b)$$

Eq. (14.a) is able to reproduce the softening branch of a concrete unidimensional tensile test, asymptotically to the strain axis. With this evolution law for d^+ , a finite area is retained between the stress-strain curve and the strain axis, which is crucial to appropriately define the fracture energy concept (as it is well known, of primary importance to satisfy requisits of mesh-objectivity when dealing with softening materials)⁹. Besides the tensile damage threshold r_0^+ (usually related to the uniaxial tensile peak strength), only the parameter A^+ exists, the determination of which is made by equating the material fracture

energy to the time integral of dissipation¹⁹. By means of Eq. (14.b) it is possible to reproduce the hardening effect on concrete submitted to compression, as well the softening which occurs after the compressive strength is attained⁸. Besides r_0^- , for its characterization two parameters (A^- , B^-) must be defined, usually by imposing that the evolution curve satisfies two selected points of a unidimensional experimental test¹⁹.

It must be remarked that the aim of this model is to be able to model properly the stiffness degradation of concrete both in tensile and compressive processes. Moreover, the introduction of independent internal damage variables for tension and compression allows for stiffness recovery (also known as unilateral effect) upon load reversal, a feature which the authors have found of *primary importance when conducting seismic analysis of structures*. Figure 3 shows the cyclic behaviour of the proposed continuum damage model in a uniaxial test.

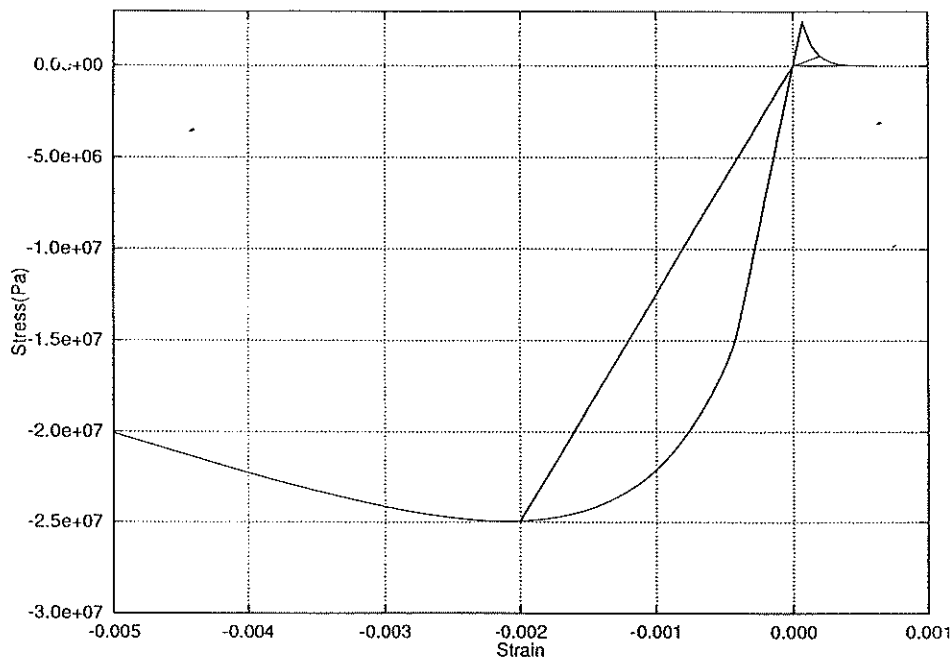


Figure 3. Cyclic behaviour of the continuum damage model in a uniaxial test

2.5 Constitutive model for soil

Soils behave non-linearly when excited by the strong earthquakes that are of interest to structural engineers. Among the different possibilities available in the literature for soil constitutive modelling, one of the alternatives is to use a similar constitutive model to that used for the structure, that is, a continuum damage model with appropriate parameters. However, when determining the input seismic excitation starting from the motion of one free-field surface control point, the principle of superposition is frequently invoked. This means that a linear soil system is actually assumed. The simplification of using a linear soil medium should be considered in connection with the actual way of determining and specifying the seismic input.

3. FLUID COMPUTATIONAL MODEL

3.1 Dynamic governing equation

The governing equation for acoustic waves for an inviscid, compressible fluid with small amplitudes for the displacements and velocities is the well-known Helmholtz equation:

$$\nabla^2 P - \frac{1}{c^2} \ddot{P} = 0 \quad (15)$$

where P is the pressure and c is the acoustic speed in the fluid. After the standard process of discretization in space¹⁵ the semidiscrete governing equation can be written as

$$\mathbf{M}_f \ddot{\mathbf{p}} + \mathbf{K}_f \mathbf{p} = \mathbf{f}_f \quad (16)$$

where subscript f refers to the fluid. The ‘mass’ matrix is \mathbf{M}_f , \mathbf{K}_f is the matrix arising from the discretization of the (linear) Laplace operator, \mathbf{f}_f is the vector of ‘force’, and $\mathbf{p} = \mathbf{p}(t)$ is the vector of nodal pressures in the fluid. Note that only natural boundary conditions have been considered and that no viscous damping term is present in Eq. (16). Note also that this is a second order equation in time, and so it can be integrated step-by-step in an analogous manner to Eq. (1).

3.2 Boundary conditions

In the fluid domain (water in the reservoir) there are three types of ‘especial’ boundaries to be considered in the fluid–structure problem (see Fig. 1):

- (a) Solid–fluid interaction boundary (Γ_{fs}): in the fluid–structure problem the normal velocities in the fluid (or their time derivatives) are prescribed to be equal to those in the solid. It can be shown¹⁵ that this condition leads to a prescription on the derivative of the pressure normal to the interface:

$$\nabla P \cdot \mathbf{n} = \rho_f \ddot{\mathbf{u}} \cdot \mathbf{n} \quad (17)$$

where \mathbf{n} is a unit vector normal to the interface (pointing inwards to the fluid), ρ_f is the fluid density and $\ddot{\mathbf{u}}$ is the acceleration. After discretization, this condition appears as a term of nodal forces on the fluid due to the accelerations in the solid that can be computed as,

$$\mathbf{f}_{fs} = \rho_f \int_{\Gamma_{fs}} \mathbf{N}_f^T (\mathbf{n} \cdot \ddot{\mathbf{u}}) d\Gamma = \rho_f \int_{\Gamma_{fs}} \mathbf{N}_f^T \mathbf{n}^T \mathbf{N}_s \ddot{\mathbf{a}} d\Gamma = \rho_f \mathbf{Q}^T \ddot{\mathbf{a}} \quad (18)$$

Note that the coupling matrix \mathbf{Q} is the same as in Eq. (2).

- (b) Radiating or ‘transparent’ boundary (Γ_{fr}): For the fluid domain it is also possible to derive a fictitious boundary that will damp completely the pressure waves that reach it, in a way similar to the one described for the solid, and under the same

assumptions^{12,14,15}. It can be shown that this condition leads to a prescription on the derivative of the pressure normal to the interface of the form:

$$\nabla P \cdot \mathbf{n} = -\frac{1}{c}\dot{P} \quad (19)$$

where \dot{P} is the time derivative of the pressure. This boundary provides tractions which are proportional to the velocities in the fluid, and therefore, its effects after the spatial discretization process will be a contribution to the damping matrix of the system that can be written as,

$$\mathbf{C}_{fr} = \frac{1}{c} \int_{\Gamma_{fr}} \mathbf{N}_f^T \mathbf{N}_f d\Gamma \quad (20)$$

For some applications it would be handy to have a ‘transparent’ boundary for the fluid with in-coming seismic wave (Γ_{fi}). This is easy to derive based on the boundary just described. The only difference is an added ‘force’ term which depends on the prescribed seismic velocities $\dot{\mathbf{v}}$, and which reads:

$$\mathbf{f}_{fi} = \frac{2}{c} \int_{\Gamma_{fi}} \mathbf{N}_f^T \dot{\mathbf{v}} d\Gamma \quad (21)$$

- (c) Free surface boundary (Γ_{ff}): On the free surface of the fluid the simplest assumption is that

$$P = 0 \quad (22)$$

and this can be imposed as a ‘forced’ condition at equation solution level. If the possibility of having surface gravity waves is considered, this can be substituted by the *linearized surface wave condition*¹⁵, which results in an addition to the ‘mass’ matrix of the form

$$\mathbf{M}_{ff} = \frac{1}{g} \int_{\Gamma_{ff}} \mathbf{N}_f^T \mathbf{N}_f d\Gamma \quad (23)$$

where g is the gravity acceleration.

4. FLUID-STRUCTURE INTERACTION

4.1 Governing equations and direct solution

Doubtless, fluid-structure interaction is one of the best known coupled problems in engineering. In this case, the coupling occurs at the interface between two different domains, occupied one by the solid and the other by the fluid. Neither the structure nor the fluid

can be solved independently of each other, since the motion of the structure depends on the pressures of the fluid at the interface, and the fluid pressures depend in turn on the normal acceleration of the wet wall of the solid. The equations considered here are the conservation of momentum for the solid (see Section 2) and the Helmholtz equation for the fluid (see Section 3), both equations being coupled through the corresponding (moving) interface boundary terms. The constitutive relationship adopted for the structure is the nonlinear isotropic continuum damage model described in Section 2, whereas a linear elastic model is assumed for the foundation.

The semidiscrete problem arising from the standard Galerkin spatial discretization reads as follows:

$$\begin{aligned} \mathbf{M}_s \ddot{\mathbf{a}} + \mathbf{C}_s \dot{\mathbf{a}} + \mathbf{S}(\mathbf{a}) &= \mathbf{f}_s - \mathbf{Q}\mathbf{p} \\ \mathbf{M}_f \ddot{\mathbf{p}} + \mathbf{C}_f \dot{\mathbf{p}} + \mathbf{K}_f \mathbf{p} &= \mathbf{f}_f + \rho_f \mathbf{Q}^T \ddot{\mathbf{a}} \end{aligned} \quad (24)$$

where subscripts s and f refer to the solid and the fluid, respectively, and the coupling forces have been explicitly written. Remember that the coupling matrix \mathbf{Q} only has non zero terms for the nodes located on the wet wall. Observe that in Eq. (24) the coupling is *linear* and the only non-linearity of the problem comes from the constitutive model for the solid (the dam). Therefore, after using a suitable time discretization (the Newmark scheme, for example) one will be led to a non-linear algebraic system of the form:

$$\begin{bmatrix} \mathbf{A}_{ss}(\mathbf{a}) & \mathbf{A}_{sf} \\ \mathbf{A}_{fs} & \mathbf{A}_{ff} \end{bmatrix} \begin{bmatrix} \mathbf{a} \\ \mathbf{p} \end{bmatrix} = \begin{bmatrix} \bar{\mathbf{f}}_s \\ \bar{\mathbf{f}}_f \end{bmatrix} \quad (25)$$

This system of equations can be easily symmetrized by scaling properly the equation for the fluid pressure, and the coupled problem can be *directly* solved, in a step-by-step fashion, by forming and solving Eq. (24) step after step. Iterations would be needed within each step due to the non-linearity of the term $\mathbf{A}_{ss}(\mathbf{a})$. One disadvantage of this strategy is that the structure of the global matrix of the system is such that entries come from the two different domains (solid and fluid), and so, integrals have to be evaluated in two different domains, and they represent physically different magnitudes. Another disadvantage is the larger size of the global matrix as compared with the ones arising from the different domains. On the other hand, the advantage is that the final algorithm is easily and clearly defined, and its analysis, regarding for instance stability, is feasible (although complicated).

4.1 Block-iterative solution

Let us consider now the use of block-iterative algorithms to solve problem (24). This will reduce the size of the resulting subproblems at the expense of iterating. Assuming that the first equation in (24) is solved first, there are two possible block-iterative schemes, namely,

$$\begin{aligned} \mathbf{A}_{ss}(\mathbf{a}^{(i)})\mathbf{a}^{(i)} &= \bar{\mathbf{f}}_s - \mathbf{A}_{sf}\mathbf{p}^{(i-1)} \\ \mathbf{A}_{ff}\mathbf{p}^{(i)} &= \bar{\mathbf{f}}_f - \mathbf{A}_{fs}\mathbf{a}^{(k)}, \quad k = i-1 \text{ or } i \end{aligned} \quad (26)$$

Here, superscripts in parenthesis refer to iteration counters. For $k = i-1$ this is the *block-Jacobi* (or *block-total-step*) method, whereas for $k = i$ it is the *block-Gauss-Seidel*

(or *block-single-step*) method. From elementary numerical analysis it is known that, under certain conditions, both the Jacobi and the Gauss-Seidel methods converge linearly when applied to linear systems, the convergence rate of the latter being twice higher than that of the former. In their *block* counterparts these properties are inherited, the convergence rate depending now on the spectral radius of the matrices involved.

On the other hand, problem (25) (and also problem (26)) is non-linear, so that an iterative procedure must be used to deal with this non-linearity. Both the Picard (or fixed point) and the Newton-Raphson methods are suitable candidates to perform the necessary linearization. Either the non-linearity or the coupling could be dealt with in two nested iterative loops. However, there is the strong temptation to use a single iterative loop to deal both with the non-linearity and the coupling^{10,11,13}. This would lead (for the Picard method) to:

$$\mathbf{A}_{ss}(\mathbf{a}^{(i-1)})\mathbf{a}^{(i)} = \bar{\mathbf{f}}_s - \mathbf{A}_{sf}\mathbf{p}^{(i-1)} \quad (27)$$

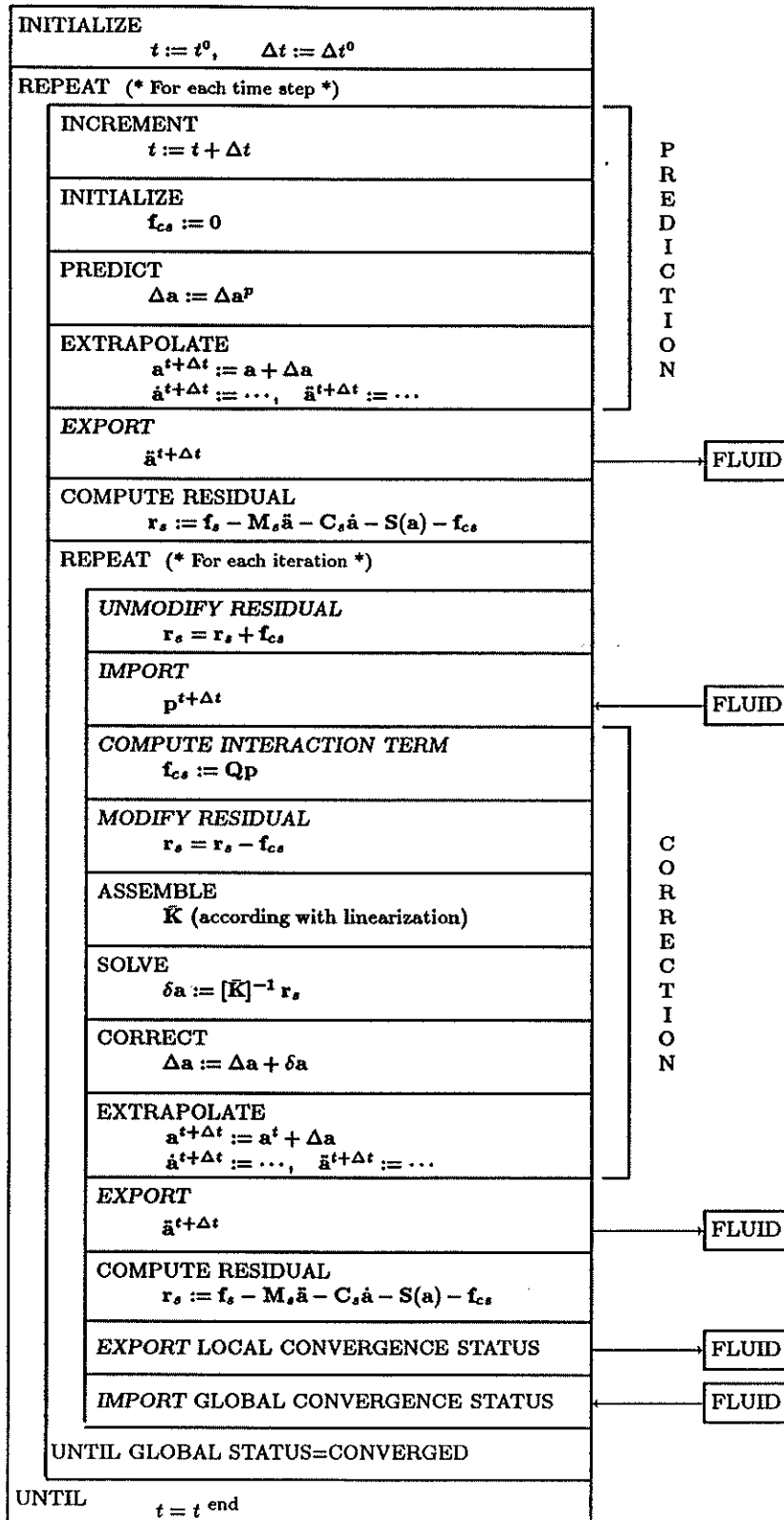
$$\mathbf{A}_{ff}\mathbf{p}^{(i)} = \bar{\mathbf{f}}_f - \mathbf{A}_{fs}\mathbf{a}^{(k)}, \quad k = i - 1 \text{ or } i \quad (28)$$

Perhaps the simplest choice to implement is: once $\mathbf{a}^{(i)}$ is known by solving Eq. (27), it is used to evaluate the right-hand side (RHS) of Eq. (28), and then this can be solved.

Box 1 presents the computational algorithm one of these block-iterative techniques applied to the solid phase of the fluid-structure interaction problem. Note that here an implicit predictor-multicorrector scheme^{11,17} has been assumed for the solution of the non-linear transient problem, without loss of generality. Obviously, the computational algorithm for the fluid phase could follow an identical or similar procedure. The squares labelled “FLUID” refer to the necessary inter-communication to interchange data between the solid and the fluid phases in the problem. Note also the *modify/unmodify* steps introduced for the evaluation of the residual force vector, which save unnecessary re-evaluations of the internal forces $\mathbf{S}(\mathbf{a})$ every time that the coupling term is recalculated.

The advantage is now that the structure of the matrices in the left-hand side, \mathbf{A}_{ss} and \mathbf{A}_{ff} , is such that entries come only from the single field currently considered, and so, integrals have to be evaluated only in that domain, and they represent physically homogeneous magnitudes. Moreover, for many practical applications these matrices are symmetric. There is no difficulty in evaluating the coupling terms appearing in the RHS of Eqs. (27) and (28), as they only involve integrals over the ‘interaction boundary’, and this is “seen” from both domains. Finally, note that the *two* systems of equations to be solved are smaller in size and with reduced band-width, as well as better conditioned, as compared to that yielding from the direct solution of Eq. (25). On the other hand, the disadvantage of the block-iterative solution of Eq. (24), is that iterations will be needed *even if the problem is linear* (note the need to check global or overall convergence in Box 1). *This is not especially inconvenient if the problem is non-linear, as equilibrium iterations would be required anyway, or if the coupling effect is not too strong.*

As the time dimension is involved, the analysis of any proposed solution strategy must consider the time integration stability of the approach. It may happen that, even if an unconditionally stable algorithm has been used for every one of the fields, the overall algorithm may still be conditionally stable^{10,15}. In practice, as the size of the chosen time step will always be limited by accuracy considerations, this may not be a serious



Box 1. Computational algorithm for block-iterative technique applied to the solid phase of the fluid-structure interaction problem.

drawback. Regarding the stability analysis of the block-iterative solution, it is certainly complicated and very problem dependent. Stabilization methods have been proposed to ensure unconditional stability of the block-iterative solution for specific problems under certain circumstances^{15,21,22}, but they require matrix operations that destroy the modularity (and so, the main motivation) of this approach.

An important point to remark regarding stability of this iterative technique is that time integration stability will also depend on the tolerance demanded to achieve overall convergence. If the solution of problem (26) is iterated until *full* overall convergence is achieved, then the stability characteristics of the approach are identical to those of the direct solution (problem (25)). However, as this is impossible or impractical to manage in real computations, a new source of instability will come from the tolerance specified by the user. As a limit case, if no check on the overall convergence is made, the approach becomes block-explicit (also known as “*staggered*” methods), and it will be obviously conditionally stable, or, in some unfortunate cases, unconditionally unstable^{10,12,23}. Sensibility to this factor is again very problem dependent. No difficulty was found by the authors in the numerical examples run for fluid-structure interaction even if slack tolerances were used.

The main conclusion from the authors’ experience in solving this and other coupled problems is that dealing with the non-linearity and the coupling within a single iterative loop is very effective. Roughly speaking, the number of iterations due to the nonlinearity and the coupling *do not* add up. Even with weak nonlinearities, these are who govern the global process, so that the coupling is achieved automatically, and unexpensively¹³. For a more detailed discussion of the efficiency of the block-iterative techniques applied to coupled problems, as well as some clues to their implementation, see reference 24.

5. SEISMIC EVALUATION OF CONCRETE GRAVITY DAMS

When dealing with a large structure it is important to be able to quantify somehow a ‘factor of safety’ to measure the safety of the structure against the possibility of failure. This is not a simple concept to apply in cases of complex non-linear structural behaviour, as present, for instance, in the seismic analysis of dams. The difficulties associated to this and similar definitions have been clearly stated by Fanelli²⁶: “... *the currently accepted quantitative definitions of the ‘factor of safety’ of a dam are rather fuzzy concepts, open to criticism from a rational viewpoint... In each instant of a dam’s life, there will be a definite relationship between the ‘load’ acting on it and the ‘ultimate load’ of the same type that the dam is able to withstand (this concept of ‘ultimate load’ requires that the path to ‘failure’ and the very concept of ‘failure’, be defined in an unambiguous way, which is by no means a trivial operation). ... [The factor of safety] is a continuously changing function of time, as load vary and the dam ages; its instantaneous physical values cannot be computed in a realistic way, because we lack complete information on loads and material properties and distribution. Besides, these values are also bound to vary considerably according to the different definitions of the ‘path to failure’ for any given situation. ... So, we are forced to conclude that there is not, in any given instant, a unique value of the safety factor, but rather and indefinite number of them, and that all those safety factors are also continuously varying in time*”.

Additionally, there are situations in which the occurrence of a certain degree of 'local failure' is unavoidable. Such is the case of a concrete dam subjected to severe seismic excitation, where stress reversals will almost certainly produce damage in certain areas of the dam. This will not, in general, lead to the (global) collapse of the structure. In some rare cases, the non-linear behaviour of the material and the change of stiffness associated to partial damage may even help the structure to withstand the earthquake without reaching a state of 'failure'.

Nevertheless, the concept of safety (or unsafety) of a structure is intuitively linked to the 'damage' that it suffers when subjected to a particular external action. The 'ultimate load' that a structure is able to withstand is associated to a high level of damage, while a load producing little or no damage is far from leading to structural collapse. Keeping in mind that there may exist mechanisms of global collapse not associated to damage (elastic instability, brittle fracture, etc.) the present work intends to study the intuitive relation between damage and safety.

5.1 The concept of global damage

The damage or degradation variables d^+ and d^- defined in Section 2 are a measure of the loss of secant stiffness of the material at a point and at a given time. Therefore, these variables are understood as a measure of the 'local damage' inside a structure, and as such it provides very useful information to the analyst. The purpose of this section is to introduce a 'global damage index' D^+ (and D^-) whose value gives an indication of the state of the structure, as a whole, at a given time.

Some important aspects must be considered for the definition of such a global damage index: (i) The global damage index must be the same for two identical structures with the same distribution of local damage, regardless of the instant of time or the type of loading. Therefore, the global index must be computed uniquely in terms of the values of the local damage variable, defined at each point inside the dam, and its distribution; (ii) As the local variable d^t , the global index D^t must be a non-dimensional scalar value, ranging between 0, for an undamaged structure, to 1, for a fully degraded structure; (iii) The structure is undamaged ($D^t = 0$) if and only if no local damage has occurred ($d^t = 0$ for all points); similarly, the structure is fully degraded ($D^t = 1$) if and only if all the point are fully damaged ($d^t = 1$ for all points); (iv) If a structure with a certain degree of damage is subjected to an external action, the global damage index can only increase or remain unchanged.

Thus, we will define the *global damage index* for a structure, at a given time t , as a scalar variable D^t verifying the following conditions:

- (i) $D^t = D^t(d^t)$
- (ii) $0 \leq D^t \leq 1$
- (iii) $D^t = 0 \iff d^t = 0$ for all points
 $D^t = 1 \iff d^t = 1$ for all points
- (iv) $D^{t_1} \leq D^{t_2} \iff t_1 \leq t_2$

Among the many possibilities for the definition of the ‘global damage index’ we propose the following two:

$$D_1^t = \frac{\int_{\Omega} d^t d\Omega}{\int_{\Omega} d\Omega} \quad (29.a)$$

$$D_2^t = \frac{\sqrt{\int_{\Omega} (d^t)^2 d\Omega}}{\sqrt{\int_{\Omega} d\Omega}} \quad (29.b)$$

where d^t is the local damage variable. Note that both definitions verify the necessary conditions.

The first proposed alternative D_1^t is the average value of the local damage over the nonlinear part of the structure and it is the simplest measure of global damage that can be devised. However, this value does not consider at all the distribution of damage over the structure. In particular, it is not sensitive to the existence of relatively small areas with relatively high values of damage, a circumstance that can very well affect significantly the overall behaviour of the dam. On the other hand, the second proposal D_2^t gives a greater weight to the higher values of local damage, and thus it takes somehow into account the localization effect. For the same value of the average damage D_1^t , the index D_2^t will be greater depending on the degree of localization of the damage variable. That is why it has some interest the consideration of both indexes when comparing different distributions of local damage for the same structure subjected to different seismic excitations.

5.2 Definition of the structural collapse

When attempting to perform the safety assessment of a concrete dam against seismic actions it is important to define a situation of structural collapse. Ideally, this definition should be unambiguous and independent of the computational model used to analyze the structural behaviour. Furthermore, the safety assessment must answer to (at least) three quite different questions: firstly, does the dam collapse *while* subjected to an earthquake of a given intensity and with a given response spectrum?; secondly, if this is not the case, which is the state of the dam *after* the seismic excitation?; and thirdly, how has the factor of safety of the dam against, for instance, the hydrostatic pressure been affected by the action of the earthquake?.

In this work we will distinguish between:

- *Dynamic collapse during the earthquake*, in any of the three following related situations: (a) when the computed displacements at selected points reach unacceptable values or grow unbounded, or (b) when the state of damage is either widely spread or highly localized, or (c) when the non-linear dynamic response departs greatly from the one obtained in a linear analysis.
- *Static collapse after the earthquake*, when the dam is able to withstand the seismic excitation but a *quasi-static analysis* performed *a posteriori* shows that the factor of safety against the action of the hydrostatic pressure has been greatly reduced due to the state of degradation induced by the earthquake.

It is clear that these definitions are not totally objective, and more effort should be put into their quantitative assessment, particularly for the dynamic collapse. Also, they are linked somehow to the computational model used in the analysis (a damage model in this case). However, they address questions of engineering interest and could be 'easily' re-interpreted for other material models, such as plasticity or smeared crack models or fracture mechanics.

6. SEISMIC ANALYSIS OF A GRAVITY DAM

The computational model described in the previous sections is now applied to the analysis of a concrete gravity dam. The geometry of the problem is depicted in Figure 1. The dam selected resembles very closely Koyna Dam in India (107 m high) that has been studied by many researchers interested in seismic analysis. The water level in the reservoir is 100 m. The natural damping is tuned to provide a damping ratio of 5 % for the first and second modes of the dam-soil system (Rayleigh parameters $a = 0.8 \text{ s}^{-1}$, $b = 0.003 \text{ s}$).

With the objective of analysing the response of this large concrete dam subjected to seismic actions of different intensities an artificial velocigram has been generated¹². The design spectrum and the response spectrum of the generated accelerogram are compared in Figure 4, which shows the good agreement obtained. The generated velocigram has a total duration of 10 seconds, with a peak ground acceleration of $0.255g$ and maximum ground velocities around 0.25 m/s (occurring about $t = 3.7 \text{ s}$). The dominant period of the signal is 0.4 s , which is very close to the first fundamental period of the dam-soil system ($T_1 = 0.4355 \text{ s}$). This input velocigram is shown in Figure 5 compared with the velocity computed at the free-field of the computational domain. Note that, apart for the shift due to the time that the signal takes to travel through the soil domain, the agreement between both of them is good. This shows that the boundary conditions are properly represented in the computational model.

Three seismic analyses are performed by scaling the input velocigram to achieve peak ground accelerations of $0.255g$, $0.383g$ and $0.510g$, respectively. The corresponding signals are applied as an horizontal seismic excitation along the canyon direction. Figure 6 shows the computed horizontal displacements (relative to the ground) for the three signals. Non-linear effects are present for the smallest intensity, and grow significantly for the other two (stronger) signals. This is also evident in Figure 7, which depicts the evolution with time of the global (tension) damage index D_2^t (no compression damage occurred during any of the analyses). Note that the evolution of damage is mostly concentrated in a few intervals of time where the maximum positive and negative displacements occur (close to $t = 1.6 \text{ s}$. and $t = 4.0 \text{ s}$). This is again shown in Figures 8 and 9, which show the distribution of damage and the deformed shape of the dam at selected times for the lowest and medium intensities, respectively. Note how for $0.255g$ damage does not bridge across the 'neck' of the dam, whereas this does occur for $0.383g$. However, as the up-stream and down-stream faces are not under tensile stress at the same time, the dam retains its overall stability. Regarding the evolution of the hydrodynamic pressure acting on the up-stream wall (not shown), it must be said that the graphs follow closely those of the (relative) horizontal displacement. Negative pressures are only encountered in the upper tenth of the dam, for

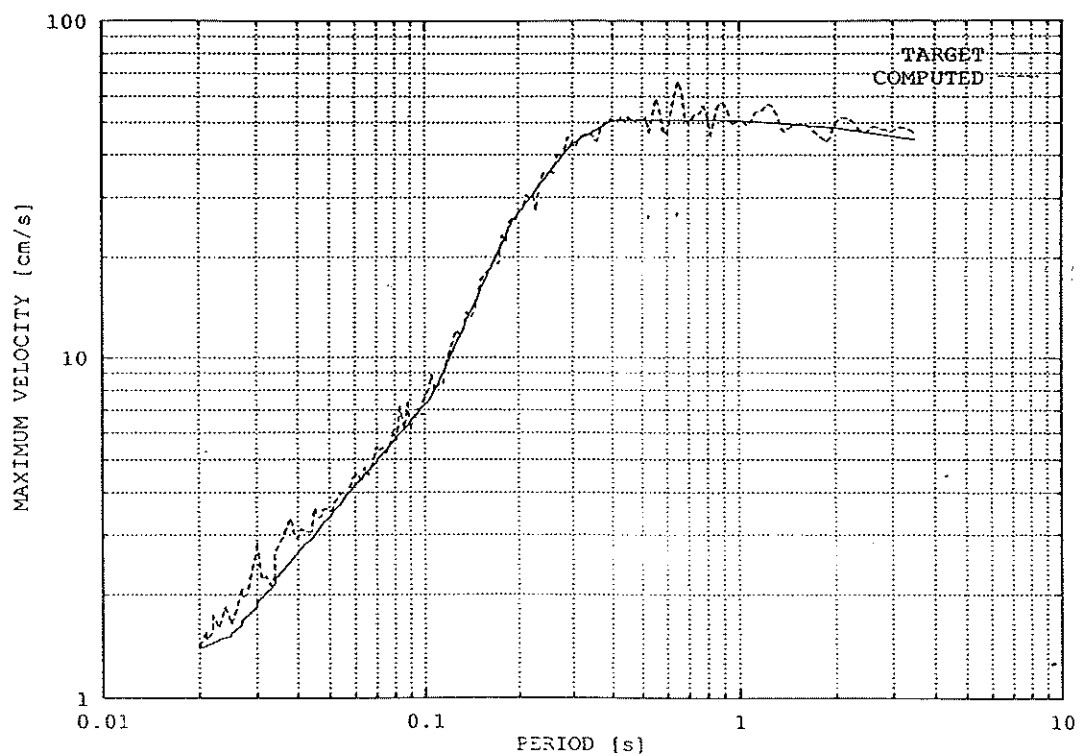


Figure 4. Comparison between the design and the computed velocity spectrum

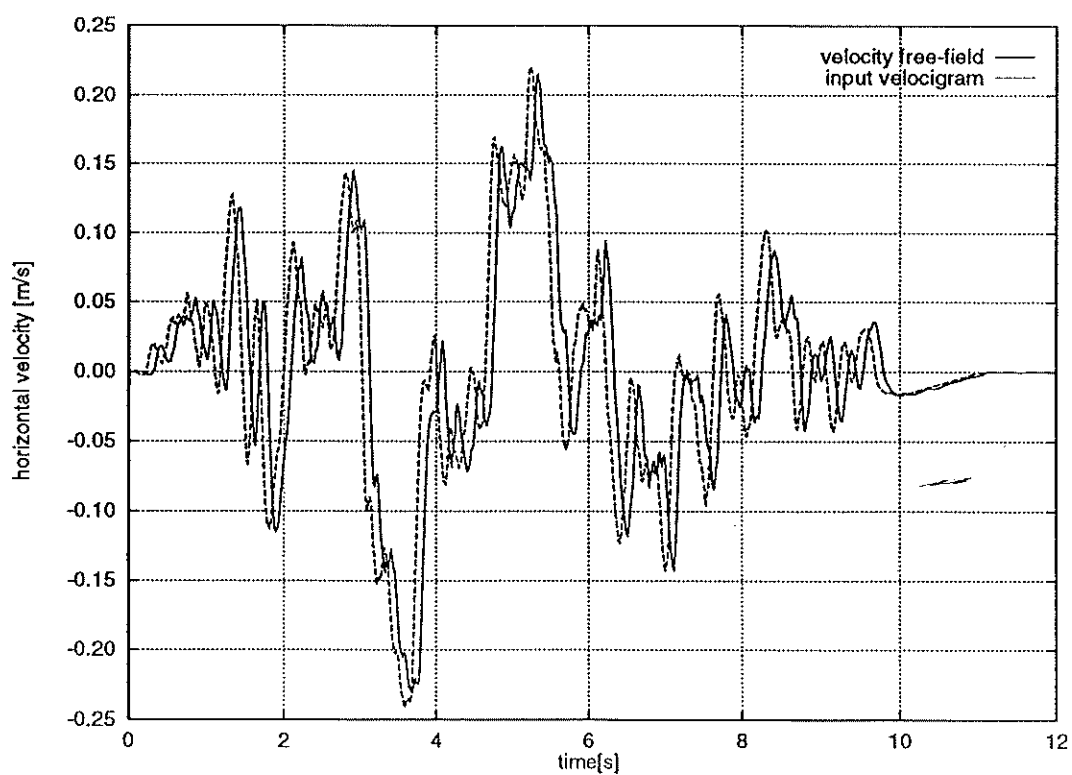


Figure 5. Comparison between the input velocigram and the computed velocity at the free-field

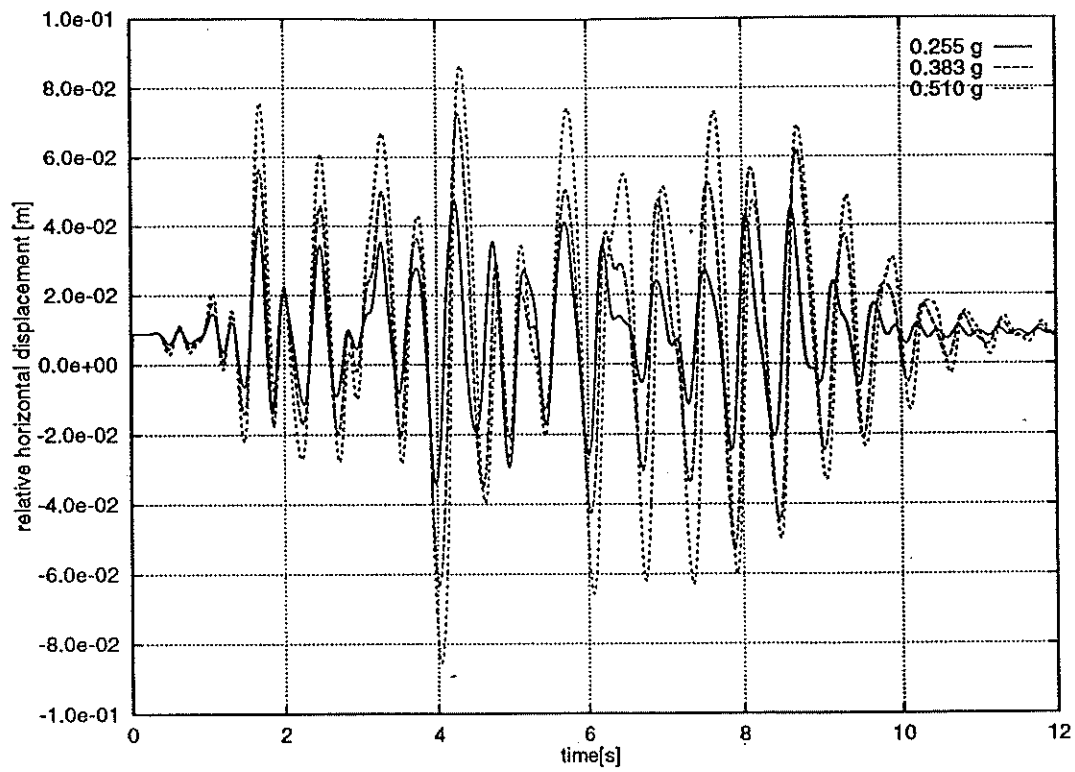


Figure 6. Koyna Dam. Horizontal (relative) displacement at the top of the dam for different seismic intensities

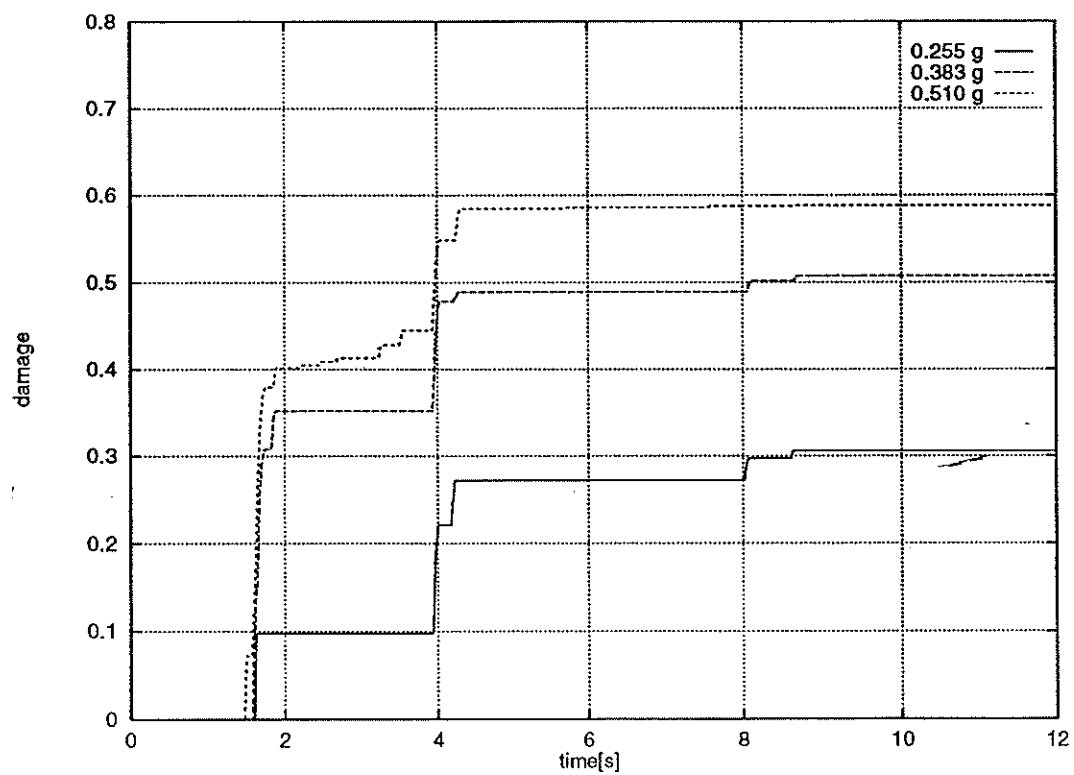


Figure 7. Koyna Dam. Evolution of the global (mean square value) tensile damage index for different seismic intensities

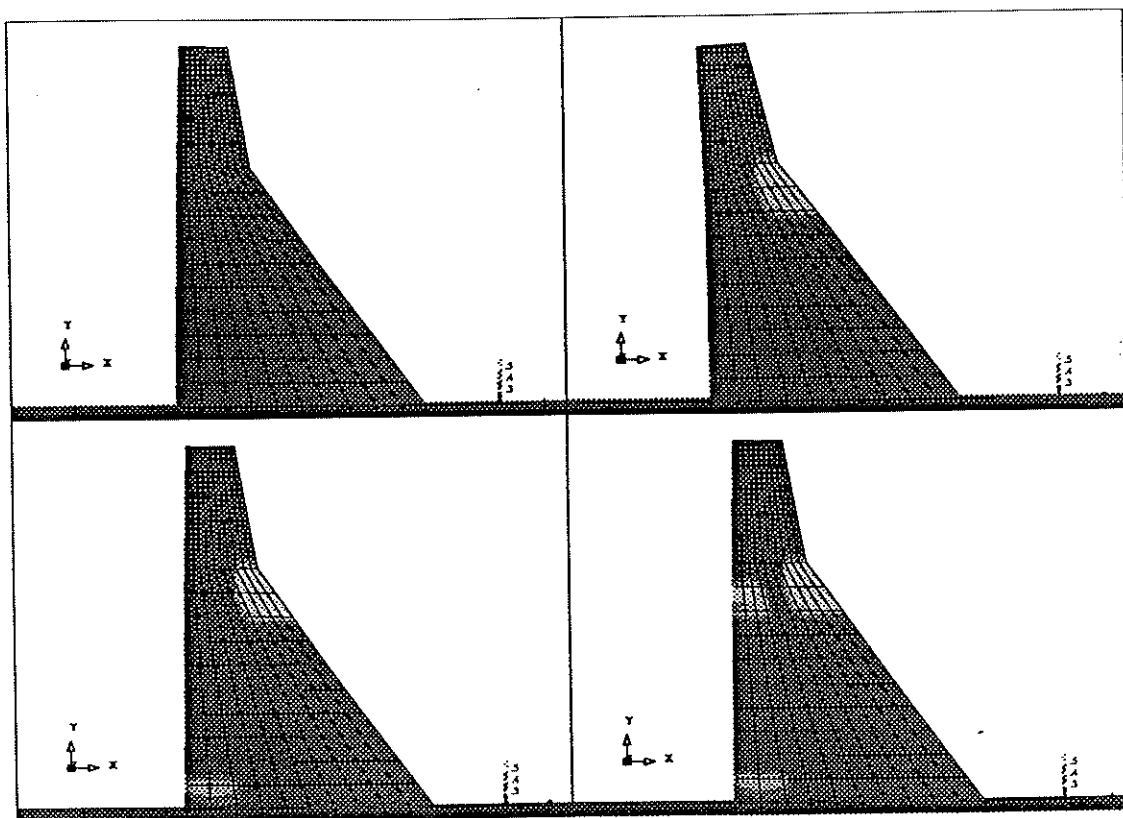


Figure 8. Koyna Dam. Evolution of the tensile damage and deformed shapes for the 0.255g signal

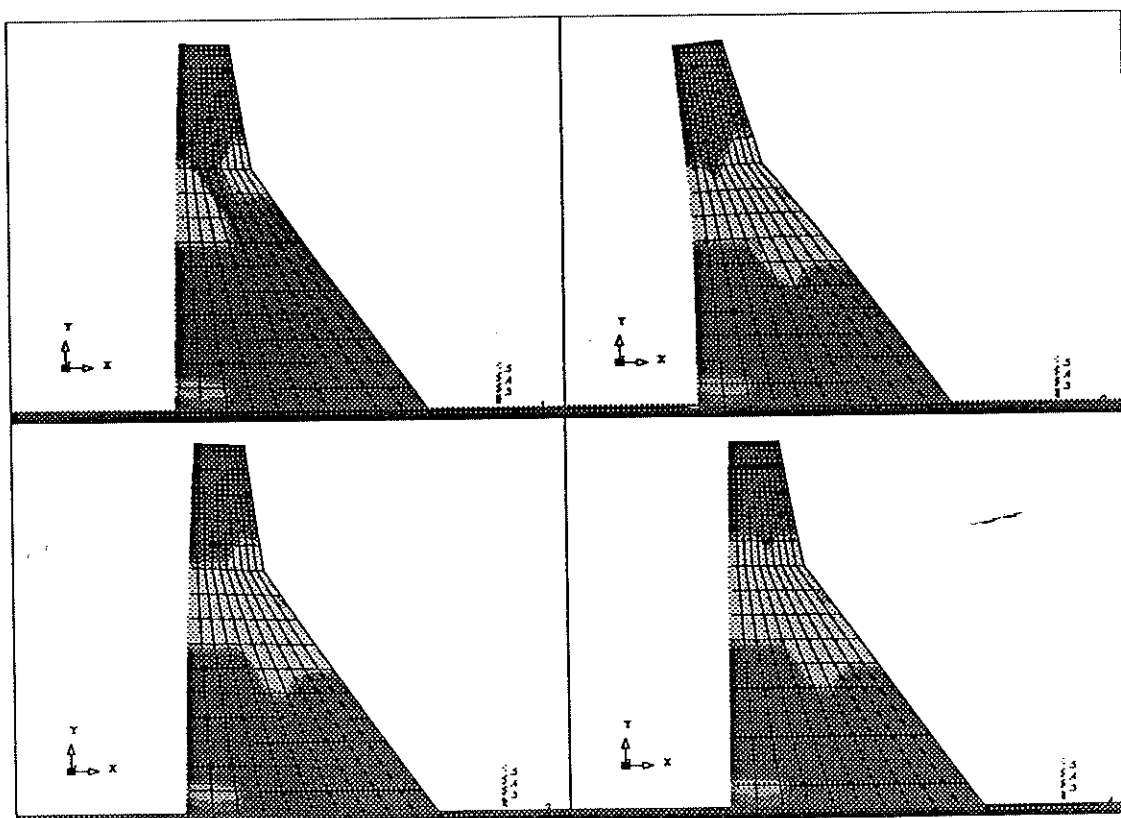


Figure 9. Koyna Dam. Evolution of the tensile damage and deformed shapes for the 0.383g signal

the highest intensity and only for $t = 4.0$ s. Thus, it seems that the assumption of linear behaviour for the fluid is valid for this particular case.

About the assessment of seismic safety the results of the analyses are open to discussion. It can be said that the dam is severely damaged by the earthquake with a peak acceleration of $0.255g$, and more importantly for the stronger signals. Therefore, the collapse intensity for a signal with this particular frequency content could be placed around $0.250g$. However, it must be remarked that in all the analyses the dam retains its structural integrity. Furthermore, the *a posteriori* quasi-static analyses with increasing hydrostatic pressure produce a safety factor of 2.28 for all cases, with an identical collapse mechanism of over-turning. This can be explained considering that a gravity dam resists the hydrostatic pressure due to its self-weight, and for this load it is subjected to a triaxial state of compression everywhere. Clearly, this structural mechanism is not affected at all by the tensile damage induced by the earthquake.

7. SEISMIC ANALYSIS OF AN ARCH DAM

The computational model described in the previous sections is now applied to a the seismic analysis of an arch dam, which constitutes a 3D nonlinear coupled problem. To this end we have selected Talvacchia Dam, in Italy, a 75 meters high double curvature dam which has been studied previously by several researchers. The finite element meshes used for the reservoir water and the dam-soil domain are shown in Figure 10. It must be remarked that although the Figure shows both meshes together, the analysis has been performed separately for each of the domains, following the scheme presented in Section 3. Damping elements are appropriately situated at the bottom and lateral boundaries to prevent the out-going waves from artificially reflecting on them. The model is subjected to a horizontal earthquake in the longitudinal direction of the river (symmetric excitation), propagating vertically from the base of the model.

Figure 11 shows the amplified deformed shape of the dam (amplification factor equal to 500) for two given times (top and bottom) of the analysis correspondent to the earthquake with a peak acceleration of $0.364g$. The Figure shows only half of the model (the water is not shown for clarity) from the front (left) and from the rear (right), with the corresponding tensile iso-damage contours. As expected, due to the symmetry of the model and the excitation, the higher values of the damage appear at the top of the central cantilever. Lower values of damage appear at the dam-foundation interface in the down-stream wall. Figure 12 shows the horizontal displacement at the top of the central cantilever for different intensity factors of the excitation. It can be seen that the response for a peak acceleration of $0.312g$ is only mildly nonlinear, while for $0.364g$, and specially for $0.416g$, the nonlinear effects are evident. Figure 13 shows the evolution of the global (mean square value) damage with time for these three intensities. It can be seen that most of the damage develop during the first two seconds of the excitation, where the peak accelerations of the ground occur. Note that, nevertheless, important displacements occur later without changing significantly the level of damage.

Regarding the computational cost of the analysis it must be said that the additional cost due to the fluid interaction is very small (about 4% of the total CPU time), because

of the formulation used (a single degree of freedom per node). Unfortunately, most of the computer time is spent by the foundation; therefore, and always supposing that linear behaviour is a valid assumption, alternative techniques, such as the boundary element method, may be used. In this work, we have used reduced integration with an hourglass-control technique to keep the computational cost within reasonable limits.

8. CONCLUSIONS

The paper presents a general methodology for the evaluation of large dams subjected to seismic actions with two main objectives: *generality*, as it is valid both for gravity and arch dams and it includes most of the relevant features present in the problem, and *efficiency*, as it allows for the use of modular and computationally efficient software. Four different conclusions can be drawn from this work: (a) The non-linear behaviour of the dam may be appropriately represented via an isotropic continuum damage model with separated internal variables for degradation under tension and compression stress states. Moreover, this option allows for stiffness recovery (also known as unilateral effect) upon load reversal, a feature of primary importance for seismic analysis of structures. Also, the model is particularly suitable for large scale problems due to its explicit format. (b) The treatment of the boundary conditions for the dynamic transient problem is fully stated both for the solid and the fluid phases in the computational model. The introduction of radiating or 'transparent' boundaries, and the imposition of the in-coming seismic wave as an appropriate force term seem an adequate option from the analytical and computational standpoints. (c) The partitioned block-iterative solution of the fluid-structure interaction problem is formulated and tested for real application analyses. It is found that both the non-linearity and the coupling can be treated most efficiently within a single iterative loop, without loss of generality. No stability difficulties are found for real case data and the overhead to be paid due to the coupled analysis of the fluid is almost negligible. (d) Finally, some qualitative criteria for the definition of structural collapse and the seismic assessment of concrete dams are presented. The topic is open for discussion and future work must be primarily directed in this direction. To conclude, the application of the proposed methodology to the seismic analysis of two real dams of different topologies shows that it can be used as a valid tool for earthquake engineering and structural analysis.

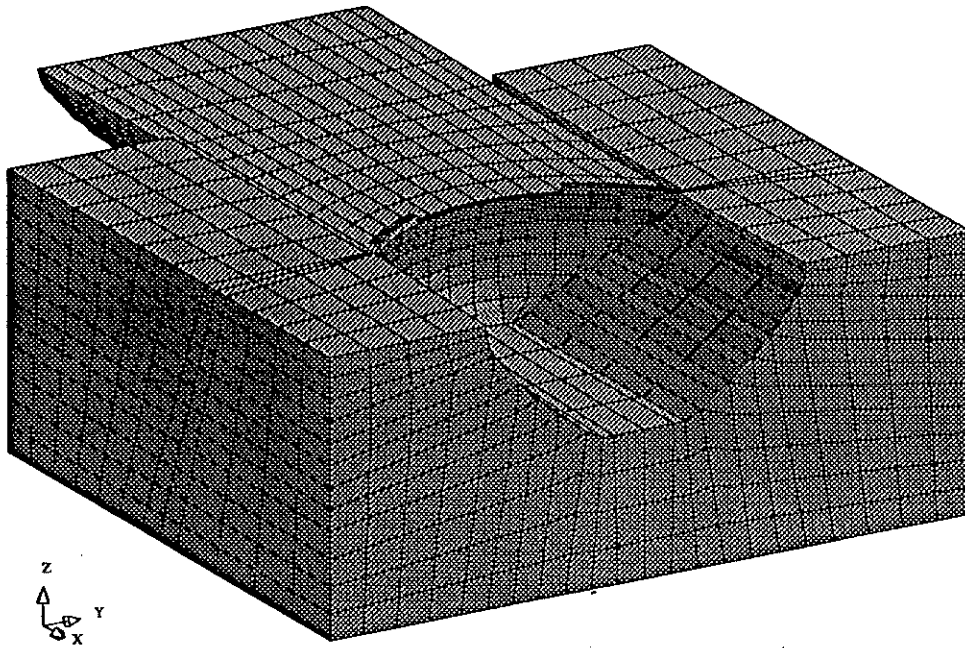


Figure 10. Talvacchia Dam. Computational model

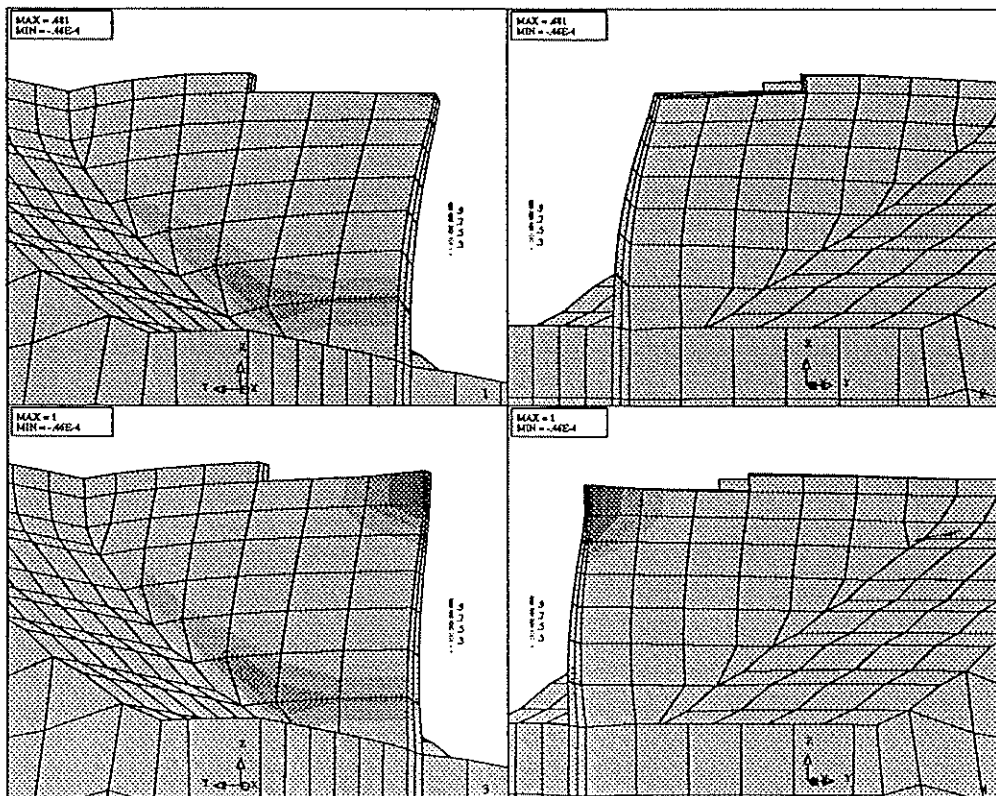


Figure 11. Talvacchia Dam. Deformed mesh with iso-damage contours

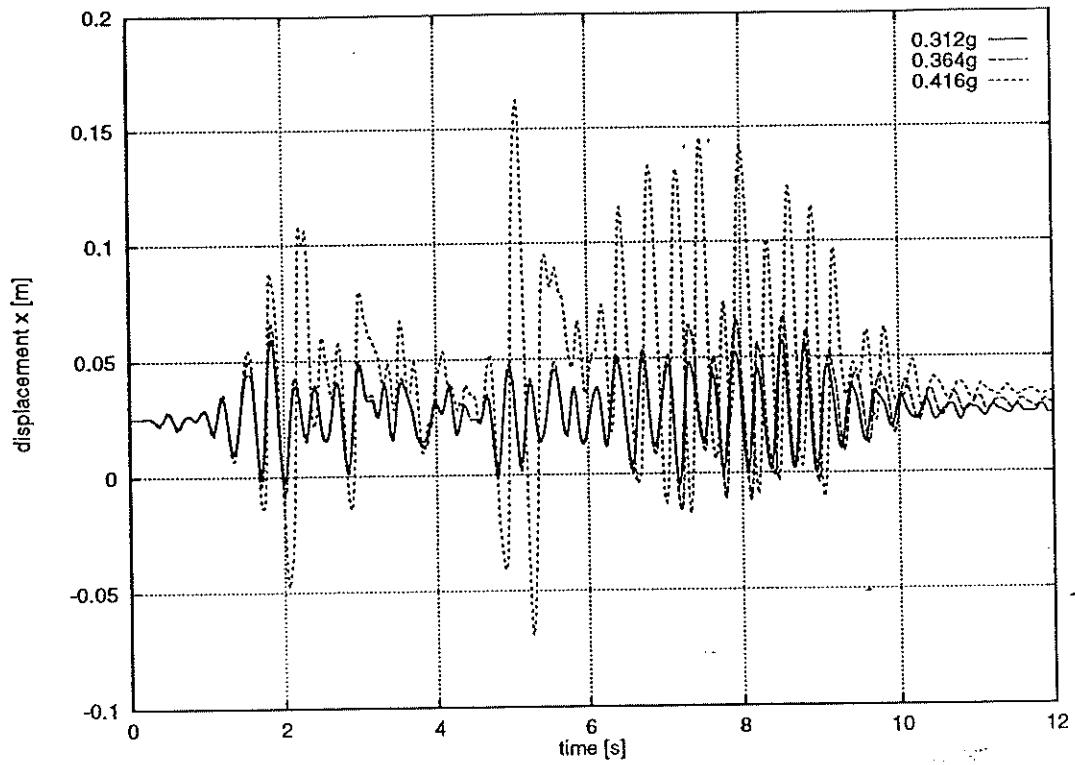


Figure 12. Talvacchia Dam. Horizontal displacement at the top of the central cantilever for different intensity factors

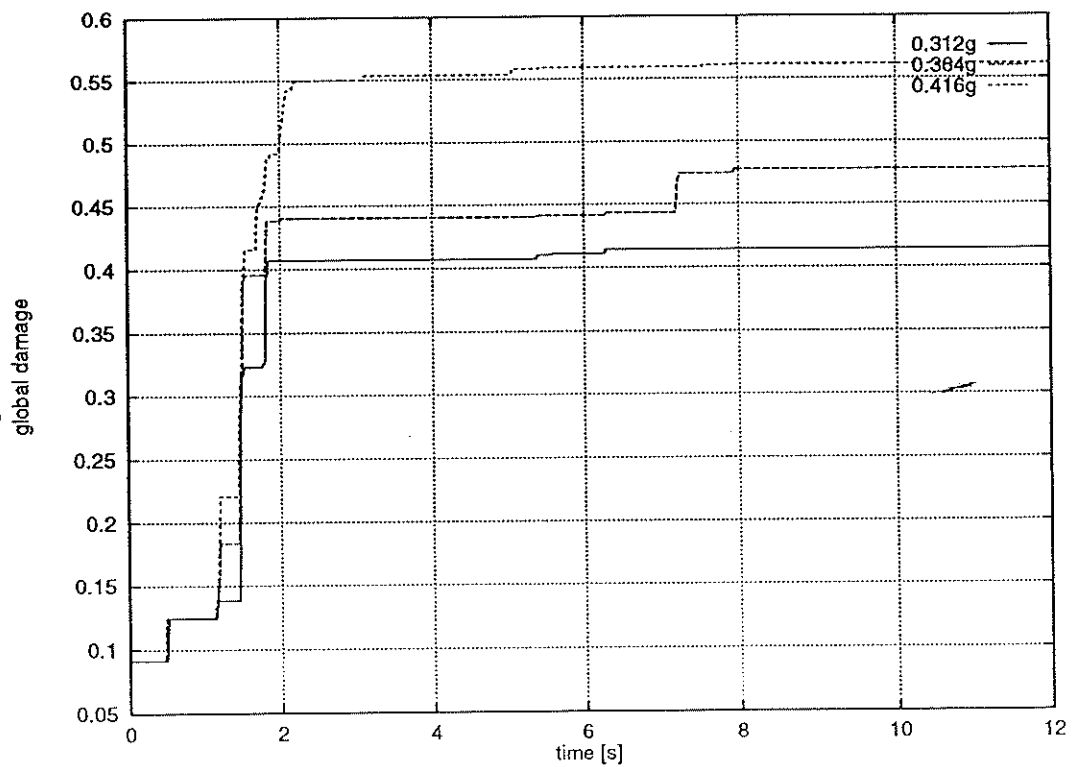


Figure 13. Talvacchia Dam. Evolution of the global (mean square value) damage for different intensity factors

REFERENCES

- 1 L. M. Kachanov, 'Time of rupture process under creep conditions'. *Izvestia Akademii Nauk, Otd Tech Nauk.*, **8**, 26-31 (1958).
- 2 J. Lemaitre and J. L. Chaboche, 'Aspects Phénoménologiques de la Rupture par Endommagement'. *J. Méc. Appl.*, Vol. **2**, **3**, 317-365 (1978).
- 3 J. Lemaitre, 'How to use Damage Mechanics'. *Nuclear Eng. and Design*, **80**, 233-245 (1984).
- 4 J. C. Simo and J. W. Ju, 'Strain- and Stress-Based Continuum Damage Models – I. Formulation'. *Int. J. Solids Structures*, Vol. **23**, **7**, 821-840 (1987).
- 5 J. C. Simo and J. W. Ju, 'Strain- and Stress-Based Continuum Damage Models – II. Computational aspects'. *Int. J. Solids Structures*, Vol. **23**, **7**, 841-869 (1987).
- 6 J. L. Chaboche, 'Continuum Damage Mechanics: Part I – General Concepts'. *J. Appl. Mechanics*, **55**, 59-64 (1988).
- 7 J. L. Chaboche, 'Continuum Damage Mechanics: Part II – Damage Growth'. *J. Appl. Mechanics*, **55**, 65-72 (1988).
- 8 J. Mazars and G. Pijaudier-Cabot, 'Continuum Damage Theory – Application to Concrete'. *J. of Eng. Mech., ASCE*, Vol. **115**, **2**, 345-365 (1989).
- 9 J. Oliver, M. Cervera, S. Oller and J. Lubliner, 'Isotropic Damage Models and Smeared Crack Analysis of Concrete'. *Proc. 2nd Int. Conf. on Computer Aided Analysis and Design of Concrete Structures.*, 945-957, Pineridge Press (1990).
- 10 C. A. Felippa and K. C. Park, 'Staggered transient analysis procedures for coupled mechanical systems: Formulation'. *Com. Meth. Appl. Mech. and Engng.*, **24**, 61-111 (1980).
- 11 D. K. Paul, *Efficient Dynamic Solutions for Single and Coupled Multiple Field Problems*. Doctoral Thesis, University of Wales (1982).
- 12 M. Galindo, *Una metodología para el análisis numérico del comportamiento resistente no lineal de presas de hormigón con cargas estáticas y dinámicas*. Doctoral Thesis, Technical University of Catalonia (1993).
- 13 R. Codina, M. Cervera and M. Galindo, 'On the efficiency of block-iterative algorithms for two nonlinear coupled problems', *Proceedings of the II Asian-Pacific Conference on Computational Mechanics*, 1241-1246, Balkema (1993).
- 14 M. Galindo, M. Cervera and J. Oliver, 'Efficient solution schemes for fluid-structure-soil interaction problems', *Proceedings of 10th World Congress on Earthquake Engineering*, 4651-4656, Balkema (1991).
- 15 O. Z. Zienkiewicz and R. L. Taylor, *The finite element method*. McGraw Hill (1991).
- 16 T. J. R. Hughes, *The Finite Element Method: Linear Static and Dynamic Finite Element Analysis*. Prentice-Hall International (1987).
- 17 T. J. R. Hughes, K. S. Pister and R. L. Taylor, 'Implicit-explicit finite elements in nonlinear transient analysis'. *Comp. Meth. Appl. Mech. Engng.*, **17/18**, 159-182 (1979).
- 18 S. S. Bhattacharjee and P. Léger, 'Seismic cracking analysis and energy dissipation in concrete gravity dams.' *Earth. Engng. Struc. Dyn.*, **22**, 991-1007 (1980).
- 19 R. Faria and J. Oliver, *A Rate Dependent Plastic-Damage Constitutive Model for Large Scale Computations in Concrete Structures*. Monography CIMNE, N. 17. (1993).

- 20 M. Galindo, M. Cervera and J. Oliver, 'Parallel Synchronized Communication: an algorithmic approach to coupled problems'. *Proceedings of the International Conference on Numerical Methods in Engineering and Applied Sciences*, 389-398, CIMNE (1992).
- 21 O. C. Zienkiewicz, D. K. Paul and A. H. C. Chan, 'Unconditionally stable staggered solution procedures for soil-pore fluid interaction analysis'. *Int. J. Num. Meth. Eng.*, **19**, 1669-1673 (1986).
- 22 A. H. C. Chan, *A unified Finite Element Solution to Static and Dynamic problems of Geomechanics*. Doctoral Thesis, University of Wales (1988).
- 23 K. Wisniewski, E. Turska, L. Simoni and B. A. Schrefler, 'Error analysis of staggered predictor-corrector scheme for consolidation porous media', *The Finite Element Method in the 1990's*. Springer-Verlag/CIMNE (1991).
- 24 M. Cervera, R. Codina and M. Galindo, *On the computational efficiency and implementation of block-iterative algorithms for nonlinear coupled problems*, Research Report CIMNE, N. 43. (1994).
- 25 O. C. Zienkiewicz, R. W. Clough and H. B. Seed, *Earthquake analysis procedures for concrete and earth dams*, Research Report INME, C/R/457/83 (1984).
- 26 M. Fanelli, 'The safety factor of dams - an abstract concept or a measurable quantity?'. *Dam Engineering*, Vol. II, **2**, 97-99 (1991).