

A machine learning based approach to predict the stress intensity factors in 2D linear elastic fracture mechanics

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Within the framework of linear elastic fracture mechanics, the stress intensity factors (SIFs) are the mostly applied crack-tip characterizing parameters. To obtain the SIFs, approximate formulae are widely used because exact analytical solutions are available only for very simple geometrical and loading configurations [1]. However, even approximate solutions for SIFs are also rather limited to very simple geometrical and loading conditions. In this work, an accurate and efficient SIF prediction model based on Physics-informed neural network (PINN) [4] is developed, where we incorporate the equilibrium equations and constitutive relations into the PINN. In order to capture the singular behavior of the stress and displacement fields around the crack-tip, we extend the standard PINN structure by including the crack-tip asymptotic functions such that the singular solutions at the crack-tip region can be modeled accurately. Then the enhanced Physics-informed neural networks are trained to satisfy the governing equations and the corresponding boundary conditions.

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