ADAPTIVE TWO-PHASE PARTICLE FINITE ELEMENT MODEL FOR SOFT SOIL EXCAVATIONS IN PARTIALLY SATURATED SOILS

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Abstract. A coupled solid velocity-water pressure (vp) Particle Finite Element (PFEM) formulation in conjunction with a hypoplastic model for sandy soils is presented. Large deformations of the soil and the ever-evolving topology of the ground free surface, key features characterizing the cutting tool-soil interaction, are efficiently captured via the PFEM. The utilization of a hypoplastic constitutive formulation allows for the realistic modeling of the non-linear behavior of the soil deformable skeleton. The hydromechanical description of the partially saturated soft soil is completed by incorporating the van Genuchten hydraulic model for the calculation of the Soil Water Retention Curve (SWRC) in combination with the Karman-Cozeni equation for the estimation of the soil permeability. Finally, computational simulations of tool-soil interaction performed in sand are compared against experiments and the capabilities of the proposed model are demonstrated.

1 INTRODUCTION

Tool-soil interactions in water-saturated soft soils are relevant in a variety of engineering activities such as agricultural tillage, submarine dredging and mechanized tunneling for underground constructions. The efficiency of these operations are largely dependent on the torque and energy requirements of the cutting tools and the tool wear during the excavation of the ground. Computational methods open possibilities for a detailed investigation of different aspects connected with the hydromechanical behavior of fully or partially saturated soil during the tool-soil interaction, e.g. ground deformations, effective stresses and pore pressure distributions in the ground. Additionally, reaction forces generated on the cutting tool in dependence of the soil properties and operational parameters

of the excavation procedure are easily obtainable. This information can be subsequently utilized in the design of more efficient and durable cutting tools with optimal geometry and configuration which may result in substantial improvements in the excavation operation as a whole.

In this contribution, a two-phase Particle Finite Element (PFEM) [1] numerical model suitable for the analysis of tool-soil interactions in partially saturated soils is presented. The tool-soil interactions are characterized by very large soil deformations, continuously changing spatial boundaries and the development of localized shear deformations in the ground, which are properly handled by the PFEM. The non-linear mechanical response of the soil skeleton is modeled by means of a hypoplastic formulation for granular materials. The hydraulic behavior of the partially saturated soil mixture is described by appropriate constitutive relations characterizing the degree of saturation and the saturated hydraulic conductivity of the soil. The capabilities and limitations of the proposed hypoplastic two-phase PFEM model are demonstrated by means of computational re-analyses of laboratory tests of tool-soil interaction performed with an in-house excavation device in initially fully saturated sand. Computed and measured results pertaining to the topology of the excavated ground and the reaction forces on the cutting tool are compared and discussed.

2 NUMERICAL MODEL

2.1 Velocity-pressure Particle Finite Element formulation

A coupled two-phase PFEM model, based on the three-phase FEM formulation for partially saturated soils proposed in [2] is developed using a passive air phase approach. The balance of momentum equation of the mixture, written in Updated Lagrangian (UL) format, reads

where $\dot{\mathbf{v}}_s$ is the material time derivative of the soil skeleton velocity, $\nabla \cdot \boldsymbol{\sigma}$ the divergence of the total Cauchy stress tensor, $\nabla = \frac{\partial(\cdot)}{\partial \mathbf{x}}$ the spatial gradient operator, $\mathbf{x}$ the vector of spatial coordinates, t the time, $\rho \mathbf{b}$ the vector of body force, $\rho = (1 - n)\rho_s + n\rho_w$ is the averaged density of the mixture, ρ_s , ρ_w the intrinsic densities of the solid and water constituents, respectively, and n the porosity of the medium.

In this work, the two-phase PFEM model is coupled to a hypoplastic constitutive formulation which also incorporates the void ratio of the soil as state variable. Therefore, the porosity is computed in terms of the void ratio e via the expression

$$n = \frac{e}{1 + e}, \quad (2)$$

where e is computed by means of the following evolution equation

$$\dot{e} = (1 + e)\text{tr}(\mathbf{d}). \quad (3)$$

In Eq. (3), $\mathbf{d} = \frac{1}{2} (\nabla \mathbf{v}_s + \nabla \mathbf{v}_s^T)$ is the rate of deformation tensor.

The mass balance equation for the fluid phase is given as

$$n \frac{\partial S_w}{\partial t} + \nabla \cdot \hat{\mathbf{v}}_{ws} + S_w \nabla \cdot \mathbf{v}_s = 0. \quad \text{in } \Omega \quad (4)$$

where S_w is the degree of water saturation of the soil mixture and $\hat{\mathbf{v}}_{ws}$ the averaged relative flow velocity, computed with the help of Darcy's law as

$$\hat{\mathbf{v}}_{ws} = -\frac{k_w}{\rho_w g} (\nabla p_w - \rho_w \mathbf{g}), \quad (5)$$

with k_w as the hydraulic conductivity of the water phase (given in m/s) and $g = \|\mathbf{g}\|$.

The governing equations (1) and (4) are supplemented by the following boundary conditions

$$\mathbf{v}_s - \hat{\mathbf{v}}_s = \mathbf{0}, \quad \text{on } \Gamma_v, \quad (6)$$

$$\boldsymbol{\sigma} \cdot \mathbf{n} - \hat{\mathbf{t}} = \mathbf{0}, \quad \text{on } \Gamma_\sigma, \quad (7)$$

$$p_w - \hat{p}_w = 0, \quad \text{on } \Gamma_p, \quad (8)$$

$$\hat{\mathbf{v}}_{ws} \cdot \mathbf{n} - \hat{q} = 0, \quad \text{on } \Gamma_q, \quad (9)$$

where $\mathbf{n}$ is the outward normal vector on the boundary, and $\hat{\mathbf{v}}_s$ and $\hat{\mathbf{t}}$ are the velocity and traction vectors prescribed on their respective boundaries Γ_v, Γ_σ , respectively and $\hat{p}_w$ and $\hat{q}$ are the water pressure and flux prescribed on Γ_p, Γ_q , respectively.

The spatial discretization of the governing equations is accomplished by the Finite Element Method. Test functions and the primary field variables of the formulation are approximated in terms of nodal values (denoted with an upper bar ($\bar{\cdot}$)) as

$$\mathbf{v}_s \approx \sum_{I=1}^{NN} N_I \bar{\mathbf{v}}_{sI}, \quad p_w \approx \sum_{I=1}^{NN} N_I \bar{p}_{wI}, \quad (10)$$

$$\delta \mathbf{v}_s \approx \sum_{I=1}^{NN} N_I \delta \bar{\mathbf{v}}_{sI}, \quad \delta p_w \approx \sum_{I=1}^{NN} N_I \delta \bar{p}_{wI}, \quad (11)$$

where N_I are linear shape functions associated with node I and NN is the number of nodes per element. In this work, 3-node linear triangles (containing one Gauss point per element) are used for 2D analyses.

The semi-discrete element residuals obtained from Eqs. (1) and (4) are integrated over

the current element domain Ω_n^e and written in matrix notation as

$$\begin{aligned} {}_e\mathbf{R}_v^{n+1} &= \int_{\Omega_n^e} \mathbf{N}_v^T \rho \mathbf{N}_v d\Omega_n^e \dot{\mathbf{v}}_s + \int_{\Omega_n^e} \mathbf{B}^T \boldsymbol{\sigma}' d\Omega_n^e - \int_{\Omega_n^e} \mathbf{B}^T S_w \mathbf{1} \mathbf{N} d\Omega_n^e \bar{\mathbf{p}}_w \\ &\quad - \int_{\Omega_n^e} \mathbf{N}_v^T \rho \mathbf{b} d\Omega_n^e - \int_{\Gamma_e^n} \mathbf{N}_v^T \hat{\mathbf{t}} d\Gamma_e^n = \mathbf{0}, \end{aligned} \quad (12)$$

$$\begin{aligned} {}_e\mathbf{R}_p^{n+1} &= - \int_{\Omega_n^e} \mathbf{N}^T n \frac{\partial S_w}{\partial p_c} \mathbf{N} d\Omega_n^e \dot{\mathbf{p}}_w + \int_{\Omega_n^e} \mathbf{N}^T S_w \mathbf{1}^T \mathbf{B} d\Omega_n^e \bar{\mathbf{v}}_s - \int_{\Omega_n^e} \nabla \mathbf{N}^T \hat{\mathbf{v}}_{ws} d\Omega_n^e, \\ &\quad + \int_{\Gamma_e^n} \mathbf{N}^T \hat{\mathbf{q}} d\Gamma_e^n + {}_e\mathbf{f}_{\text{stab}}^{n+1} = \mathbf{0}, \end{aligned} \quad (13)$$

where $\mathbf{N}_v$ and $\mathbf{N}$ are matrices containing the shape functions, $\mathbf{B}$ denotes the strain-displacement matrix computed in the current configuration, $\boldsymbol{\sigma}'$ is the Cauchy effective stress, $p_c = -p_w$ the capillary pressure and ${}_e\mathbf{f}_{\text{stab}}^{n+1}$ the element stabilization vector defined in this work based on the Fluid Pressure Laplacian (FPL) stabilization procedure for partially saturated media, proposed in [3].

The temporal discretization of the semi-discrete balance of momentum equation is performed via the α -Bossak integration scheme [4]. The rate of the water pressure $\dot{\mathbf{p}}_w$ in the mass balance equation is approximated via

$$\dot{\mathbf{p}}_w \approx \frac{\Delta \mathbf{p}_w^{n+1}}{\Delta t} = \frac{\mathbf{p}_w^{n+1} - \mathbf{p}_w^n}{\Delta t}. \quad (14)$$

The incremental solution of the coupled equations (12) and (13) is performed monolithically by means of an Newton-Rapshon procedure. The nodal increments of the velocities of the solid matrix and the fluid pressures are obtained after iteratively solving the following assembled linearized system

$$[\mathbf{K}]_{n+1}^i \begin{bmatrix} \Delta \bar{\mathbf{v}}_s \\ \Delta \bar{\mathbf{p}}_w \end{bmatrix}_{n+1}^{i+1} = - \begin{bmatrix} \mathbf{R}_v \\ \mathbf{R}_p \end{bmatrix}_{n+1}^i, \quad (15)$$

with i as the current iteration number, $\mathbf{K}^{n+1}$ the system tangent matrix and $\mathbf{R}_v^{n+1}$, $\mathbf{R}_p^{n+1}$ the assembled residual vectors of Eqs. (12) and (13).

Equation (15) has been numerically solved with an iterative Biconjugate Gradient Solver (BiCGS) in combination with an Incomplete LU factorization (ILU) preconditioner.

2.2 The Particle Finite Element method

The PFEM [1] is an Updated Lagrangian global re-meshing procedure suitable for the robust numerical analysis of solid and fluid problems characterized by large deformation and strains, using a FEM-based solution approach. In particular, the Lagrangean nature of the method provides the PFEM with superior capabilities in the treatment of evolving spatial boundaries and substantial changes in the topology of the spatial domain. In

this method, the spatial discretization of the problem is accomplished by means of nodes (denoted as particles) which are allowed to move freely according to the solution of the governing equations. These equations are solved in a time-staggered fashion using standard FEM procedures with the help of a computational mesh. After each solution step, the elements comprising the mesh are cleared and the information of kinematic and state variables is transferred to the nodes.

In standard versions of the PFEM, the finite elements are generated by means of the Extended Delaunay Tessellation (EDT) technique [5]. The EDT is a mesh triangulation procedure that enforces the generation of well-shaped elements with optimal aspect ratios and maximal internal angles. After construction of the mesh, domain boundaries are detected by means of the α -shape technique [5], where elements are preserved or discarded on the basis of a geometric criterion involving their characteristic length. This procedure is performed at each time step, thus allowing to efficiently capture complex boundaries and evolving free surfaces.

During the excavation process of highly compacted soils, localized deformations of the ground in the form of shear bands, may propagate from the cutting tool towards the free surface. To enhance the capabilities of the PFEM concerning the representation of these shear bands, a local adaptive mesh refinement strategy is implemented. In this approach, nodes are inserted in the mesh according to the activation of a soil dilatation criterion, designed to track the development of strain localization patterns in the soil, based on the relative increase of the void ratio e at time t^{n+1} with respect to e_0 , given by

$$\frac{\Delta e^{n+1}}{e_0} = \frac{e^{n+1} - e_0}{e_0} \geq \alpha_{\text{dil}}, \quad \text{Activation of mesh refinement} \quad (16)$$

where (α_{dil}) is the activation threshold value. In the presented simulations, $\alpha_{\text{dil}} = 4.5\%$.

In this work, the tool-soil frictional interface is modeled by means of special contact elements using the Continuum Constraint Method (CCM) [6]. In the CCM, the elements discretizing the contact interface are of the same kind and order of those comprising the main domain (i.e. linear triangular elements in 2D) and the contact behavior is reflected only at the constitutive level. In this sense, the response of contact elements is modeled using a different material model and properties different from those employed for the discretization of the domain.

2.3 Constitutive relations

The determination of the degree of water saturation S_w of the soil mixture is accomplished by means of a Soil-Water Characteristic Curve (SWCC) according to the van Genuchten model [7]. The SWCC relates S_w to the matrix suction h_{suc} (utilized herein in cm)

$$S_w = S_w^r + \frac{S_w^s - S_w^r}{(1 + (\alpha_{vg} h_{\text{suc}})^n)^m}, \quad (17)$$

where S_w^r and S_w^s denote, the residual and maximum saturation degrees, respectively, α_{vg} and n are independent parameters to be calibrated from hydraulic experimental data of the soil and $m = 1 - \frac{1}{n}$.

The hydraulic conductivity of the partially saturated porous medium $k_w = k_w^r k_w^{\text{sat}}$ is obtained from the scaling of its saturated value k_w^{sat} by the relative permeability coefficient k_w^r . The saturated hydraulic conductivity is estimated in accordance to the Kozeni-Carman permeability model [8], given here in terms of the void ratio e ,

$$k_w^{\text{sat}} = C \frac{g}{\rho_w \mu_w} \frac{e^3}{S^2 G_s^2 (1 + e)}, \quad (18)$$

where C is the shape factor of the particles, $G_s = \frac{\rho_s}{\rho_w}$ is the specific gravity of the soil grains and μ_w the dynamic viscosity of the water ($\mu_w = 1 \times 10^{-3}$ Pa·s at 20°C).

The relative hydraulic conductivity, on the other hand, is computed in terms of the effective degree of saturation S_w^e as

$$k_w^r = \sqrt{S_w^e} \left[1 - \left(1 - (S_w^e)^{\frac{1}{m}} \right)^m \right]^2, \quad (19)$$

with $S_w^e = \frac{S_w - S_w^r}{S_w^s - S_w^r}$.

For the deformable soil skeleton, the hypoplastic formulation for granular materials proposed by Von Wolffersdorff [9], is utilized for the characterization of effective stresses. In this constitutive model, the non-linear behavior of the soil skeleton is captured by means of the following tensorial rate form

$$\dot{\boldsymbol{\sigma}}' = f_b f_e (\mathbf{L} : \mathbf{d} + f_d \mathbf{N} ||\mathbf{d}||), \quad (20)$$

where $\mathbf{L}$ and $\mathbf{N}$ are fourth-order and second-order constitutive tensors, respectively, and f_b and f_e are scalar functions utilized to account for the non-linear dependence of the soil stiffness on the mean skeleton pressure and the soil density, respectively. The factor f_d is utilized to reproduce the volumetric dilatancy observed in dense specimens.

3 COMPUTATIONAL SIMULATION OF EXCAVATION OF SANDY SOIL

3.1 Experimental setup and material parameters

An excavation testing device [10] has been designed and constructed at Ruhr University Bochum for the investigation of tool-soil interaction processes in both dry and partially saturated soft soils. It consists of a rectangular soil container (width 23 cm, length 140 cm, height 53 cm) enclosed by transparent plastics (Plexiglass) (see Fig. 1). As excavation tool, a rectangular blade made of Plexiglas with a height of 25 cm is employed. The motion of the blade is controlled by a trolley driven by a stepper motor and supported on dual

rail-linear bearing systems. Additionally, four force transducers mounted on the cutting tool allow for the measurement of the generated reaction forces during the excavation process.

Figure 1: Experimental and numerical analysis of tool-soil interaction in soft soils: a) Schematic illustration of the excavation device; b) PFEM model with geometry and boundary conditions.

The experiments are characterized by horizontally displacing the cutting tool along the length of the soil bin. The maximum horizontal displacement of the tool was approximately 450 mm. The advance velocity of the blade was prescribed as $\hat{v}_x = 12$ cm/s and the penetration depth is fixed to 10 cm. The initial height H_0 of the material for this experiment is approximately 30 cm. The saturation process of the soil was performed by gently pouring water into the container until the water level was slightly above the free ground surface.

The sand used in experiments was Haltener Silbersand with the following granulometric properties: Diameter of the grains 0.06-0.71 mm, uniformity coefficient $C_u = 1.8$ and $d_{50} = 0.23$ mm. The measured friction angle at repose is 33° . The tool-soil interface friction angle is $\delta = 13^\circ$ [10] for dry sand and has been increased to $\delta = 18^\circ$ accounting for the observed increase of the sliding friction coefficient with very high water content in the soil, pointed out in [11]. The minimum and maximum void ratios (at zero mean skeleton pressure) for this sand are $e_{d0} = 0.557$ and $e_{i0} = 0.901$, respectively. The critical void ratio (at zero mean skeleton pressure) is set to $e_{c0} = 0.90$. The sand is assumed to be in a dense state with an initial void ratio $e_0 = 0.66$ (relative density $I_d = 0.70$).

In this work, the hypoplastic parameters for Karlsruhe fine sand (diameter of the grains: 0.06-0.3 mm, $C_u = 1.5$ and $d_{50} = 0.14$ mm) [12] are adopted due to insufficient laboratory data of Silbersand for a proper calibration procedure. These parameters are collected below in Table 1.

It should be noted that, since the soil excavations herein presented are performed at ground level, where effective stresses are comparatively low, we have reduced the granular hardness h_s from its original value i.e. 4×10^9 Pa (calibrated for mean skeleton pressures above 20 kPa), to 2.25×10^7 Pa, as suggested in [13], to mitigate overestimations of ground

Table 1: Hypoplastic parameters utilized for Silbersand. In parentheses ($\cdot$), the value of h_s calibrated for a mean skeleton pressure of $p' > 20$ kPa is included.

φ_c [°]	h_s [Pa]	α_H	n	β_H	e_{i0}	e_{c0}	e_{d0}
33	$2.25 \times 10^7 (4 \times 10^9)$	0.14	0.27	2.5	0.901	0.9	0.557

heaving predicted by the hypoplastic model [13]. The SWCC for Silbersand is generated using the parameters displayed in Table 2, and the saturated hydraulic conductivity k_w has been estimated using Eq. (18).

Table 2: Parameters for the SWCC of Silbersand according to the van Genuchten's model.

e_0	S_s	S_r	α_{vg}	m	n
0.66	1	0.06	0.02913	0.7616	4.1942

3.2 Computational model

A plane-strain PFEM excavation model, shown in Fig. 1 b), has been generated according to the previously described experimental setup. The boundary conditions for the model are applied as follows: The lateral boundaries are fixed in horizontal direction (i.e. $v_x = 0$), whereas the bottom boundary is fixed in both horizontal and vertical directions.

A prescribed velocity of $\hat{v}_x = 12$ mm/s is imposed on the rigid cutting tool. At the free ground surface, a free drainage boundary ($p_w = 0$) is assumed, whereas the side and bottom boundaries are assumed as impervious. The PFEM mesh consists of 19500 linear triangular elements with sizes ranging from 5.5 mm near the cutting tool to 18.5 mm in the right boundary. At the contact interface the elements size is 5 mm. The hypoplastic model is initialized with effective stresses $\sigma'_{y0} = \gamma' z$ and $\sigma'_{x0} = K_0 \sigma'_{y0}$, where z is the depth measured from the free surface and γ' denotes the effective unit weight of the soil sample. The lateral earth pressure coefficient $K_0 = 0.46$ is calculated according to Jaky's formula [14].

3.3 Computed soil deformations and reaction forces on the cutting tool

Figure 2 presents snapshots of the deformed soil for a tool displacement of $S_x = 300$ mm as obtained from the experiment and the numerical simulations using the proposed adaptive PFEM model for fully and partially saturated soft soil. Laboratory results show a staggered topology of the ground free surface. This is produced by the progressive activation of shear bands during the soil cutting process. Numerical predictions concerning the topology of the excavation front qualitatively agree with experiments. In particular,

the two-phase PFEM model is able to capture to a good extent the observed shear bands. Within these shear bands, the soil undergoes dilatation which is then utilized by the adaptive refinement scheme for the insertion of nodes and creation of new elements, as seen in Fig. 2 b). Details are contained in [15].

The height of the excavation pile ahead of the tool obtained in the test and the PFEM analysis are compared. The maximum height in the laboratory test, measured from the base of the tool, is approximately 197.5 mm, whereas the length of the pile, considered from tool-soil interface, is ≈ 404 mm. According to the PFEM model, the maximum height of the pile is 206 mm whereas its length is 345 mm. These results yield relative errors of 4.3 % and 14.6 % for the maximum height and length of the excavation heap, respectively.

Figure 2: Topology of the ground free surface: Snapshots of the excavation front as obtained from a) experiments and b) numerical simulations for a tool horizontal displacement of $S_x = 300$ mm (see also [15]).

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Figure 3 a) illustrates the computed and measured evolutions of tool reaction forces as a function of the horizontal tool displacement, considering the reference simulation case (i.e. using $\varphi_c = 33^\circ$). Measurements from five different experimental runs are displayed in light blue lines. The force-displacement plot indicates, that the reaction forces are increasing according to an oscillatory pattern associated with the sequential activation of shear bands in the soil. In the shear bands, the material locally shows strong dilatation, and intense negative pore pressures develop. The computed reaction forces lie within experimental range, however, the proposed numerical model fails to reproduce the aforementioned oscillatory pattern. This issue might be connected to inherent limitations of the utilized hypoplastic model to fully capture the localized pore pressure variations within the shear deformation bands.

Figure 3: Evolution of the reaction forces on the cutting tool vs. horizontal tool displacement considering different values for the critical internal friction angle: a) $\varphi_c = 33^\circ$ (reference case) and b) $\varphi_c = 23^\circ, 33^\circ$ and 36.5° . (light blue lines: Experiments. Blue, red and black lines: Hypoplastic two-phase PFEM model).

3.4 Influence of the critical friction angle of the soil (φ_c)

The influence of the critical state friction angle of the soil is investigated by comparing two results from numerical analysis using φ_c i.e. 23° and 36.5° , respectively, in Fig. 4. Comparing the topology of the deformed configurations of the sand, a smoother and more continuous free surface is observed for $\varphi_c = 23^\circ$ (left subfigure). As the value of φ_c is increased to 36.5° , two distinctive bumps appear on the ground surface. According to these results, it is apparent that a higher critical state friction angle leads to the development of sharp discontinuities in the ground associated with the sequential activation of shear failure. The top and middle subfigures in Fig. 4 show the resulting ground surface topography at simulations performed with $\varphi_c = 23^\circ$ and 36.5° are ≈ 202 mm and 196 mm, respectively.

The influence of φ_c in the evolution of the tool reaction forces, is examined in Fig. 3b). It shows, that higher critical friction angles of the soil also lead to higher reaction forces in the tool. For the excavation simulation performed with $\varphi_c = 23^\circ$, the computed maximum reaction force is around 403 N, whereas for the reference case ($\varphi_c = 33^\circ$) it is 786 N. Simulations with $\varphi_c = 36.5^\circ$ show higher reaction forces as compared to the reference case during the first 280 mm of tool horizontal displacement.

4 SUMMARY AND CONCLUSIONS

In this contribution, a two-phase PFEM formulation in conjunction with a hypoplastic constitutive model was presented for the analysis of tool-soil interactions in partially saturated soils. For the validation of the model, excavation experiments have been performed in a box filled with initially fully saturated sand. The proposed model has demonstrated good capabilities concerning the prediction of the complex evolution of large deformations of the ground and the evolution of the topology of the ground surface during the

Figure 4: Influence of φ_c on the topology of the deformed soil at a horizontal tool displacement of $S_x = 300$ mm for two different assumptions for the critical friction angle of the soil. a) 23° and b) 36.5° .

excavation. Adopting an adaptive mesh refinement scheme controlled at each time step by the relative increase of the void ratio, it was shown, that the model is able to replicate the sequential appearance of shear bands in the soil. Also, the computed reaction forces generated on the tool have shown a good quantitative agreement with the measured forces. It was found however, that the computed forces do not show the oscillatory pattern observed in the measured reaction force-displacement curve. This issue might be connected to intrinsic limitations of the hypoplastic formulation to fully capture the water pore pressure development. On the other hand, it is also expected that a more accurate characterization of the hypoplastic and hydraulic parameters of the soil may yield improved results. Finally, the influence of the critical friction angle of the material was elucidated. Numerical experiments have shown, that a lower critical friction angle leads to a smoother excavation profile, less pronounced shear bands in the ground and smaller tool reaction forces as compared to the reference analysis using calibrated soil parameters.

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