

# NUMERICAL PREDICTION OF A LARGE BUBBLE BEHAVIOR IN WALL TURBULENT FLOW

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**Abstract.** Air lubrication systems for underwater applications have gained great popularity in recent years. Large bubbles, around  $We \geq 100$ , show a large area of drag reduction than a small and microbubble, especially for large scale flow problems such as ship surface. However, it is hard to maintain their shape and prone to deform in a turbulent flow. In order to understand and control the drag reduction mechanism by the large bubble injection, it is necessary to know the behavior of large bubbles in the turbulent boundary layer and their interaction with the skin friction. In this study, a solver “*interIsoFoam*” for two-phase flow of an open-license software “*OpenFOAM*” is applied for an LES of turbulent channel flow with a large bubble, the gas-liquid interface of which is directly captured by improved VOF method. In a recent publication [1], we presented the numerical procedure of how to inject the large bubble on turbulent channel flow. The research objectives in this study are investigation on flow change of the horizontal channel flow included large bubble. From this observation, understanding large bubbles characteristic such as the surrounding flow phenomena was observed.

## 1 INTRODUCTION

As growing the attention of global warming all around the world, the IMO released the requirement on the ship’s greenhouse gas emission. To comply with increasing EEDI Phase 3 levels, the air lubrication system is one of the technologies to achieve it and developed to meet the industry need [2]. This system can be categorized into two main categories, the microbubble method started by McCormick and Bhattacharyya [3] and the air-film method (Fukuda et al., [4][5]). Recently, the above-mentioned two methodologies have the same issue on a decrease of drag reduction performance from downstream because of the large bubble. Meanwhile, Murai et al. [6][7] reported the drag reduction mechanism for these bubbles (10-50mm) and motivated a turning point in the drag reduction of the large bubble, as a new material for drag reduction. In addition, The advantage is that supplying a large bubble is much easier than generating a high flow rate of microbubbles or stabilizing air films with a wide area. Oishi and Murai [8] investigated and depicted detailed characteristics related to

drag reduction by measuring the single large bubble. Kim et al. [1] established a numerical procedure how to inject a large bubble on turbulent channel flow and investigated the behavior of a large bubble with wall turbulent flow. Interestingly, the vortical structures showed between the bubble and upper wall on the liquid film and secondary flow. In this study, a numerical simulation of the turbulent channel flow containing a large bubble is carried out, we investigate the flow field around the bubble and the mechanism of generating vortical structure.

## 2 NUMERICAL METHOD

### 2.1 Governing equations

In this study, the flow is considered incompressible and the fluids are considered Newtonian. The governing equations in this study for continuity and momentum equation can be expressed by Eq. (1) and (2), respectively, and the mass conservation equation is presented in Eq. (3).

$$\frac{\partial \alpha}{\partial t} + \nabla \cdot (\alpha \mathbf{u}) = 0 \quad (1)$$

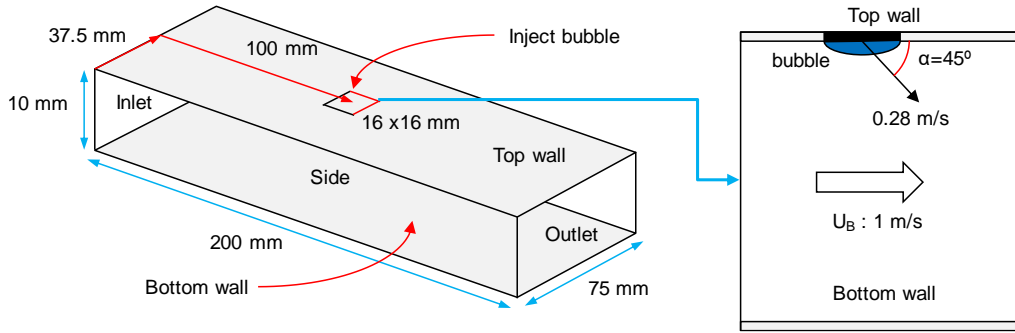
$$\frac{\partial \rho \mathbf{u}}{\partial t} + \nabla \cdot (\rho \mathbf{u} \mathbf{u}) = -\nabla \cdot p + \nabla \cdot \mathbf{T} + \rho \mathbf{f} + \mathbf{f}_\sigma \quad (2)$$

$$\nabla \cdot \mathbf{u} = 0 \quad (3)$$

where  $\rho$  is the fluid density,  $\mathbf{u}$  is the velocity vector,  $p$  is the pressure,  $\mathbf{T}$  is the viscous stress tensor,  $\mathbf{f}$  represents the body forces, and  $\mathbf{f}_\sigma$  is the surface tension force. In this study, the body forces include gravity and a pressure gradient in the streamwise direction. In two-phase flow, the continuity equation is introduced density term,  $\alpha$ , to define a discontinuity of density at the interface. From *interIsoFoam*, the *isoAdvector* algorithm applied introduces a sub-grid scale model for estimating intracellular distribution from the given volume fraction data to capture this local distribution information to keep the density field sharp and bounded. Further information on the *isoAdvector* algorithm is provided in Gamet et al. [9].

### 2.2 Numerical setup

The numerical condition and method in this study were reported by Kim et al. [1] based on Oishi and Murai [8], shown in Tables 1 and 2. In addition, the geometrical configuration of the computational domain is presented in Fig. 1, the size of the domain is 10 mm high ( $H = 2h$ ), 75 mm wide, and 200 mm long between two horizontal walls. The flow is driven from the whole region by a mean pressure gradient. In addition, injecting condition is located 100mm from upstream with a rectangular shape, at the upper wall. Table 3 shows the procedure of numerical simulation is divided into 3 stages to inject and maintain a large bubble successfully, and the detail is described in Kim et al [1]. In all cases, bubbles are added after turbulent channel flow, which is generated by *pimpleFoam* of *OpenFOAM*, then bubble simulation is performed through *interIsoFoam*.



**Figure 1:** Computational domain and Boundary condition [9].

**Table 1:** Numerical condition [1].

Channel	Present CFD
Size(mm)	10 × 75 × 200
Condition	Water (17°C)
$\rho$ (kg/m <sup>3</sup> )	998.7
$\nu$ (m <sup>2</sup> /s)	1.08 × 10 <sup>-6</sup>
$U_{mean}$ (m/s)	1.06
$Fr$ (-)	3.19
$Re$ (-)	9260
$Re_{\tau}$ (-)	260

**Table 2:** Numerical method [1].

	Detail properties
Turbulent model	Large eddy simulation (WALE)
Gradient terms ( $\nabla\phi$ )	Gauss linear
Divergence terms ( $\nabla \cdot \phi$ )	Gauss vanLeer
	Gauss interface Compression
	Gauss limited Linear
Time derivative terms ( $\frac{\partial}{\partial t} \phi$ )	Backward (2nd-order implicit)
Pressure-velocity coupling	Pimple Algorithm

**Table 3:** Boundary condition in each stage. [1]

	Stage 1		Stage 2		Stage 3
Solver	<i>PimpleFoam</i>	→	<i>InterIsoFoam</i>		<i>InterIsoFoam</i>
Inlet	<i>Cyclic with Outlet</i>	→	<i>Fixedvelocity</i>	→	<i>Cyclic with Outlet</i>
Outlet	<i>Cyclic with Inlet</i>	→	<i>InletOutlet</i>	→	<i>Cyclic with Inlet</i>
Side	<i>Cyclic between Left and Right</i>				
Bottom	<i>Noslip</i>	→	Contact angle (1°)		
Top	<i>Noslip</i>	→	<i>Codestream for Injection of bubble</i>	→	Contact angle (1°)

### 3 NUMERICAL RESULTS AND DISCUSSION

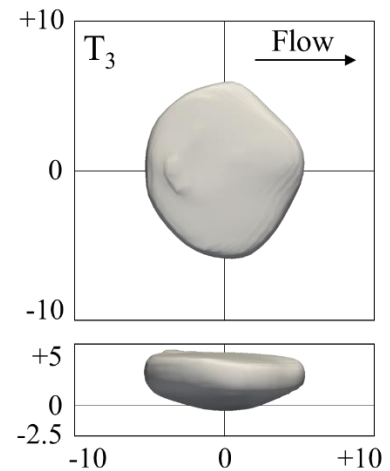
The general properties and shape of bubbles are summarized in Table. 4 and Fig. 2. In the table, the diameter is calculated by the bubble's volume, which is evaluated from the numerical simulation. In addition, Weber number, which characterizes the deformation of the bubble, is defined as:

$$We = \frac{\rho U_b^2 d}{\sigma} \quad (4)$$

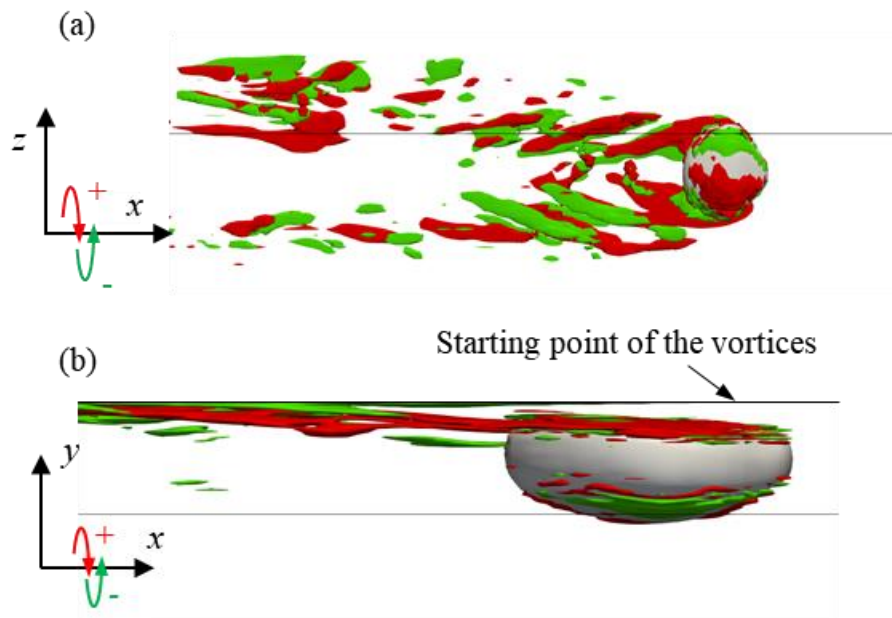
In the case of shape factor, it is defined as  $l_1/l_2$ ,  $l_1/b$ ,  $l_2/b$ , where  $l_1$  and  $l_2$  are streamwise and spanwise length,  $b$  is the height of the bubble, respectively. In the case of the bubble shape, The interface stretched to streamwise and spanwise directions, and the thickness of the liquid film gradually decreased in the direction of the rear of the bubble. The comparison of bubble shape as the series of samples was explained in Kim et al. [1].

**Table 4:** Summary of bubble parameters. [1]

		Present CFD
Weber number		168
Diameter [mm]		9.6
Bubble velocity [m/s]		1.11
Shape factor	$l_1/l_2$	0.90
	$l_1/b$	2.66
	$l_2/b$	2.97



**Figure 2:** The bubble shape / top and side view from Kim et al. [1].



**Figure 3:** Snapshots on Iso-surface of vorticity streamwise component; (a) Bottom view, (b) Side view from Kim et al. [1].

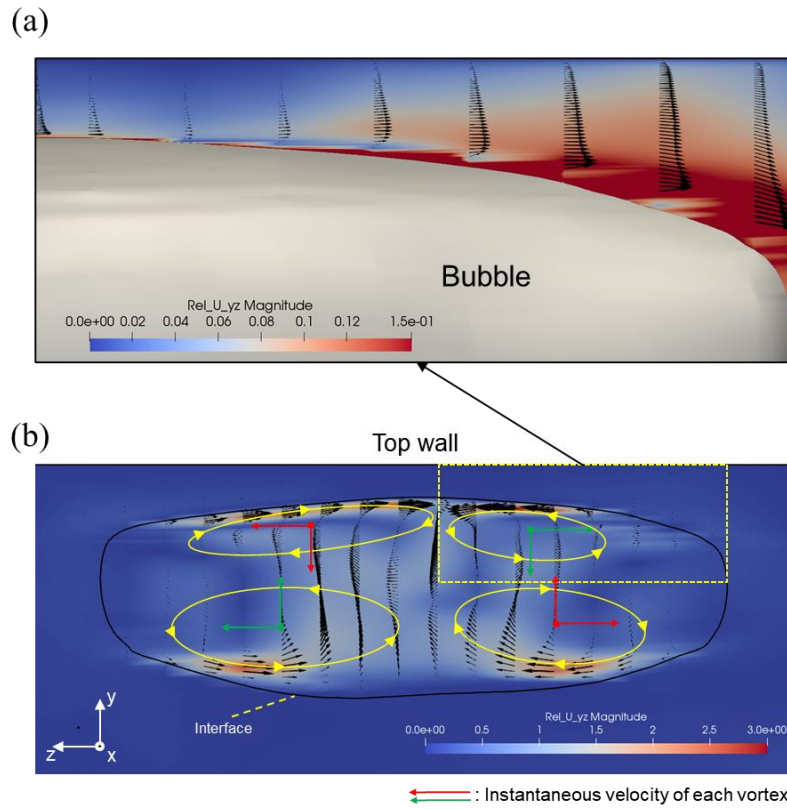
Fig. 3 show the iso-surface of vorticity in streamwise component around the bubble. The vorticity values are  $\pm 330$ , visualized from the side and bottom view. The counter-rotating vortices are developed around the centroid of the bubble. Simultaneously, the counter-rotating vortices are also developed at the same side, but the size of the pairs is unequal as shown in Fig. 3(a). From Fig.3(b), the origin of these vortices can be observed from the wall and bubble interface. These vortices spread widely then separate with forming horseshoe vortices. In the horseshoe vortices of the same side, the positions of these structures are corresponding with each other and the tilting angle of vortices is  $\pm 25^\circ$ . The sequence of generating these vortices was discussed in detail by Kim et al. [1]. This means that the current size of the bubble turns the flow condition below the buffer layer into the turbulent regime. The reason why vortices are generated can be explained by the instantaneous velocity from the section view of the bubble. Figs. 4 and 5 show the velocity vector contours on the front and side view and obtained from the centroid of the bubble. The vector is originated from the relative velocity, expressed as:

$$\mathbf{u}(x, y, z) = \mathbf{u}_0(x, y, z) - \mathbf{u}_{mean}(x, y, z), \quad \mathbf{u}_{mean}(x, y, z) = (1, 0, 0) \quad (5)$$

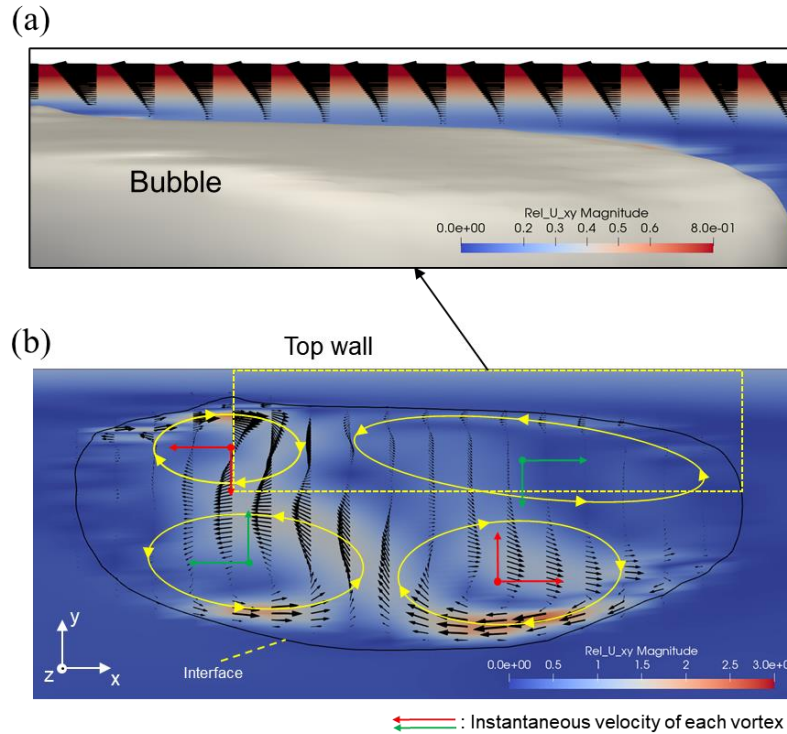
where  $\mathbf{u}_0$  is velocity vector,  $\mathbf{u}_{mean}$  is target velocity of the pressure gradient in the streamwise direction. Fig. 4 shows the velocity vector contour from the front view, the vector is obtained from  $y$  and  $z$  components. we can clearly observe four vortexes inside the bubble. Based on the rotating direction, the pair of vortices at the same height which rotates in counter-direction caused instantaneous velocity heads outside of the bubble, while the pair of vortices at the same width generated instantaneous velocity heads center of the bubble. This feature also shows from Fig.5 which visualized the vector contour of  $x$  and  $y$  components from the side view. Thus, we can understand the reason why large bubble extends streamwise and spanwise direction that wall-normal direction. In the case of the velocity contour at the liquid film, the velocity in the spanwise direction head for outside as shown in Fig. 4(a). In addition, its magnitude value increase as the location change to outside in the spanwise direction. This generates the vortices in a streamwise direction. This is the opposite direction of velocity vectors inside the bubble where is near the liquid film. In the case of velocity contour at the liquid film in the streamwise direction, the velocity gradually increases as the location changes to the rear direction as shown in Fig. 5(a). This increase in the relative velocity may influence the drag reduction on the wall.

#### 4 SUMMARY AND CONCLUSIONS

We investigated large bubble behavior in wall turbulent flow of a horizontal channel flow. It can be achieved by the basis of the previous study, and the previous study was observed the characteristics of a large bubble such as bubble shape and vortical structure around the bubble. To investigate these features, the present work was visualized in two parts; inside of the bubble for understanding bubble shape and the liquid film to investigate the mechanism of generation of vortical structure. As a result, some vortexes were observed from inside of the bubble, the instantaneous velocity from the pair of vortices maintains the bubble shape like a plate. In the case of the liquid film, the bubble-induced spanwise velocity was generated, and this became the source to generate a vortical structure and persisted to the wake.



**Figure 4:** Velocity contour from front view (a) liquid film region, (b) internal region of the bubble.



**Figure 5:** Velocity contour from side view (a) liquid film region, (b) internal region of the bubble.

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