

# Through-thickness water transport and hygro-expansion in a paper sheet

Nik Dave<sup>†, ¶, \*</sup>, Ron Peerlings<sup>†</sup>, Thierry Massart<sup>¶</sup>, and Marc Geers<sup>†</sup>

<sup>†</sup> Eindhoven University of Technology, 5600 MB, Eindhoven, The Netherlands  
E-mail: [n.dave@tue.nl](mailto:n.dave@tue.nl), [r.h.j.peerlings@tue.nl](mailto:r.h.j.peerlings@tue.nl), [m.g.d.geers@tue.nl](mailto:m.g.d.geers@tue.nl)  
Web page: <https://www.tue.nl/>

<sup>¶</sup> Université Libre de Bruxelles, Avenue F.D. Roosevelt, 50 B-1050, Brussels, Belgium  
E-mail: [thmassar@ulb.ac.be](mailto:thmassar@ulb.ac.be)  
Web page: <http://batir.ulb.ac.be>

\* Corresponding author: [n.dave@tue.nl](mailto:n.dave@tue.nl) (Nik Dave)

## ABSTRACT

Paper, a hydrophilic material, is notably susceptible to deformations due to variations in moisture content, which develop over time. Understanding the moisture transport through the thickness of a paper sheet and the time-dependent mechanics allows us to study the curling behaviour of paper.

In this work, the time-dependent factors involved in deformation of a paper strip that is fully or partially wetted from one side and subjected to different boundary conditions is studied with a 1D numerical model. The different time-scales involved, in the process of imbibition in the inter-fibre pores and absorption (or water uptake) by the fibres, are analysed. The resulting hygro-expansion due to swelling of the wet fibres is then solved to predict the deformation and bending response of the paper strip.

We provide a phenomenological model here to describe the dynamic water flow through the thickness of a paper strip using the unsaturated flow theory. The numerical analysis shows a fair qualitative agreement with experimental observations.

## REFERENCES

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